

Studying the Effects of Incarceration on Offending Trajectories: An Information- Theoretic Approach

*Technical Report Submitted to the
Data Resources Program (DRP),
National Institute of Justice (NIJ)*

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research for safer communities

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Office of Justice Program
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Abstract

Research Goals and Objectives: The main goal of this project was to develop an analytical approach that will enable researchers, analysts, and practitioners to utilize detailed dated criminal history information, when such information is available, in order to investigate whether, and to what extent, incarceration is able to deter offenders from future offending. A secondary goal of the project was to demonstrate the utility of the developed framework by applying it to a real-world dataset.

Research Design and Methodology: The methodology developed in this project builds on two traditions. It uses concepts common to information-theory and event-history analysis. When combined, the resulting framework allows analysts (i) to estimate individual-specific offending micro-trajectories; (ii) to project counterfactual trajectories (i.e., trace out the offending trajectory for each individual had (s)he not been incarcerated); and (iii) to assess the actual post-release offending patterns against the backdrop of these counterfactuals. The information-theoretic underpinnings of the framework also help quantify the extent of deviation between the counterfactual and actual micro-trajectories for each individual. This composite statistic allows one to classify individuals' incarceration as having had a deterrent, an incapacitative or a criminogenic effect on them.

Research Results and Conclusions: Dated arrest histories of a sample of prisoners released from state prisons in 1994, collected by the Bureau of Justice Statistics and publicly archived at ICPSR (Study # 3355), were used to model these trajectories and study their deflection. Estimated models largely confirmed expectations. Upon release, being later in the offending sequence exerted an upward pressure on the risk path (trajectory) relative to what was anticipated and, all else being equal, being closer to prior offending activity exerted a downward pressure on the trajectory relative to the counterfactual. Moreover, a comparison of the counterfactual and actual offending patterns suggests that most releasees were either deterred from future offending (40 percent) or merely incapacitated (56 percent) by their incarceration. About 4 percent had a criminogenic effect.

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Executive Summary

BACKGROUND AND OBJECTIVES

Imprisonment, for any length of time, is a life-interrupting event. The process of reentry into society after a period of incarceration is riddled with questions of individual sustainability, vulnerability, and fear of failure. Therefore, identifying and understanding the effects that incarceration can have on different types of offenders under different contexts is crucial to developing strategies that minimize any criminogenic harm, and maximize any deterrent benefits, that result from it. This report describes an analytical framework designed to aid practitioners, analysts, and researchers in investigating these issues.

It builds on one of the well established and widely accepted empirical regularities in criminology: the link between an individual's past and future crime. Criminologists are not in complete agreement with regard to explanations of this link. However, none deny that such continuity in offending is a very real phenomenon. To the extent that such links exist, studying prior involvement in crime should provide useful insights into future offending patterns. This notion is validated in almost all studies of criminal recidivism—that prior criminal history is one of the best and most consistent predictors of recidivism.

It is also a well established fact in criminology that the rate of offending increases as youthful offenders age but that, at some point, the rate begins to decline. Hence, this non-monotonic shape (first increasing then decreasing)—termed the “age-crime curve”—is a very predictable aspect of offending over the life course. Given this second fact, it is not at all surprising that individuals' past involvement in crime predicts recidivism well. The total amount of crime accumulated by any individual at the time of release captures one aspect of the “age-crime curve.” However, the second aspect of this relationship—the process by which individuals were accumulating their criminal histories—is seldom utilized in recidivism research in general, or for understanding the effects of incarceration in particular. Since it can be anticipated that individuals' involvement in criminal activities over the life course can be characterized (probabilistically) by a *trajectory*, then it should be helpful to study how incarceration deflects an individual's trajectory.

With this goal in mind, the objective of this research effort is to develop, and demonstrate the utility of an analytical framework that can aid practitioners, analysts, and researchers to:

- Model the pre-release criminal history accumulation process in order to characterize, as trajectories, the process by which these individuals had been accumulating their respective criminal histories;
- Use this knowledge as a way to project into the future what could reasonably have been expected of these individuals given their past—i.e., project a counterfactual trajectory; and
- Use this counterfactual trajectory as a backdrop against which to assess the actual post-release offending patterns.

The framework has the potential to help researchers answer a very basic question: *How does incarceration affect individuals?* This report describes one way of addressing this important question in terms of whether, and to what extent, incarceration is able to *deflect* the trajectory a particular offender is on. In order for any analytical framework to provide meaningful insights into this question it must confront three related problems. First, it needs to be able to model individuals' trajectories using knowledge of their past offending patterns. Second, it needs to be capable of projecting trajectories into the future. Finally, it needs to have a mechanism by which to compare actual and counterfactual trajectories for each and every individual so that their incarceration can be appropriately classified as having had a deterrent, a criminogenic, or an incapacitative effect on them.

The information-theoretic approach described in this report is one approach that offers each of these capabilities. It only requires that detailed dated arrest histories, both before incarceration and after prison release, be available to the analyst. Moreover, it provides the usual statistical inferential apparatus whereby analysts can gauge the sensitivity of their results to sampling variation—i.e., how different their estimates would be had a slightly different sample been used. The report provides detailed derivations of the analytical framework and points readers to appropriate sources in the related econometrics/statistics literatures.

DATA USED

The developed framework is tested using a real world data set. In early 2002, the Bureau of Justice Statistics issued a report titled *Recidivism of prisoners released in 1994* that reported on criminal re-involvement of a sample of roughly 38,000 prisoners who were released in 1994 from prisons in 15 states (Langan and Levin, 2002). The data used to support their findings were subsequently archived at the National Archive of Criminal Justice Data at the Inter-University Consortium of Political and Social Research (study # 3355). These data contain detailed information on up to 99 arrest events for each of the individuals in the sample. This includes their pre-incarceration arrest events as well as arrest events within a period of three years after release. In addition, the data provide standard demographic

information on each of the individuals as well as some limited information on their 1994 release mechanism.

To show how the developed framework may fruitfully be applied by researchers, analysts, and practitioners having access to such detailed data the BJS recidivism data were used as a test bed. The report describes in detail how the data were restructured, what predictable patterns were found in the data, and provides detailed estimates of the models. Once modeled, the counterfactual trajectories of each individual in the sample were compared with the actual post-release offending patterns in order to classify the effect that incarceration had in deflecting these trajectories. Finally, the limited set of explanatory information available in these data were used to model and study what factors, if any, helped explain the kinds of experiences people were expected to have. Unfortunately, this source provides insufficient data to make sound policy recommendations about what factors (or policy options) can be expected to maximize the deterrent benefits (or minimize criminogenic harm) of incarceration. The results presented in this report, for this part of the analysis, are intended primarily to showcase the capabilities of the developed framework.

FINDINGS

Despite the emphasis of this research effort being on the *development* of the framework, some interesting findings are summarized below.

- There was a fair amount of consistency among all the pre-prison based models of the criminal history accumulation processes across the 15 states analyzed. For example, being further along in the criminal career (i.e., being at risk of a higher arrest number) and starting the career later (i.e., having a higher age at first arrest) are consistently associated with lowered hazard trajectories. Similarly, all else being equal, being closer to past arrest clusters is consistently associated with an increased hazard trajectory. There was less consistency among states when modeling the deviation between the counterfactual and actual rearrest trajectories after release. Being later in the criminal career was found to exert an upward pressure on the offending trajectory relative to the counterfactual. Similarly, being closer to past cluster was found to exert a downward pressure on the trajectory relative to the counterfactual.
- The criminal history accumulation process contained valuable information about the long-term trends in individuals' offending patterns over the life course. The counterfactual trajectories, based on estimated models of the pre-prison based criminal history accumulation process and projected for the post-release period, perform remarkably well in predicting rearrests within three years of release. On the other hand, these same counterfactuals do not perform as well when used for making short-term projections. The false-positive rates are at very high levels throughout the follow-up period. When updated with models of the post-release behavior, the models perform much better.

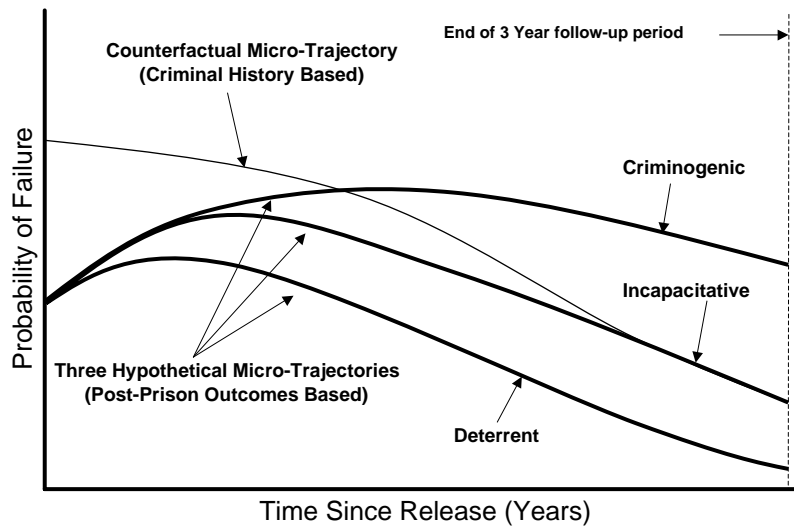


Figure A: A counterfactual trajectory compared with three hypothetical post-release trajectories showing criminogenic, incapacitative, and deterrent effects of incarceration.

- Information-theoretic measures were developed to quantify and classify the divergence between the counterfactual and the actual post-release micro-trajectories. Figure A displays three hypothetical post-release trajectories compared to a counterfactual and how each would be classified. Based on those computations, and in this analysis, large portions of the released cohort were classified as having had an incapacitative (56 percent) or a deterrent (40 percent) experience. A small proportion of the sample (4 percent) experienced criminogenic effects as a result of this incarceration.
- Using these classifications as the criterion outcome, being older at release and being closer to past clusters were consistently found to *increase* the likelihood of a releasee being deterred. Having more prior accumulated arrests and having a later age at first arrest were both found to significantly *decrease* the likelihood of a deterrent effect. Being released to supervision was found not to deter releasees substantially.
- Using the average log divergence between the counterfactual and the actual trajectories as the criterion some conflicting findings emerged. However, the effects of age at first arrest and age at release were qualitatively similar to what were found in the categorical analysis. Additionally, females experienced larger deterrent effects compared to similar males.

IMPLICATIONS

This research effort has important substantive, methodological, and practical implications.

- *Substantive implications.* Substantively, the analytical framework developed here has the potential to shed light on a very important question: *How does incarceration affect individuals?* The framework allows researchers to determine, or at the very least investigate, the types of individuals likely to be deterred by incarceration. In a similar way, it allows them to better understand how incarceration can have differing impacts on the same people at various stages in their life and/or criminal careers.
- *Methodological implications.* When the detailed dated arrest histories of a sample of releasees is available to researchers, utilizing only one source of variation in the data—the total amount of criminal history accumulated prior to prison admission—when modeling the risk of future recidivism forces analysts to waste valuable information and thereby forgo learning opportunities. A second source of variation available in these pre-prison arrest histories—the process by which individuals were accumulating these histories—contains immense amount of information about future offending patterns. The information-theoretic event-history models, developed in this research effort, show how this knowledge can be introduced into the modeling strategy in a very effective way. The process by which individuals accumulate their pre-prison arrest histories, typically, have very predictable patterns that can be modeled. These models allow projection of person-specific micro-trajectories that trace out the evolution of rearrest risk *had the individual not been incarcerated.* As such, they are perfect counterfactuals against which to assess post-release offending patterns.
- *Practical Implications.* Although much of the software needed for the analysis conducted here needed to be programmed from scratch, the availability of standard software allowing researchers to utilize information and entropy based methods is increasing rapidly. For example, SAS has introduced an experimental procedure under its ETS module called PROC ENTROPY that is designed for the estimation of linear and non-linear models using the Generalized Maximum Entropy (GME) approach introduced by Golan, Judge, and Miller (1996). Additionally, LIMDEP—another popular econometrics software—has recently added the GME methods for estimating binary and multinomial logit models.

Software needed to estimate generalized hazard models using the framework described in this report here is far from being developed. In the interim, researchers and practitioners will need to rely on routines and macros developed and made available to the public. An Appendix to this report provides a sample SAS program that was developed to estimate the models presented in this report.

FUTURE RESEARCH

As a result of this research effort, and based on the findings reported in this report, some recommendations for future research can be enumerated.

- The emphasis in this research effort was on development of the analytical framework and demonstration with an application. Comparison of the developed framework to existing and related approaches remains to be done as does the work of assessing the framework's performance using artificially generated data. Such simulation exercises are crucial to establish the credibility of the modeling approach as well as its performance relative to others.
- The framework can also be fruitfully extended to study the trajectories of multiple types of repeatable events such as offending and drug use over the life-course, or offending and employment, etc. Such analyses have the potential of shedding light on how incarceration can interrupt the *co-evolution* of these interrelated behaviors.
- The framework can also be extended to study how other interventions, not just incarceration, may deflect the trajectories of offending. For example, the effects of participation in various treatment programs may be quantified in terms of the program's ability to deflect individuals' offending trajectories.

Chapter 1

Background and Motivation

Imprisonment, for any length of time, is a life-interrupting event. The process of reentry into society after a period of incarceration is riddled with questions of individual sustainability, vulnerability, and fear of failure. Therefore, identifying and understanding the effects that incarceration can have on different types of offenders under different contexts is crucial to developing strategies that minimize any criminogenic harm, and maximize any deterrent benefits, that result from it. This report describes an analytical framework designed to aid practitioners, analysts, and researchers in investigating these issues.

One of the well established and widely accepted empirical regularities in criminology is the link between an individual's past and future crime.¹ Criminologists, however, are not in agreement as to the explanation for this persistence in and, more interestingly, divergence from criminal behavior. Due in large part to the publication of the 1986 National Academy of Sciences report on criminal careers and career criminals (Blumstein, Cohen, Roth, and Visher 1986), the last three decades have seen a surge in research activity that has sought to theorize and explain continuity and change in crime as well as to inform policy of the appropriate role incarceration can and should play in crime control.

The theoretical debate, and the related empirical debate, centers on the causal interpretation attributed to the link between past and future crime. Some criminologists argue that this link is simply a manifestation of a constant (unchanging) criminal propensity, where others argue that the link between past and future crime is causal. The policy relevance of this debate is obvious: To the extent that an individual's relative criminal propensity is "fixed", incarceration can and should play only an incapacitative role. If, on the other hand, an individual's relative criminal propensity is not "fixed", then incarceration could serve as a deterrent and possible turning point to desistance from crime. See, among others, Hirschi and Gottfredson (1983), Farrington (1986), Sampson and Laub (1990,1993), and Piquero, Farrington, and Blumstein (2003) for reviews of the theoretical and methodological issues

¹Over two-thirds of individuals released from prison nationwide, for example, were rearrested for a new crime within three years of release (Langan and Levin 2002). When attempting to explain such high recidivism rates, researchers typically find that releasee's criminal histories are the most reliable predictors.

surrounding the criminal career paradigm.

As a point of departure, this research effort acknowledges the possibility that incarceration could have an incapacitative, a deterrent, or a criminogenic effect on *every* releasee. In this report, I explain and demonstrate the utility of applying an event history-based, information-theoretic method for modeling the detailed criminal history accumulation process of every releasee and, furthermore, for using this process as a backdrop against which to analyze and understand the releasee's post-prison offending behavior.

Although the developed analytic framework has multiple uses, here I have utilized it for a very specific purpose: to compare every releasee's post-prison and pre-prison offending micro-trajectories in order to assess whether *this* incarceration episode had an incapacitative, a deterrent or a criminogenic effect on each of the releasees in the sample. Theoretically, these classifications can then be linked to individual, contextual, and policy relevant variables in an attempt to understand what factors are related to these three types of experiences. The research effort was aimed mainly at developing the analytical framework and not at providing any specific policy recommendations. Fortunately, sufficiently detailed data were available for the first part of the analysis—i.e., modeling the detailed criminal history accumulation process and comparing the pre-release and post-release micro-trajectories. The detailed explanatory data needed for the latter half of the analysis, however, were not available. Therefore, only a limited set of results are presented and discussed here in order to demonstrate how this approach may be helpful to practitioners.

This research effort builds on prior research on recidivism, generally, and post-prison recidivism research, specifically, although the emphasis is different.² Its goal was not to develop models of recidivism as prediction tools (per se). Rather, its goal was to develop tools for estimating and comparing a releasee's actual post-prison offending trajectory with (her)his criminal history-based *counterfactual* offending trajectory for the sole purpose of answering the question: "How, if at all, has this incarceration experience *deflected* the trajectory (path, career) the offender was on?" Since the offender, in question, was incarcerated and had (her)his career interrupted, the pre-prison offending micro-trajectory is termed a *counterfactual* because we never actually observe what this individual would have done had (s)he not been incarcerated. The strategy developed here is a flexible way of using *all* available knowledge about prior offending patterns to make inferences about post-prison offending trajectories.

This idea is not new. Bushway, Brame, and Paternoster (2004, pg 97), for example, note that "... [P]re-existing rates of offending at the time of incarceration would be a

²There exists a significant literature on modeling criminal (or other) recidivism using fully- and semi-parametric survival-type duration models from single or multiple (split) populations. Maltz (1984) and Schmidt and Witte (1988) are authoritative early texts on this topic. More recently, researchers have begun to link these approaches with the study of desistance from criminal careers (Brame, Bushway and Paternoster 2003; Bushway, Brame, and Paternoster 2004) using probabilistic definitions of desistance. The aim of this research effort is to develop tools for understanding the effects of incarceration on post-release offending behavior, classify these effects, and investigate their correlates.

perfect control for individual heterogeneity.” But, two individuals with exactly the same pre-incarceration offending rates may have been on differently sloped trajectories at the time of incarceration and, given varying lengths of time served in prison, could be released at very different times in their lives/careers. The analytical strategy developed here, in utilizing a projected counterfactual for *each and every* individual, is a flexible and robust means of explicitly taking these differences into account.

The methodological challenge lies with developing this counterfactual and in assessing whether, and to what extent, the (actual) post-prison offending trajectory deviates from the counterfactual, and subsequently classifying the incarceration experience accordingly.

Identifying and understanding the correlates of these distinct experiences should be of tremendous help to correctional authorities in reentry planning. Knowledge about the types of releasees likely to experience criminogenic or deterrent effects as a result of their incarceration, for example, could be used in the development of support systems designed to foster positive reentry experiences, and could be a crucial ingredient to individual successes, and ultimately to the promotion of public health and safety.

Crucial to the proposed analytic approach is the availability of the calendar dates of the criminal events that constitute an individual’s past criminal record, as well as the dates of post-release criminal events within the follow-up period. This project relied on the recently released BJS study documenting the detailed criminal histories (as measured by arrests) of a sample of approximately 38,000 offenders released from state prisons across 15 states in 1994. These data were collected by BJS and are publicly available at NACJD (ICPSR). Unfortunately, these data do not provide the kind of detailed information that would be needed to make recommendations regarding specific policy options that may affect the likelihood of incarceration being a deterrent (rather than merely incapacitative or actually criminogenic). To the extent that state and local authorities have access to such detailed data, the analytical framework explained in this report can be applied in a straight forward manner.

Chapter 2

The Analytical Framework

As noted in the previous chapter, the basic challenge researchers or practitioners face in assessing the effects of incarceration on a particular releasee is two-fold. First, they must decide on an appropriate measure that quantifies the outcome they wish to assess. For example, they may wish to assess the effects of incarceration on the risk of post-release relapse into crime, chances of post-release employment, or the risk of relapse into drug use, etc. Having decided on an appropriate outcome, they must then develop plausible counterfactuals for the post release period. The effects of incarceration can then be assessed using this counterfactual. In this report, I restrict attention to the risk of recidivism (as measured by rearrest) as the outcome of interest. Extensions to other types of outcomes and/or multiple outcomes are possible and left for future work.

The challenge of developing plausible counterfactuals then boils down to developing estimates of each individual's risk of recidivism for the follow-up period *had they not been incarcerated*. If such an estimate can be developed then one can compare each releasee's actual post-release offending behavior to this counterfactual and use this as a way to classify the releasee's incarceration experience. Incarceration can be classified as having had a deterrent, incapacitative, or a criminogenic effect on a releasee depending on whether his or her risk of recidivism is found to be lower, about the same, or higher than the counterfactual.

Unfortunately, however, the risk of recidivism is not a static but a dynamic measure. Quantification of the risk of recidivism (statement about "how much") must be accompanied, implicitly or explicitly, by statements about "when". For example, a statement like "person A's risk of recidivism is 20 percent" says little without the qualification that this pertains to a two year follow-up period after release. Therefore, what is needed is a re-definition of the outcome of interest as well as its counterfactual in terms of a dynamic *function* quantifying the evolution of the risk of recidivism over time rather than a static measure. Fortunately, techniques for the analysis of duration data offer a variety of ways of linking the risk of recidivism with time or age thereby allowing the estimation of this dynamic outcome. The remaining challenges then are to (a) develop a dynamic counterfactual micro-trajectory for each individual in the sample, and (b) develop ways to test for differ-

ences between the actual and counterfactual micro-trajectories. By comparing dynamic outcomes—the micro-trajectories—we would in fact be comparing whether incarceration has altered or deflected the trajectory (the career path) a particular releasee was on.

In this chapter, I explain an information-theoretic approach that can be used for (i) developing these counterfactual micro-trajectories utilizing detailed information about past arrest patterns and (ii) testing whether or not the post-release trajectory is, in some sense (to be described later), better, worse, or about the same as the counterfactual. Therefore, the effects of incarceration are classified based on whether or not incarceration has deflected “sufficiently” an individual from his(her) own counterfactual and, if so, whether this deflection is for the better or the worse in terms of the outcome of interest.

The chapter is organized as follows. I begin by developing information-theoretic models of offending trajectories using detailed dated arrest records of a group of offenders. These models can be applied to retrospective (historical) data as well as prospective sequences of events. The dated arrest histories allow detailed models of the risk of each successive arrest number (e.g., the first, second, third, and so forth) at all ages. Once estimated using retrospective criminal histories prior to prison admission, these models then allow projection of the rearrest risk trajectories for each individual given their age at release and the rearrest number they were then at risk of. These projections form the counterfactuals against which the actual rearrest patterns (postrelease) can be assessed. Finally, I develop the tests of the divergence between the actual and counterfactual micro-trajectories.

The following conventions will be used throughout this report. Scalar quantities will be denoted by italicized letters (x_n) or greek symbols (β_k) with appropriate subscripts. Column vectors will be denoted by bold unitalicized letters (\mathbf{x}_n) or symbols ($\boldsymbol{\beta}_k$), again with appropriate subscripts as needed. Row vectors will be denoted with the transpose of the column vectors (e.g., \mathbf{x}'_n). Finally, matrices, where needed, will be denoted by bold unitalicized and capitalized letters (\mathbf{X}) and symbols ($\boldsymbol{\Phi}$). How scalars are gathered to construct vectors and how vectors are gathered to construct matrices will be made explicit when the relevant quantities are defined.

2.1. A SIMPLE NON-PARAMETRIC MODEL

Consider, as a point of departure, the following problem. We have available detailed dated sequences of events (arrests) for a group of individuals. To be concrete, I will restrict the explanation and discussion to arrest sequences although the models are just as applicable to other events. Also, the sequence can be prospective or retrospective histories of a particular cohort. Here, I will first develop the framework for the retrospective histories of arrest events prior to prison admission. The cohort of interest, therefore, is a sample of prisoners released at a particular time. For example, the cohort of interest for the application discussed in this report will be a sample of prisoners released from state prisons in 1994. It is assumed that detailed information pertaining to the pre-prison arrest histories are available for each of the individuals in the sample in addition to dated re-arrest event(s) within a

finite window after the current release.

Detailed information pertaining to each arrest need to include, at a minimum, the date of the arrest and its order in the sequence (i.e., arrest number 1, 2, 3, etc.). Detailed information pertaining to the individuals need to include, at a minimum, the date of birth of the individual. This minimal amount of information is needed in order to construct sequences of ages at each successive arrest events. Harding and Maller (1997) refer to this sequencing as individuals' *arrest profiles*. Assume that such profiles exist for the period before incarceration and for a fixed period after release.

Given that a prison release cohort is likely to have variation in the age at release *and* variation in the amount of time served in prison, it can be expected that this cohort will have had varying amounts of time between their birth and the last prison admission (from which they are released in 1994). Therefore, we can expect to have available two sources of variation in the data. First, we can expect sufficient variation among the individuals with respect to the number of arrests accumulated prior to prison admission—i.e., the “amount” of criminal history accumulated. Second, we can expect variation in the way these arrest histories were accumulated—i.e., the criminal history accumulation “process.” In most criminal recidivism research, the total *amount* of criminal history accumulated prior to release is a very strong determinant of future arrest risk. However, with few exceptions, researchers typically do not utilize the full variation in the criminal history accumulation *process* when assessing future rearrest risk.¹ In the analytical approach developed next, I make full use of this second source of variation.

First, some definitions. Let a_{rn} denote the age of the n th individual when (s)he was arrested for the r th time. The subscript $n = 1, \dots, N$ is used to index individuals and $r = 1, \dots, R_n$ is used to index arrest events. Each individual can have a different number of total arrests in the sequence (hence the limit R_n). Let us restrict, for the moment, the derivation only to the pre-release portion of the arrest profiles. This means we do not have to deal with censoring—the last arrest in each individual's sequence was what got them into prison for the R_n th time. After that, they were not at risk of any more arrests.

Next, let us artificially discretize the continuous “age at arrest” variable. That is, for M mutually exclusive and exhaustive artificially defined intervals (say monthly, quarterly, etc.), let us define the following dummy variables

$$y_{rnm} = \begin{cases} 1 & \text{if } a_{rn} \in (z_{m-1}, z_m) \\ 0 & \text{otherwise} \end{cases} \quad \forall n \in N; r \in R_n; m \in M. \quad (2.1)$$

¹However, there are some exceptions. Visher, Lattimore, and Linster (1991), for example, apply declining weights to prior arrest events thereby giving more relevance to arrest events in the recent past and lower relevance to arrest events from the more distant past. This allows them to develop a more refined criminal history score measure that they then use to model/predict future crime. However, this score is still a static measure that does not allow one to compute a counterfactual offending trajectory against which to assess post-release behavior. In fact, any score developed by a weighted or unweighted combination of prior arrest events can only provide a static measure and cannot be used to construct a dynamic counterfactual.

Table 2.1: An example of creating the y_{rnm} and d_{rnm} flags from arrest profiles.

			z_1	z_2	z_3	z_4	z_5	z_6	z_7	z_8	z_9
			0	5	10	15	20	25	30	35	40
n	r	a_{rn}	y_{r1n}	y_{r2n}	y_{r3n}	y_{r4n}	y_{r5n}	y_{r6n}	y_{r7n}	y_{r8n}	y_{r9n}
1	1	19	0	0	0	0	1	0	0	0	0
1	2	25	0	0	0	0	0	1	0	0	0
2	1	17	0	0	0	0	1	0	0	0	0
2	2	23	0	0	0	0	0	1	0	0	0
2	3	37	0	0	0	0	0	0	0	0	1
n	r	a_{rn}	d_{r1n}	d_{r2n}	d_{r3n}	d_{r4n}	d_{r5n}	d_{r6n}	d_{r7n}	d_{r8n}	d_{r9n}
1	1	19	1	1	1	1	1	0	0	0	0
1	2	25	0	0	0	0	1	1	0	0	0
2	1	17	1	1	1	1	1	0	0	0	0
2	2	23	0	0	0	0	1	1	0	0	0
2	3	37	0	0	0	0	0	1	1	1	1

In effect, we are creating a set of M binary dummy variables for each arrest event for each individual at each age.² Consider, next a positive quantity, denoted s_{rnm} , that we believe this set of dummy variables represent. We can think of the actual outcomes as a noisy (imperfect) manifestation of some underlying reality that we wish to recover. Given the assumption of imperfection, we can only link these unknown quantities (s_{rnm}) to their observed counterparts (y_{rnm}) as approximations. Therefore, let

$$y_{rnm} \approx s_{rnm} \quad \forall r, m, n. \quad (2.2)$$

So far we have assumed that each event is a distinct outcome without regard to their order. To build in the order of the events we need to define a corresponding set of dummy variables that flag whether or not a particular event is possible at a particular age. Let

$$d_{rnm} = \begin{cases} 1 & \text{if } z_m \in (a_{(r-1)n}, a_{rn}) \\ 0 & \text{otherwise} \end{cases} \quad \forall n \in N; r \in R_n; m \in M. \quad (2.3)$$

Here, unlike (2.1), we are creating a set of dummy variables flagging the possibility of each arrest event for each individual at each age. An example of what these dummy variables would look like for two arrest profiles is given in Table 2.1.

Individual 1, for example, was arrested for the first time at age 19 and for the second

²Note, this is only for developing the model. As will be explained below, the artificial discretization of the continuous variable will be removed and the full variation in the continuous age will be used.

time at age 25 after which this individual entered prison and was released as part of the 1994 release cohort. Therefore, $y_{rmm} = y_{1,5,1} = 1$ and $y_{1,m,1} = 0 \forall m \neq 5$. Similarly, $y_{rmm} = y_{2,6,1} = 1$ and $y_{2,m,1} = 0 \forall m \neq 6$. Lets turn next to the d flags. For the first event, $d_{rmm} = d_{1,m,1} = 1 \forall m \leq 5$ and are set to 0 $\forall m > 6$. This is because the individual is not at risk of being arrested for the first time after (s)he has been arrested for the first time. The individual is now at risk of being arrested for the second time, i.e., $d_{rmm} = d_{2,m,1} = 1 \forall m \in (5, 6)$, until (s)he is arrested for the second time. After that the individual enters prison for the last time before being released in 1994.

Having defined the two interrelated sets of dummy variables, let us combine them. To do so, let us pre-multiply both sides of (2.2) by the d_{rmm} flags, sum across all individuals with the same r and m , and assume that this aggregation washes out all the imperfections. In other words, even though each y_{rmm} are only imperfect manifestations of the corresponding s_{rmm} , let their sums within r and m be perfectly preserved. This allows us to convert the inequalities into the following equalities:

$$\sum_n d_{rmm} y_{rmm} = \sum_n d_{rmm} s_{rmm} \quad \forall r, m. \quad (2.4)$$

Finally, if we assume that $s_{rmm} = s_{rm} \forall r, m$, i.e., that this quantity is fixed within each r and m pairs, then we can solve explicitly for each of these unknown quantities to get

$$s_{rm} = \frac{\sum_n d_{rmm} y_{rmm}}{\sum_n d_{rmm}} \quad \forall r, m. \quad (2.5)$$

Since an event occurs (i.e., $y_{rmm} = 1$) only when an individual is at risk of that event occurring (i.e., $d_{rmm} = 1$), we see that the numerator of this ratio is merely the number of individuals being arrested for the r th time within the m th age interval. The denominator, on the other hand, is merely the number of persons that were at risk of being arrested for the r th time during the m th age interval. This quantity is, of course, a familiar one. In statistics and econometrics it is referred to as the hazard (rate) and in demography it is referred to as a Parity Progression Ratio (PPR).³ The derivation in (2.5) is in fact a nonparametric estimate of the hazard of the r th event occurring during age interval m (or the probability of progressing to the next event, conditional on being at risk of that progression).

Visually, this concept can best be explained by means of the Lexis diagram in Figure 2.1, where the criminal history accumulation process of five hypothetical offenders are shown.⁴ Each diagonal line represents a releasee's life prior to the current incarceration. The filled black circles represent arrest events (with the arrest numbers indicated alongside them), and a hollow circle represents the arrest that resulted in the current incarceration.

Now consider the rectangular region (ABCD). This region contains the criminal ac-

³See Chapter 9 in Hinde (1998) for a general discussion of PPRs. See Feeney and Yu (1987) and Bhrolchain (1987) for applications of PPRs to changes in fertility patterns.

⁴See the Maltz and Mullany (2000) for other interesting ways in which this information could be visualized.

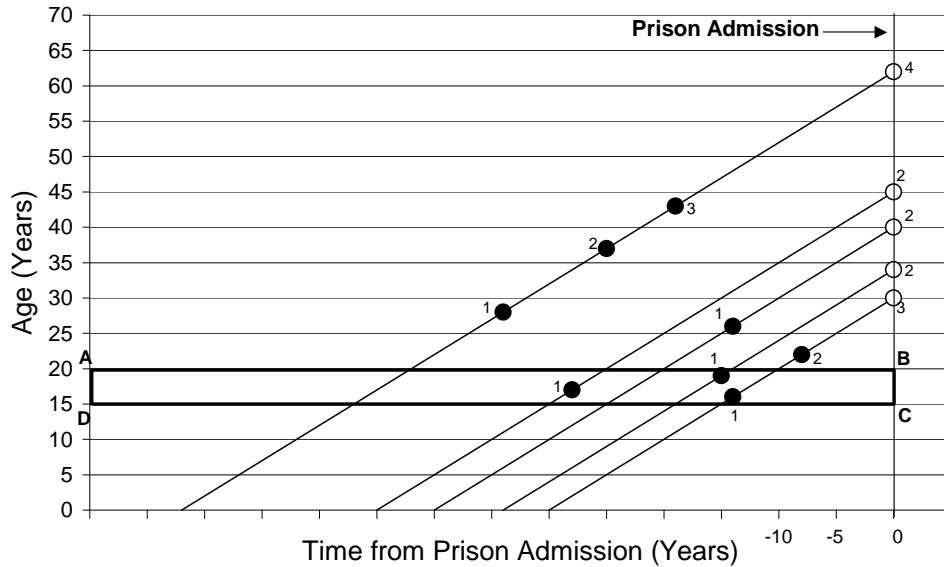


Figure 2.1: Lexis Diagram showing the Criminal History Accumulation Process of five hypothetical offenders entering prison

tivities of the five hypothetical offenders during their 15 to 20-year life-phase. Since there were no criminal activities (for this group) prior to that age, we find that all five persons are at risk of initiating their criminal career at age 15 (i.e., $\sum_n d_{rnm} = 5$). Next, we note that, of these, only three actually committed their first crime during this phase of their life (i.e., $\sum_n d_{rnm} y_{rnm} = 3$). This allows us to compute the PPR for the first progression (initiation) by age 20 for this group of people as $s_{1m} = 0.6$. In a similar manner, we may compute the PPR for the first progression during other life-phases, and we may compute the PPR for subsequent progressions during this and other life-phases. In essence, for any given sample, we may use detailed dated criminal histories to construct PPRs that characterize the sample members' criminal history accumulation process.

The point of this analytical and graphical derivation was simply to demonstrate that, when combined with the set of dummy variables d_{rnm} , any manipulation of the left and right hand sides of (2.2) will yield constraints on the values the hazard can take. In fact, this same derivation can be extended without change of notation to include censored cases. We only need to define d_{rnm} to be 0 after the event has occurred *or* if the individual is no longer being observed, i.e., the case is censored. Note that for censored cases y_{rnm} will always be 0 because we never see the event occurring. However, between the $r - 1$ st event and the time of censoring, this individual will contribute towards the denominator of (2.5).

In the example provided in Table 2.1, I used 5-year intervals. In fact, one can use as small an interval as one desires. For example, when studying age profiles as measured in year, one can define intervals as small as a quarter or a month. However, computation of the nonparametric PPR or hazard becomes more unstable because we end up with many

empty cells and many cells where the denominator is 0. This suggests moving towards a parametric formulation of the problem which allows a flexible functional form linking the hazards across persons, ages, and event numbers. I turn to that formulation next.

2.2. A SEMI-PARAMETRIC INFORMATION-THEORETIC APPROACH

Instead of assuming that $s_{rnm} = s_{rm} \forall n$, suppose we allow the hazard to vary across n , m , as well as r . What we need now is some way to impose structure on the model. Consider the minimal set of variables we have available in Table 2.1: z_m = the age grid points just defined, and r = the event number. A simple way to impose structure on the model is to weight both sides of the approximation (2.2) with z_m and r and take the weighted and unweighted sums across all n . This yields the following two equations:

$$\sum_{rn} \sum_m z_m d_{rnm} y_{rnm} = \sum_{rnm} \sum_m z_m d_{rnm} s_{rnm} \quad (2.6)$$

$$\sum_{rn} r \sum_m z_m d_{rnm} y_{rnm} = \sum_{rnm} r \sum_m z_m d_{rnm} s_{rnm} \quad (2.7)$$

Unfortunately, unless we make some assumptions about s_{rnm} , we cannot proceed to solve for their values like we did in the non-parametric case. However, under the Information-theoretic approach, to be developed below, we *can* recover information about the s_{rnm} without making any a-priori assumptions about the form of s_{rnm} .

Before proceeding to that, however, I generalize the problem to include an expanded set of explanatory variables that can vary across individuals, events, and time. As in all moment based methods, however, it is still assumed that the variables in this set are not *perfectly* correlated.

2.2.1. Setting up the basic problem

Suppose there exist a set of K event- and person-specific attributes (denoted x_{krn}) that we believe are part of the mechanism generating the outcomes—i.e., part of the hazard model. Minimally, this would include r and z_m as shown above. How do we introduce these attributes into the model? As explained in the previous section, introducing the order of event was accomplished simply by pre-multiplying both sides of (2.2) by the flags d_{rnm} . Introducing attributes can be done in much the same way, as explained above. That is, we can pre-multiply both sides of (2.2) by the corresponding d_{rnm} flags, the artificial discrete support points z_m , as well as the available attributes x_{krn} , and aggregate across m , r , and n in order to convert the inequalities into equalities. This yields the following K equality constraints:

$$\sum_{rn} x_{krn} \sum_m z_m d_{rnm} y_{rnm} = \sum_{rn} x_{krn} \sum_m z_m d_{rnm} s_{rnm} \quad \forall k \in K. \quad (2.8)$$

where, we assume that the attributes includes a column of 1's. Note that each event can occur only once in an individual's lifetime (e.g., the 4th arrest can only occur once) and since we are dealing with the uncensored records (pre-prison criminal histories) we can assume that none of the at-risk periods end without an event. In other words, $\sum_m z_m d_{rnm} y_{rnm} \approx a_{rn} \forall r, n$ on the left hand side (LHS) of (2.8).⁵ But the approximation is merely a result of our artificial discretization of the continuous age variable and by making the discrete intervals arbitrarily small we, in fact, approach the continuous variable. Therefore, we can replace the term $\sum_m z_m d_{rnm} y_{rnm}$ on the LHS with the actual continuous age variable in order to utilize the full variation available to us. This allows us to re-write these constraints as:

$$\sum_{rn} x_{krn} a_{rn} = \sum_{rn} x_{krn} \sum_m z_m d_{rnm} s_{rnm} \quad \forall k \in K \quad (2.9)$$

We now have, what is termed, an ill-posed inversion problem—more unknowns than equations linking them (Levine, 1980). In the non-parametric hazard model case, we solved this problem by assuming that $s_{rnm} = s_{rm} \forall n$ and we only summed within each r and m pairs. In other words, we had exactly the same number of unknowns as we had constraints. That allowed us to explicitly solve for a particular solution by *inverting* the quantity multiplying each s_{rm} on the right hand side (RHS) and taking that to the LHS. Here, the problem is ill-posed. We have far more unknowns than we have constraints. How do we solve this ill-posed problem?

2.2.2. Information Theory: A brief digression

Edwin Jaynes (1957a,b), in a series of influential papers in statistical physics proposed a solution to such a problem provided that the unknown quantities are in the form of proper probabilities. He proposed that when faced with a problem that has possibly an infinite number of solutions, we should choose the one solution that implies maximum uncertainty while ensuring that the constraints (evidence) are satisfied. That way, we will be making the most conservative (safe) use of the evidence. Jaynes (1982) provides axiomatic derivation of the rationale underlying this approach.

Of course, for it to be operationalized, we need some quantification of uncertainty. Within the context of a problem in communication theory, Shannon (1948) defined the uncertainty contained in a message with J mutually exclusive and exhaustive outcomes as $H = -\sum_j p_j \log p_j$ and termed it *Information Entropy*. Here p_j is the probability that we will observe event j from the set of J possible events. In what came to be known as the Maximum Entropy formalism (or the principle of insufficient reason), Edwin Jaynes proposed to use Shannon's Entropy as the criterion to maximize, subject to all available constraints, in order to derive conservative inferences from the evidence.

In addition, if we have some non-sample prior information about the probabilities

⁵Extending this to censored cases is trivial and will be discussed later.

$\{p_j^0\}$, then an equivalent problem is to minimize the Kullback-Leibler directed divergence, or Cross Entropy, between the prior and the posterior probabilities (Kullback 1959; Good 1963). The Cross Entropy is defined as $CE = \sum_j p_j \log(p_j/p_j^0)$ if p_j^0 are the priors. Furthermore, if the prior probabilities p_j^0 are assumed to be uniform, then the Cross Entropy formalism reduces to the Maximum Entropy formalism. Not surprisingly, both the CE and the H objectives are related and really special cases of the family of Cressie Read power divergence measures (Cressie and Read 1984). Notwithstanding the diverse types of constraints that theory may suggest (e.g., geometric moment, higher order moment, inequality constraints, etc.) and whether or not we believe their sample analogs are measured with noise, this method of using information in a sample (evidence) to recover information about social, economic, or behavioral phenomenon falls within the growing field of *Information and Entropy Econometrics*.⁶

The key requirement of this formulation is that the unknowns be proper probabilities (i.e., non-negative quantities that sum to one). This is because Shannon's entropy, as well as the Kullback-Leibler directed divergence measures, are defined in terms of proper probabilities. Zellner (1991) and Zellner and Highfield (1988) have developed this approach extensively in the econometrics field to derive a general class of distributions that satisfy various side conditions (constraints) that may be suggested/provided by economic theory.

In an important extension of their work, Ryu (1993), used this same principle to derive *regression functions* rather than *probability distributions*. Ryu (1993) showed that if the unknown quantities can be assumed to be non-negative, then the application of the Maximum Entropy (or Minimum Cross Entropy) principle can, under suitable side conditions (constraints), yields a large number of functional forms. Using the example of a production function with 2 inputs (Capital and Labor), Ryu (1993) derived the Exponential polynomial, the Cobb-Douglas, the Translog, the Generalized Cobb-Douglas, the Generalized Leontiff, the Fourier flexible form, and the Minflex-Laurent Translog production functions simply by manipulating the side conditions.

It should also be noted that utilizing the maximum entropy formalism simply with non-negative quantities—that may not be proper probabilities—is not, however, entirely new. Similar approaches are used in the field of image reconstruction. See, for example, Gull and Daniell (1978), Gull (1989), and Donoho, Johnstone, Joch, and Stern (1992) for detailed discussions.

⁶For recent theoretic and applied work in this field, see the 2002 special issue of the *Journal of Econometrics* (Vol 107, Issues 1&2), Chapter 13 of Mittelhammer, Judge and Miller (2000), the 1997 Volume (12) of *Advances in Econometrics* titled "Applying Maximum Entropy to Econometric Problems," and the Golan, Judge, and Miller (1996) monograph. See also Maasoumi (1993), Soofi (1994), and Golan (2002) for historical discussions and general surveys.

2.2.3. An information-theoretic solution to the basic problem

This brings us back to the problem at hand. The evidence we have is in the form of the constraints (2.9) and our unknowns are in the form of non-negative hazards—precisely the kind of problem for which the Maximum or Cross Entropy formalism could be applied very profitably. However, unlike Ryu (1993), where each of the unknowns are completely unrestricted (other than being non-negative), in our case, some of the hazards are just not possible. Hence, following Ryu (1993), I define a generic Cross Entropy problem but, additionally, I introduce the d_{rnn} flags into the objective function. This ensures that hazards corresponding to periods when individuals are *not* at risk of a progression will in no way influence the objective being optimized. This modified information recovery problem can be written as:

$$\min \quad CE = \sum_{rnn} d_{rnn} \left\{ s_{rnn} \log(s_{rnn}/s_{rnn}^0) \right\} \quad (2.10)$$

subject to the constraints of (2.9). Here s_{rnn}^0 is an arbitrary non-negative quantity representing our prior state of knowledge. This is a constrained optimization problem (in the unknown hazards s_{rnn}) that can be solved by variational methods. The primal Lagrange function for this problem is:

$$\mathcal{L} = \sum_{rnn} d_{rnn} s_{rnn} \log(s_{rnn}/s_{rnn}^0) + \sum_k \alpha_k \left\{ \sum_{rn} x_{krn} a_{rn} - \sum_{rn} x_{krn} \sum_m z_m d_{rnn} s_{rnn} \right\} \quad (2.11)$$

where α_k are the set of K Lagrange Multipliers corresponding to the constraints (2.9). The first order conditions for this problem can be written as:

$$\frac{\partial \mathcal{L}}{\partial s_{rnn}} = d_{rnn} \log(s_{rnn}/s_{rnn}^0) + d_{rnn} - d_{rnn} z_m \sum_k x_{krn} \alpha_k = 0 \quad \forall r, m, n, \quad (2.12)$$

so that canceling the d_{rnn} terms and solving for s_{rnn} yields the general solution:

$$s_{rnn} = s_{rnn}^0 \exp \left(z_m \sum_k x_{krn} \alpha_k - 1 \right) \quad \forall r, m, n. \quad (2.13)$$

If we assume that $s_{rnn}^0 = \exp(1)$ then this yields a simple log-linear solution for the hazard. That is, we get $\log s_{rnn} = z_m \mathbf{x}'_{rn} \boldsymbol{\alpha} \forall r, m, n$.⁷ Other assumptions are possible and will yield different solutions. More on this later.

Note that we can also use the general solution of (2.13) back in the primal *constrained* optimization problem (2.11) to derive a dual *unconstrained* optimization problem in the

⁷Here $\mathbf{x}_{rn} = (x_{1rn}, \dots, x_{Krn})'$ and $\boldsymbol{\alpha} = (\alpha_1, \dots, \alpha_K)'$ are the attributes and Lagrange Multipliers written in vector notation so that $\mathbf{x}'_{rn} \boldsymbol{\alpha} = \sum_k x_{krn} \alpha_k \forall r, n$.

unknown Lagrange Multipliers. By inserting this solution into the primal problem we get

$$\begin{aligned}
\mathcal{L} &= \sum_{rnn} d_{rnn} s_{rnn} \left(z_m \sum_k x_{krn} \alpha_k - 1 \right) + \sum_k \alpha_k \left\{ \sum_{rn} x_{krn} a_{rn} - \sum_{rn} x_{krn} \sum_m d_{mrn} z_m s_{mrn} \right\} \\
&= \sum_{krnn} \alpha_k x_{krn} z_m d_{rnn} s_{rnn} - \sum_{rnn} d_{rnn} s_{rnn} + \sum_{krn} \alpha_k x_{krn} a_{rn} - \sum_{krnn} \alpha_k x_{krn} z_m d_{rnn} s_{rnn} \\
&= \sum_{krn} \alpha_k x_{krn} a_{rn} - \sum_{rnn} d_{rnn} s_{rnn} = \mathcal{G} \tag{2.14}
\end{aligned}$$

Given that the solution (2.13) is a function of the unknown Lagrange Multipliers α_k , (2.14) is simply an unconstrained objective function that needs to be maximized with respect to the unknown quantities α_k . That is, *minimizing* the objective (2.10) with respect to the unknowns s_{rnn} subject to the constraints (2.9) is identical to *maximizing* the dual objective (2.14) with respect to the unknowns α_k . Additionally, the dual is an *unconstrained* optimization problem therefore conventional software that contain unconstrained optimization routines (e.g., SAS, GAUSS, etc.) can be used to solve this problem.

The dual objective is a non-linear function that must be maximized with respect to the parameter vector α . As such, it falls under the general class of extremum estimators. The consistency and asymptotic normality of these estimators can be established under fairly general regularity conditions (Mittelhammer, Judge, and Miller 2000, pg 132-139). However, as is evident, the objective ignores the clustering of observations within an individual. That is, individuals that have multiple arrest events are treated as contributing multiple independent pieces of information to the objective. This typically results in biased (downwards) asymptotic standard error estimates misleading us into being overly confident about our parameter estimates. To correct for this bias, following Ezell, Land, and Cohen (2003), I construct and utilize a *modified sandwich variance estimator*. Sandwich estimators (Huber 1967; White 1980) are now very commonly utilized in econometrics and statistics when researchers are unsure about the complete specification of the distribution in a fully parametric model but are fairly sure that the mean value is well specified. The modified sandwich variance estimator merely corrects the sandwich estimator further for the possibility that there may be unobserved but persisting heterogeneity within individuals over time. Detailed analytical derivations are available from the author on request.

2.2.4. Flexible functional form and generalized hazard models

The solution described above was generic and I utilized a single set of constraints (2.9) in deriving it. However, formal theoretical reasoning and/or casual past experience may suggest many other forms of constraint each of which will alter the solution derived. For example, we may believe that attributes x_{krn} not only explain variation in the age at which particular events occur (i.e., how a_{rn} varies across n and r) but also its higher moments (e.g., how $a_{rn} \log a_{rn}$ varies across n and r). If so, then, in addition to requiring the satisfaction of

constraints involving the a_{rn} , we can require satisfaction of constraints involving $a_{rn} \log a_{rn}$ as well.

To do so, we proceed in the same way as before. Let us pre-multiply both sides of the approximation (2.2) by d_{rmn} , $z_m \log z_m$, and x_{krn} , and sum over all r , m , and n . In a manner analogous to (2.9), this yields constraints of the form:

$$\sum_r x_{krn} a_{rn} \log a_{rn} = \sum_r x_{krn} \sum_m z_m \log z_m d_{rmn} s_{rmn} \quad \forall k \in K. \quad (2.15)$$

This set of constraints does not need to have the same attributes as (2.9). I am assuming that they are the same for ease of notation. Now, our information recovery task can be modified to a constrained optimization problem subject to the two sets of constraints *simultaneously*. Following the same derivations as above, we can derive the optimal solution as:

$$s_{rmn} = s_{rmn}^0 \exp(z_m \mathbf{x}'_{rn} \boldsymbol{\alpha} + z_m \log z_m \mathbf{x}'_{rn} \boldsymbol{\beta} - 1) \quad \forall r, m, n, \quad (2.16)$$

where, $\boldsymbol{\beta} = \beta_1, \dots, \beta_K$ are a new set of Lagrange Multipliers corresponding to the constraints (2.15). Moreover, as in the simpler case, we can convert the constrained minimization problem into an unconstrained maximization problem in the unknown Lagrange Multipliers (both $\boldsymbol{\alpha}$ and $\boldsymbol{\beta}$) simultaneously. This dual objective takes the form:

$$\mathcal{G} = \sum_{krn} \alpha_k x_{krn} a_{rn} + \sum_{krn} \beta_k x_{krn} a_{rn} \log a_{rn} - \sum_{rmn} d_{rmn} s_{rmn} \quad (2.17)$$

where s_{rmn} is the solution given in (2.16).

An appropriate definition of d_{rmn} can help restrict the analysis to a single event, to include censored cases, and/or to remove individuals from the risk pool. For censored cases, as noted in the non-parametric derivation, we simply define $d_{rmn} = 1$ when the individual is at risk of experiencing the next event until he or she is censored. After that, we set $d_{rmn} = 0$. This means that, on the LHS of the constraints, we will have the actual values of a_{rn} and/or $a_{rn} \log a_{rn}$ only when the event is observed but a value of 0 when the case is censored. To see this note that the term $\sum_m d_{rmn} y_{rmn} z_m = 0$ for all censored cases because $y_{rmn} = 0 \forall m$ when the record is censored. Hence, in addition to redefining the set of dummy variables d_{rmn} appropriately, if we let $c_{rn} = 1$ flag the censored cases, and re-define the age variables as

$$a_{rn}^* = \begin{cases} a_{rn} & \forall c_{rn} = 0 \\ 0 & \forall c_{rn} = 1 \end{cases} \quad \text{and} \quad a_{rn}^* \log a_{rn}^* = \begin{cases} a_{rn} \log a_{rn} & \forall c_{rn} = 0 \\ 0 & \forall c_{rn} = 1 \end{cases} \quad (2.18)$$

then we can use a_{rn}^* and $a_{rn}^* \log a_{rn}^*$ in the objective function (2.17) when the data include censored cases. The remaining derivations remain unaltered.

More generality can, of course, be built into this framework by assuming a general set of constraints that involve various transformations of a_{rn} . These could include linear,

quadratic, cubic, quartic, Fourier, log-linear, etc. By adjusting these constraints, we can derive a large number of parametric forms. Moreover, we can impose sets of these constraints *simultaneously* to get more generalized forms that nest several alternatives and test for specific functional forms.

The framework presented here is not, however, entirely innovative. In a recent survey of dynamic duration models, Ebrahimi and Soofi (2003) show how several of the standard parametric models along with several mixture models by utilizing an information-theoretic objective while specifying differential equation constraints that govern the evolution of the hazard over time (See also Table 1 in Soofi, Ebrahimi, and Habibullah [1995]). Other recent articles involving the same principle—what the authors refer to as the principle of *Minimum Dynamic Discrimination* or *Maximum Dynamic Entropy*—include Ebrahimi, Habibullah, and Soofi (1992), Ebrahimi and Kirmani (1996), and Asadi, Ebrahimi, Hamedani, and Soofi (2005).

The framework I present in this report builds on this literature but utilizes a discrete support thereby negating the need for differential equation constraints and, following Ryu (1993), I formulate the objective in terms of the hazard directly (rather than the underlying probability distributions). This adds considerable computational efficiency.

2.3. DEFLECTING OFFENDING TRAJECTORIES

2.3.1. Estimating the deviation of trajectories from counterfactual paths

So far we have not made any explicit assumptions about the priors s_{rmm}^0 except noting that if we fix it to $\exp(1)$, we obtain a simple log-linear specification for the path. If we do have some prior knowledge about the evolution of the hazard over time, we can introduce that information in the form of the s_{rmm}^0 so that the final solution is computed as a *deviation* from this prior. This formulation is particularly relevant for our analysis since we wish to study the deviation of a trajectory from a counterfactual. But first, we need to construct a plausible counterfactual.

A simple way to construct this counterfactual is to model the links between age, arrest number, and other attributes using the framework described above but by estimating it only with the pre-prison part of the available arrest histories. This model would therefore capture the dynamic process by which individuals in the sample had been accumulating their arrest histories prior to prison admission. Next, using this model, we can project a future trajectory (from the age at release onwards) using knowledge about the arrest number this particular individual was at risk of as well as all the other attributes as \tilde{s}_{rmm} . These projections trace out the entire evolution of the hazard *for the next arrest* over the remaining life of the individual given knowledge about the past criminal history accumulation process. As such, each provides the perfect counterfactual for assessing future offending patterns since this is the path we should expect the releasee to have been on at the time of release *had (s)he not been incarcerated*. Therefore, when we model the post-release offending

trajectory—i.e., the hazard of the next event in the sequence of arrests—we simply replace s_{rnm}^0 with \tilde{s}_{rnm} in the dual objective function (2.17). This yields a solution exactly like (2.16) where $s_{rnm}^0 = \tilde{s}_{rnm}$.

Why would this procedure model the deviation from the pre-prison based counterfactual trajectory? To see why, consider the case where all parameters in this post-release model are found to be 0 (i.e., $\alpha_k = 0$ and $\beta_k = 0 \forall k$). We then obtain the result that $s_{rnm} \equiv \tilde{s}_{rnm}$. In other words, if all the parameters of the post-release model are zero then there has been no deviation from the path the individual was projected to be on—i.e., the counterfactual. To the extent that these parameters are non-zero, there has been a deflection of the trajectory as a result of this incarceration experience. What remains then is to find a way to decide whether this deflection is for the better (lowered trajectory compared to the counterfactual), worse (higher trajectory compared to the counterfactual) or about the same. I derive one such measure next.

2.3.2. Classifying the incarceration experience

Ebrahimi and Soofi (2003), present a method for comparing information across two hazard paths (either across individuals or across two different paths for the same individual) that is particularly well suited for comparing the evolution of two trajectories over time. Their approach utilizes the notion that the Kullback-Leibler directed divergence measure (or Cross Entropy) is a measure of divergence between two probability distributions. Since probability distributions and hazards are two different ways of representing the same underlying phenomenon, they derive dynamic divergence measures between the evolution of two hazard functions.

Applying this idea in our case is fairly straightforward. Since the objective is defined in terms of the natural log of the ratio of two strictly positive numbers, then

$$\log(s_{rnm}/s_{rnm}^0) \begin{cases} > 0 & \text{iff } s_{rnm} > s_{rnm}^0 \\ = 0 & \text{iff } s_{rnm} = s_{rnm}^0 \\ < 0 & \text{iff } s_{rnm} < s_{rnm}^0 \end{cases} \quad \forall r, m, n. \quad (2.19)$$

The problem with this measure, as it stands, is that it is a function of age and therefore it can, and typically will, be different for each m . What we need is a way to aggregate across this divergence measure over the entire *residual life* starting from any point z_m^* (e.g., the date of release).

Ebrahimi and Soofi (2003) present a way to approach this problem by redefining the hazards into probabilities and noting that the measure reduces to the traditional Kullback-Leibler divergence measure with an appropriate normalization and a ratio of survival functions (Ebrahimi and Soofi 2003, pg 6). In an analogous, but unrelated derivation, Ryu (1993) showed that the Maximum Entropy solution for any positive quantity could be considered an *averaged density* if we normalize appropriately. In our case, the quantity of

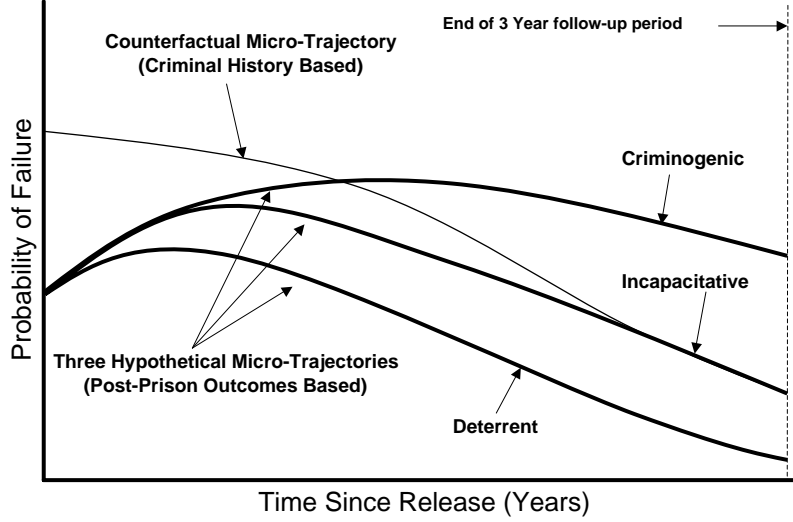


Figure 2.2: A counterfactual trajectory compared with three hypothetical post-release trajectories showing criminogenic, incapacitative, and deterrent effects of incarceration.

interest is the hazards for all points beyond the date of release. Hence, following Ryu (1993), if we define the term $s_{rmn}^* = \sum_m d_{rmn} s_{rmn}$ for some appropriately defined d_{rmn} , then we see that

$$\pi_{rmn} = \frac{d_{rmn} s_{rmn}}{s_{rmn}^*} = \frac{d_{rmn} s_{rmn}}{\sum_m d_{rmn} s_{rmn}} \quad (2.20)$$

is a proper probability wherever it is defined (i.e., $\sum_m \pi_{rmn} = 1 \forall r, n$ and $\pi_{rmn} \geq 0 \forall r, m, n$). This means that the objective function we are optimizing already contains information about the averaged difference between \tilde{s}_{rmn} and s_{rmn} . All we need to do is normalize the objective appropriately. This normalization provides a way to aggregate the various terms in the trajectory (2.19) across the entire residual life of the individual upon release. This measure is defined as:

$$\begin{aligned} \delta_{rn} &= \frac{1}{s_{rmn}^*} \sum_m d_{rmn} s_{rmn} \log(s_{rmn}/s_{rmn}^0) \\ &= \sum_m \frac{d_{rmn} s_{rmn}}{s_{rmn}^*} \log \log(s_{rmn}/s_{rmn}^0) \\ &= \sum_m \pi_{rmn} \log(s_{rmn}/s_{rmn}^0) \end{aligned} \quad (2.21)$$

The δ statistic can be seen as an average (expected) log divergence between the projected trajectory (based on knowledge about pre-prison arrest patterns) and the actual post-release offending pattern. An example of a counterfactual and three hypothetical post-release trajectories are shown in Figure 2.2. As shown there, the trajectories can be dif-

ferent at any given point in the post-release period. However, the δ statistic derived above measures divergence between two *paths* rather than points. Moreover, since π_{rnm} is a proper probability (summing to one), we can compute the standard deviation of this quantity (the log divergence) as well. The standard deviation of each δ_{rn} can be computed as:

$$\sigma_{rn} = \sqrt{\sum_m \pi_{rnm} (\log(s_{rnm}/s_{rnm}^0))^2 - \left(\sum_m \pi_{rnm} \log(s_{rnm}/s_{rnm}^0)\right)^2} \quad \forall r, n, \quad (2.22)$$

which follows from the definition of the variance of a random variable v as $E(v^2) - E(v)^2$.

Finally, we can utilize these definition of δ_{rn} and σ_{rn} to decide whether the expected log divergence of the residual life trajectories are *sufficiently* different. The current incarceration is deemed to have had an

$$\begin{aligned} \text{Deterrent Effect} & \text{ iff } 0 < \delta_{rn} + 2 * \sigma_{rn} \\ \text{Incapacitative Effect} & \text{ iff } 0 \in \delta_{rn} \pm 2 * \sigma_{rn} \\ \text{Criminogenic Effect} & \text{ iff } 0 > \delta_{rn} - 2 * \sigma_{rn} \end{aligned} \quad (2.23)$$

These classifications allow one to model the effects of individual, contextual, and policy options on the likelihood of a releasee's prison experience being one of the three types. This can be done in standard software using multinomial discrete choice models or ordered discrete choice models. Such an analysis could be used, for example, to study what measures can increase the likelihood of the deterrent experience and minimize the likelihood of a criminogenic experience.

Alternately, one can study the effects of these individual, contextual, and policy options on the continuous variable δ_{rn} directly since larger '+' values of δ indicate larger criminogenic effects and larger '-' values of δ indicate large deterrent effects. In the next chapter, I explore both these approaches and present a limited set of results.

2.4. CONCLUDING COMMENTS

In this chapter, I developed an information-theoretic framework for modeling the detailed criminal history accumulation process of a group of releasees. There exists, of course, several other methods that are capable of modeling event histories (see, for example, Mayer and Tuma [1990] and Blossfeld, Hamerle, and Mayer [1989]). The method developed here has several benefits over existing strategies.

First, unlike fully parametric functional forms, the information-theoretic approach allows an easy incorporation of several constraints that yield flexible functional-form hazard models. Under restrictive assumptions, this approach yields several of the standard hazard models as special cases. As such, the approach can be used to develop models that nest several parametric forms as special cases in order to test (statistically) assumptions about

the shape of the evolution of the hazard over time or assumptions about proportionality.

Second, given its particular emphasis on minimizing the directed divergence between a prior and posterior trajectory, the approach offers an easy method for assessing whether or not the evolution of the hazard over the residual life (defined at any appropriate point, e.g., the date of release) is different from a counterfactual. The average log divergence between the two trajectories provides a convenient summary statistic for this purpose. Moreover, this statistic is not an ad-hoc measure. It is merely a re-normalized version of the *very* objective that is being optimized to obtain the hazard models.

Finally, this average divergence measure can then simply be converted into a classification or can be viewed as a continuous measure. Large negative values on this statistic imply large deterrent effects whereas large positive values on this statistic imply large criminogenic effects. Studying how this measure correlates with various attributes as well as policy options can be of immense use to practitioners and policy makers in understanding the factors that may maximize deterrent benefits of incarceration and/or that minimize the criminogenic harm resulting from it. These factors can include not only demographic factors that are outside the control of policy makers but also factors like participation in prison programs, post-release supervision/assistance programs, as well as socio-economic, behavioral, and contextual factors such as the availability of employment opportunities, family bonds, and individuals' mental health.

The method developed here is designed to take full advantage of dated criminal history records when such information *is* available. In ignoring this information, when it is available, researchers risk wasting valuable information and thereby forgo learning opportunities. Aggregate measures of criminal history scores typically use only one source of variation in the pre-release arrest history—the number of prior arrests (weighted or unweighted). The method presented here utilizes another source of variation available in the pre-prison arrest history—the process by which this arrest history was accumulated. Furthermore, it utilizes this knowledge in informing the future evolution of the hazard.

To be sure, the method described here is not the only way one can study trajectories of offending patterns over time. There exists a large literature in criminology that aims to model the trajectories of offending patterns over the life course of individuals using group based modeling techniques (Nagin 2005; Nagin and Land 1993; Land and Nagin 1996). Responding to concerns raised by Hagan and Palloni (1988), in particular, Land and Nagin (1996) demonstrated that group-based trajectory models are well suited to take into account the order of arrest events. Similarly, the approach developed here is not incompatible with approximating unobserved heterogeneity via finite mixture modelling strategies. Therefore, it would be a profitable extension of the current work to include distinct group-based heterogeneity in the models as well. However, for the approach to have practical utility, the emphasis should remain on attempting to construct counterfactual trajectories for each and every individual in the sample (not just for groups). In this report, I rely solely on available attributes to model the heterogeneity in the evolution of the hazards.

Chapter 3

An Application

In this chapter, I apply the methods developed in the previous chapter to a specific data set. The chapter is organized as follows. I begin with a brief description of the dataset and the variables used in this report. I then summarize estimates of the pre-prison based criminal history accumulation process and discuss the findings. I also use these models to make projections for individuals at the time of their release. These projections are compared with the actual arrest events post-release. Next, I use these projected counterfactual trajectories as a backdrop against which to develop the actual post-release offending trajectories. These model estimates are also presented in summary form. Finally, using the methods developed in the previous chapter, I compute the δ statistic and use it to classify individuals' incarceration experiences. I present a limited set of results from standard linear and logistic regressions that are used to model variation in these experiences across individuals.

3.1. THE DATA

3.1.1. Data source

The data used in this research effort is available to the public from the National Archives of Criminal Justice Data (NACJD), at the Inter-University Consortium for Political and Social Research (ICPSR), University of Michigan, Ann Arbor, MI. It is archived as study # 3355 (*Recidivism of Prisoners Released in 1994 [United States]*) (BJS, [2002]).

The data were collected by the Bureau of Justice Statistics (BJS). It tracks a sample of 38,624 prisoners released from 15 state prisons in 1994 over a period of 3 years. The vast majority of the archived database consists of information on each releasee's entire officially recorded criminal history. This includes all recorded adult arrests through the end of the follow-up period. These data were obtained from state and FBI automated RAP sheets which include arrest, adjudication, and sentencing information. Each arrest event includes information on adjudication and sentencing related to that event if such action was taken. Unfortunately, however, the data do not contain detailed information on when

these individuals were released from prison if they were imprisoned after a particular arrest event.¹

In addition to the detailed dated event history data, this database also contains a limited amount of demographic and related information. Demographic measures available in the database include date of birth, race, ethnicity, and gender. Some detail is available about the type of release from prison (e.g., parole, mandatory release, etc.) and some about the type of admission into prison (e.g., new court commitment, new court commitment with a violation of conditions of release, etc.). However, this information is available only for the 1994 release and not for all prior (or future) arrest events.

Since the emphasis of this effort was to develop an analytical approach, I have restricted the analysis to rearrest only. Application to other type of outcomes (reconvictions, reincarcerations, self-reported offending patterns, or relapse into drug involvement, etc.) is straightforward.

Before conducting the analysis, some diagnostic checks were run on the data to ensure they were compatible with the model requirements. Since the data are based on official records and possible disparate sources of date information (e.g., date of birth obtained from the state data and from the FBI data could differ), I first computed the ages for each of the arrests in the data. Then, I checked for the chronology of these dates and checked to see if the age variable was well defined. I created flags for any *individual* that had records that were not in proper chronological order or whose ages were incorrect/impossible (e.g., negative or below 15). In addition, I created flags that identified any individuals that were missing information on all ages or that had gaps in their age variable. For example, individuals that had appropriate ages for the first and second arrest events but were missing age on the third event and again had appropriate ages for all subsequent arrests were flagged as potentially problematic. After creating these flags, I performed a list wise deletion of records—i.e., all records for individuals with any problem (as determined by the various flags) were dropped from the analysis set.

Additionally, the data contains a variable ANALYSIS that flags all records that were included in the BJS report titled *Recidivism of Prisoners Released in 1994* (Langan and Levin 2002). The criteria for inclusion in the report are provided on page 14 of Langan and Levin (2002). In my analysis, I also excluded all persons that were not included in BJS's report (i.e., persons flagged as ANALYSIS=0).

3.1.2. Data structure

After removing persons who either had some problem in their arrest histories or were not included in the BJS report, the remaining sample consisted of 32,628 persons across 15 states. In addition, since the sample for California releasees was very large (nearly 60,000

¹This implies that the data are unable to calculate street time. However, the data do provide information on the adjudication outcome at each successive arrest events that I utilize in the models.

person-events before prison release) I used a random subset of 2500 individuals (21,838 person events) from the California sample for estimating the pre-prison criminal history accumulation process. For the analysis of the post-release data, however, all individuals from California were included in the study. The final pre-release dataset therefore consisted of 21,226 individuals across the 15 states whereas the post-release data consisted of the 32,628 individuals.

Arrest records for these persons were next re-structured into a hierarchical person-event level file. That is, arrest events of each person were all clustered in chronological order. The arrest histories were next truncated after the first post-release re-arrest event. Recall that, for the post release period, we are only examining the first rearrest event. For those persons that were not arrested after release, the arrest age was set to the age at censoring (i.e., release age + 3 years).

The data were structured similar to the arrest profiles displayed in Table 2.1. In addition to the key criterion variable—age at arrest—the data were also manipulated to create a set of individual level fixed covariates as well as covariates changing over time.

3.1.3. Key variables included

The key independent variables used in estimating the pre-release criminal history accumulation process included the arrest number (EVENTNUM), the age at first arrest (AGE1ST), whether or not the individual was confined as a result of the previous arrest event (CONFLAST), and a measure of the number of years taken to reach each arrest event cumulated through the last arrest event (CARAGE). AGE1ST and CONFLAST were set to 0 for the first arrest event.

Besides CARAGE, the variables used in this part of the analysis are self explanatory. CARAGE was defined as a measure that captures the evolution of the heterogeneity in the sample members as they aged. It is defined as

$$\text{CARAGE}_{rn} = \sum_{j=1}^r \frac{a_{jn}}{j} \quad \forall r, n, \quad (3.1)$$

and it captures variation in the past criminal history up to the current arrest in such a way that it distinguishes people who are closer to their past arrest “clusters” from those that are further. Table 3.1 shows hypothetical past arrest histories of two individuals and demonstrates the calculation of CARAGE at each arrest event. Note that both individuals have the same CARAGE until their 2nd arrest because they follow the same path. As they differ in their arrest patterns CARAGE begins to record this heterogeneity. In fact, individual A gets a higher CARAGE on his 3rd arrest because he is “closer” to his past arrest cluster at age 30 than individual B is at age 35. After that, both individuals are rearrested at age 40 but their CARAGE continues to record their heterogeneous pasts. In this sense, the variable records heterogeneity in past offending patterns and, all else being equal, assigns a higher

Table 3.1: Computing CARAGE for two arrest profiles.

Individual A				Individual B			
r	a_r	a_r/r	CARAGE	r	a_r	a_r/r	CARAGE
1	20	20.0	20.0	1	20	20.0	20.0
2	25	12.5	32.5	2	25	12.5	32.5
3	30	10.0	42.5	3	35	11.7	44.2
4	40	10.0	52.5	4	40	10.0	54.2

score to those that are closer to their past arrest clusters. In the modeling stage, I include the lagged value of this measure in the hazard model. As with the other lagged variables, I set CARAGE=0 for the first arrest event.

The same set of basic variables were used to model the past criminal history accumulation process as well as the first re-arrest after release (recidivism). This was done in order to ensure that any deviations among the trajectories are attributable to the two different age segments of the releasee’s life. Comparisons of these trajectories produced the δ measures as well as the classifications. To understand what variables predict the deviation of the counterfactual and post-release paths, I included, in addition to the variables listed above, demographic characteristics, the type of release, the age at release, and the most serious offense for which incarcerated. Table 3.2 provides a summary of the sample used in the analysis.

Note that the variable CONFLAST captures adjudication outcomes at the last arrest event. It would seem, therefore, that this variable must be 1 for all the post-release sample. However, this does not need to be the case. Individuals may enter prison for reasons other than being convicted and sanctioned to some amount of confinement. For example, persons released from prison in 1994 could have entered prison for violating existing conditions of a previous release. However, it should be noted that the proportion of cases in Virginia that seem to be recorded as having some confinement as a result of the last arrest is too low (3 percent in the pre-release sample and 2 percent in the post-release sample). In all likelihood, this is an error in the data system. However, in this analysis I have used this variable as it is.

With the exception of the state of California the number of persons in the pre-release sample is exactly equal to the number of persons in the post-release sample. This is because the cohort of interest is a prison release cohort and this group of individuals must have, at some point in their past, been arrested at least once. As noted above, a sub-sample of 2500 persons was taken for the California sample to ease estimation of the models.

The three release type variables PAROLE, MANDATORY, and CONDITIONAL are not necessarily mutually exclusive. For some states (CA, DE, IL, and MI) release type information was either unavailable or there was insufficient variation to create distinct flags. For some states (MD, NY, NC, TX, and VA), enough detail was available to al-

Table 3.2: Summary of sample used

	AZ	CA	DE	FL	IL	MD	MI	MN	NJ	NY	NC	OH	OR	TX	VA
Pre-release sample															
# EVENTS	10920	21838	10184	25729	19209	12509	9917	12196	17136	22616	12424	4424	19780	15541	14649
# PERSONS	1418	2500	659	2554	2299	1588	1939	1728	2128	2390	2047	1100	1465	2410	2001
ARRESTAGE	26.93	26.61	23.87	27.86	25.60	26.67	26.25	25.86	25.90	25.66	26.84	26.42	28.71	27.33	27.07
EVENTNUM	8.15	8.72	11.75	9.39	8.84	6.99	5.05	6.86	8.30	9.19	5.78	4.51	10.94	6.00	7.14
AGE1ST	20.58	20.58	16.67	20.64	19.35	21.11	20.33	20.02	20.08	19.89	20.84	21.73	20.09	20.24	20.93
CARAGE	46.24	47.35	48.33	51.30	45.20	44.97	35.02	41.12	44.74	47.00	39.44	32.38	55.70	39.47	44.37
CONFLAST	0.25	0.27	0.10	0.22	0.17	0.28	0.33	0.45	0.30	0.37	0.44	0.25	0.34	0.24	0.03
Post-release sample															
# PERSONS	1418	6902	659	2554	2299	1588	1939	1728	2128	2390	2047	1100	1465	2410	2001
EVENTNUM ^a	8.70	9.66	16.45	11.07	9.36	8.88	6.11	8.06	9.05	10.46	7.07	5.02	14.50	7.45	8.32
AGE1ST	21.96	23.62	17.98	22.46	20.83	22.14	22.15	21.68	21.59	21.85	22.86	24.51	22.18	22.13	22.36
CARAGE	56.17	60.26	64.56	64.97	54.58	59.09	48.45	54.01	55.87	59.93	54.12	45.28	73.85	55.65	56.93
CONFLAST	0.51	0.50	0.52	0.26	0.46	0.63	0.82	0.86	0.73	0.71	0.85	0.37	0.79	0.78	0.02
RELAGE	33.49	34.78	31.19	34.30	31.60	32.86	34.02	31.01	32.79	33.55	31.51	34.06	35.50	34.39	33.14
BLACK	0.17	0.27	0.68	0.47	0.57	0.73	0.49	0.32	0.60	0.49	0.62	0.38	0.15	0.42	0.61
VIOLENT	0.33	0.61	0.30	0.53	0.51	0.40	0.45	0.42	0.41	0.44	0.40	0.60	0.55	0.47	0.34
PROPERTY	0.27	0.14	0.14	0.20	0.22	0.23	0.25	0.40	0.24	0.22	0.26	0.16	0.21	0.23	0.27
DRUG	0.26	0.16	0.38	0.18	0.18	0.26	0.20	0.15	0.22	0.20	0.24	0.17	0.16	0.20	0.26
PAROLE	0.77	0.00	0.08	0.70	0.00	0.44	1.00	0.21	0.73	0.54	0.27	0.64	0.63	0.41	0.40
MANDATORY	0.02	1.00	0.00	0.01	0.98	0.47	0.00	0.77	0.00	0.32	0.67	0.00	0.36	0.39	0.55
CONDITIONAL	0.79	1.00	0.08	0.70	0.98	0.91	1.00	0.98	0.73	0.85	0.94	0.64	0.99	0.80	0.95
CENSORED	0.38	0.46	0.14	0.35	0.30	0.33	0.61	0.40	0.42	0.42	0.46	0.73	0.33	0.55	0.41
RECIDIVISTS	0.62	0.54	0.86	0.65	0.70	0.67	0.39	0.60	0.58	0.58	0.54	0.27	0.67	0.45	0.59
RECIDAGE ^b	33.09	33.38	31.12	33.04	30.85	32.39	33.32	30.38	31.94	32.85	30.57	32.71	34.48	33.28	32.96
CENSORAGE ^c	38.82	40.56	39.79	41.44	38.40	38.59	38.28	36.56	38.38	38.87	36.90	37.99	42.07	39.24	37.95

^a Average re-arrest number at risk of upon release.

^b Only computed for those that recidivated within the follow-up periods.

^c Only computed for those that did not recidivate within the follow-up period.

low a classification of release type in three categories—PAROLE, MANDATORY release to supervision, and unconditional release. For others (AZ, FL, NJ, and OH) the only available information was whether the release was CONDITIONAL or otherwise. Finally, for MN and OR the only available information was whether the release was for PAROLE or MANDATORY release. Hence, when analyzing the effects of release type on the likelihood of the prisoner’s experience being deterrent or otherwise, separate models were estimated for groups of states to increase statistical power.

VIOLENT, PROPERTY, and DRUG refer to the most serious offense for which the prisoner was serving time when (s)he was released in 1994.

Finally, note that for some states the average age at which persons recidivated (RECIDAGE) would seem to be at or below the average age at which prisoners were released. However, this is misleading because the age of recidivism is computed *only* for those that were rearrested within the follow-up period. Similarly, the age at censoring (CENSORAGE) is computed *only* for those that were censored within three years of release.

Before, proceeding with the estimation and analysis of the hazard models, I first conducted some simple graphical diagnostics. I present those next.

3.2. PREDICTABLE PATTERNS

Before proceeding with model estimation, it would be good to assess whether the arrest histories contain any predictable patterns. After all, the entire strategy rests on such patterns existing. Moreover, this release cohort is a mixture of several birth cohorts and one might consider the sample too heterogeneous to capture in a single model. To that end, I first construct some basic Kernel density plots of the ages at various arrest events. The density plots for arrest events one through 20 (DEN01 - DEN20) are presented in Figure 3.1.

As is evident, there is a very predictable pattern visible. The pattern has two components. First, the age distribution of each successive arrest shifts slightly to the right as we go from lower arrest numbers to higher. Second, the dispersion of the distribution increases as we move from lower to higher arrest numbers. Recall that our flexible hazard model utilizes precisely these moments to recover information about the trajectories. Hence, if we are able to capture the process underlying these distributions, we should be able to project with fair amount of confidence what we could have expected in the absence of incarceration.

Of course, we cannot simply model the age distribution directly because this masks the dependence structure between successive arrest events. Therefore, we need to be able to model the hazards appropriately while using the predictable pattern observed in Figure 3.1. The formulation of the flexible functional form models in the previous chapter afford us that opportunity. Note, for example, that the constraints that we impose in (2.9) and (2.15) explicitly link the unknown hazards to the first two moments of the age of arrest. One of the reasons we typically need to model the second moment is if there is reason to believe that the pattern has systematic over or under-dispersion. If not, a simple moment based

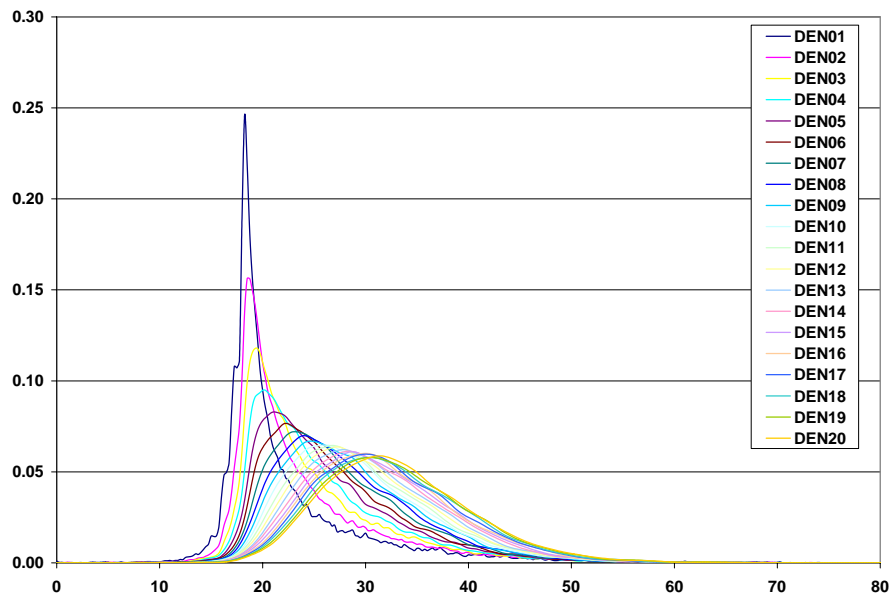


Figure 3.1: Kernel density plots of the age distribution of arrest events one through 20

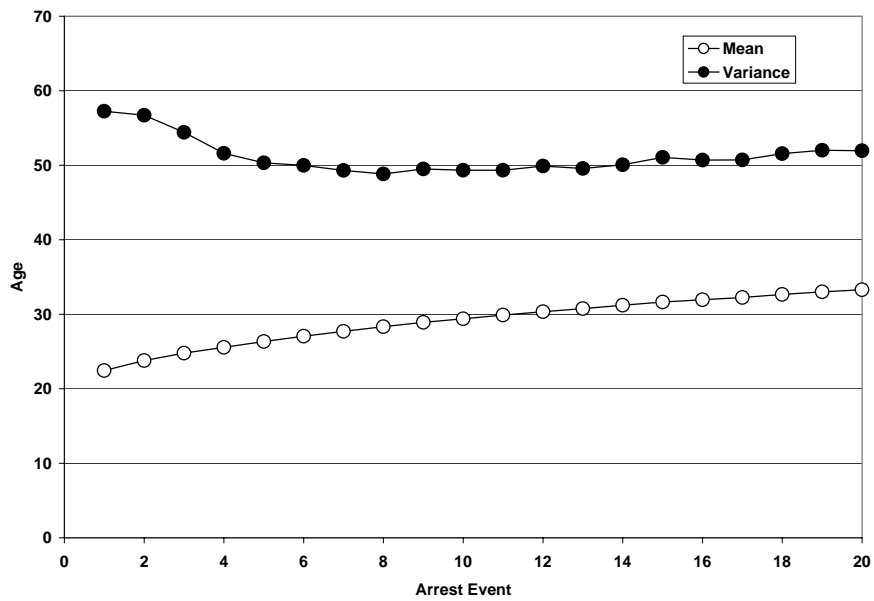


Figure 3.2: Means and variances of arrest events one through 20

model (e.g., Poisson) of the age distribution would suffice. Figure 3.2 plots the mean age and its variance for these 20 arrest events. Again, it is evident that the variance exceeds the mean at all arrest events *and* that the variance evolves in a non-linear way—first reverting towards the mean rapidly and then moving towards it more slowly.

3.3. MODELS OF THE CRIMINAL HISTORY ACCUMULATION PROCESS

In this section, I present the model estimates of the pre-release criminal history accumulation process. In order to keep the estimation manageable and to afford the model full flexibility, I estimated separate models for each of the states. The form of the model is held fixed across all state samples.

First, I present some evidence that the clustering of observations does in fact provide for biased (typically downward) standard errors. Consider, the model for Arizona. Table 3.3 shows the results of the information-theoretic model and presents three sets of asymptotic standard errors. The first set (TRAD) are those computed by inverting the negative Hessian of the dual objective function, the second set (SAND) are the sandwich estimates, and the third set (MODS) are the modified sandwich estimates. As is expected, the sandwich estimates of the standard errors are higher than the traditional estimates and the modified sandwich estimates are higher still. This is because both the traditional as well as the simple sandwich estimates ignore the clustering of the observations. Although, in this example, all the parameters remained statistically significant irrespective of the a.s.e. estimate used, as is evident from the various Wald- χ^2 values provided, there are huge reductions in the confidence we have about several of these Lagrange Multipliers when we account for the clustering. For the rest of this report, therefore, I err on the side of caution and use the modified sandwich estimates for making inferences.

Since the models are formulated in terms of hazards, a negative Lagrange Multiplier implies that the variable in question decreases the hazard's path or, put another way, the variable in question increases the expected duration to the next event. As such, the negative values of the parameters for EVENTNUM are consistent with Figure 3.1 and Figure 3.2. That is, increases in arrest numbers are associated with higher age (duration from birth to event). Moreover, the *positive* sign on the corresponding β_k multipliers suggests that the increasing age associated with increasing event numbers is at a decreasing rate. This simply means that the relationship between the arrest number and the hazard trajectory is non-linear. Note that all the β_k parameters have the reverse sign relative to the corresponding α_k parameters.

Similarly, increases in age at first arrest are associated (as expected) with increasing age at subsequent arrest (i.e., decreasing hazard paths for subsequent events). Moreover, this relationship is non-linear. CARAGE, also as expected, has a positive coefficient in the hazard model. Recall that CARAGE measures the closeness to past clusters of arrests. As such, a positive coefficient in the hazard model suggests that being close to a prior cluster decreases the duration and increases the hazard of the next event. As with the other

Table 3.3: Pre-prison based hazard models of the criminal history accumulation process of prisoners released in 1994 in Arizona

	Lagrange	TRAD		SAND		MODS	
	Multipliers	a.s.e.	χ^2	a.s.e.	χ^2	a.s.e.	χ^2
	α_k						
INTERCEPT	-0.5762	0.0124	2157	0.0268	461	0.0846	46
EVENTNUM	-0.0323	0.0009	1318	0.0017	358	0.0045	51
AGE1ST	-0.0056	0.0005	144	0.0011	27	0.0018	9
CARAGE	0.0163	0.0002	4627	0.0005	1218	0.0016	97
CONFLAST	0.0887	0.0113	62	0.0191	22	0.0175	26
	β_k						
INTERCEPT	0.1539	0.0033	2118	0.0080	371	0.0280	30
EVENTNUM	0.0086	0.0002	1319	0.0005	327	0.0013	46
AGE1ST	0.0011	0.0001	91	0.0003	13	0.0005	4
CARAGE	-0.0043	0.0001	4200	0.0001	985	0.0005	66
CONFLAST	-0.0264	0.0033	66	0.0056	22	0.0050	27

Note: Critical value for the χ^2 test at 0.05 level with 1 degree of freedom is 3.84.

parameters, this too has a non-linear link with the outcome of interest.

CONFLAST has a positive effect on the hazard path. This seems surprising at first glance. Being confined should take one off the street for some time, thus the age for the next event should be pushed out (increase) and the hazard should decrease. However, it is also possible that being confined after the arrest implies a higher level of severity of behavior that someone not confined. As such, it should decrease the age at the next arrest (i.e., increase hazard).

In order to see what the projections from this model look like, in Figure 3.3, I have simulated the predicted post-release offending trajectory for a particular individual profile. This individual was arrested for the first time at age 15, and then subsequently was rearrested at ages 22 and 25 after which he was incarcerated. He was released from prison at the age of 30. He is therefore at risk of his 4th rearrest. Figure 3.3 shows the counterfactual hazard trajectory (left scale) predicted by the model for this individual from his release age (30) to age 75 (effectively, his entire residual life). Based on this counterfactual hazard, the cumulative density function (right scale) traces the predicted probability of being rearrested within a certain number of years. For example, within three years of release, at age 33, the CDF is only about half a percent. In other words, this individual is *not* predicted to be rearrested within the three year follow-up period using knowledge only about the way he was accumulating his criminal record.

Similar individual trajectories can be plotted for *each* individual in the sample. Different criminal history accumulation processes will result in very different predictions about

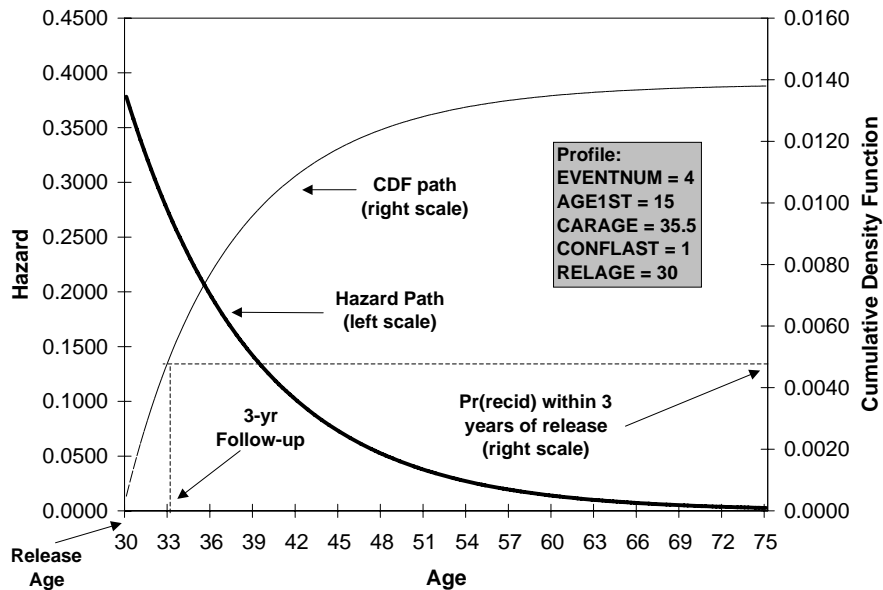


Figure 3.3: Counterfactual trajectory for a particular release

the future. In the next section, I present more comprehensive findings by computing predictions from these counterfactual trajectories for each individual. I also present a comparison of these counterfactual predictions with actual offending observed within three years of release.

3.3.1. State-specific hazard model estimates

In this section, I present and discuss the state specific estimates of the hazard models. Since the actual values of the parameters are less important than their signs, I summarize all the parameter estimates in Table 3.4 using the following conventions. Parameters that are positive and significant at the 95 percent confidence level (using the modified sandwich estimator for the asymptotic standard errors) are indicated with a ‘++’, parameters that are negative and deemed statistically significant using the same criteria are indicated with a ‘--’, and parameters that are insignificant are denoted ‘0’. Significance at the 90 percent confidence level is indicated by a single ‘+’ or ‘-’. Detailed state specific estimates of the hazard models are provided in Appendix A of this report.

With some exceptions, models from all states largely mirror the findings from Arizona discussed in the last section. The exceptions typically involve the Lagrange Multiplier corresponding to the CONFLAST flag. Qualitatively, the rest of the predictors are fairly consistent across states with the exception of NY where increasing arrest numbers seem not to be associated with decreased hazard (increased age) for the next arrest event.

In Table 3.4, I also provide estimates of the projections from these models. These

Table 3.4: Summary of the state-specific hazard models of the pre-prison criminal history accumulation process and their projections for the three-year post-release period

	AZ	CA	DE	FL	IL	MD	MI	MN	NJ	NY	NC	OH	OR	TX	VA
α_k															
INTERCEPT	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--
EVENTNUM	--	--	--	--	--	--	--	--	--	0	--	--	--	--	--
AGE1ST	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--
CARAGE	++	++	++	++	++	++	++	++	++	++	++	++	++	++	++
CONFLAST	++	++	0	++	0	++	+	++	+	++	++	++	++	++	++
β_k															
INTERCEPT	++	++	++	++	++	++	++	++	++	++	++	++	++	++	++
EVENTNUM	++	++	++	++	++	++	++	++	++	0	++	++	++	++	++
AGE1ST	++	++	++	++	++	++	++	++	+	++	++	0	++	++	++
CARAGE	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--
CONFLAST	--	--	0	--	-	--	-	--	-	--	--	--	--	--	--
3-year re-arrest projections from individual criminal history-based (counterfactual) trajectories ^a															
Projected	88.3	82.1	95.1	87.9	86.7	90.2	80.3	86.1	86.7	90.8	86.0	73.1	90.0	82.4	90.0
Actual	62.1	54.1	86.5	65.4	69.8	66.6	39.3	60.4	58.1	58.3	54.4	27.2	66.6	45.0	58.8
False-Positives	34.3	39.4	11.5	30.5	25.0	30.6	56.6	35.0	37.4	38.9	42.0	68.3	28.5	50.4	41.2
False Negatives	34.9	24.3	46.5	35.1	36.3	40.4	22.5	32.4	29.2	30.6	31.3	14.9	22.6	23.4	32.8

Note: ++ = Positive coefficient with 95 percent confidence; + = positive coefficient with 90 percent confidence; -- = negative coefficient with 95 percent confidence; - = negative coefficient with 90 percent confidence; and 0 = coefficient statistically insignificant.

^a Projections are based on converting each individual's predicted hazard trajectories into cumulative densities using (3.2). The criteria for an individual to be projected to fail within 3years of release is if his(her) cdf had reached 0.50 within three years after release.

projections are constructed as follows. Since estimated hazards, probability density functions, as well as cumulative density functions are different ways of characterizing the same underlying process, we can convert one into the other fairly easily (Allison 1995, pg 16). For example, the cumulative density function may be estimated as

$$\text{CDF}_{mrn} = 1 - \exp\left(-\sum_{j=1}^m d_{rjn}\hat{\delta}_{rjn}\right) \quad \forall r, m, n, \quad (3.2)$$

where $d_{rjn} = 0$ for all points before the age of release and $d_{rjn} = 1$ for all points after release and $\hat{\delta}_{rjn}$ is the projected hazard for all ages based on the estimated Lagrange Multipliers. This allows us to compute the cumulative probability of re-arrest for the next arrest assuming the individual survives to some point after release. Here, I present summary statistics for the three year window. In the lower panel of Table 3.4 I present the proportion of state specific sample members that are predicted to be re-arrested within three years of release *based purely on knowledge about their prior criminal history accumulation process*. Note, that we should not expect these predictions to be very good *unless* the model has captured some salient underlying feature of the process under study. This is because the current prediction problem is very different from predicting in-sample or predicting out-of-sample using a randomly sub-setted validation sample. Here, the predictions are being done for a period beyond the estimation sample.

In the lower panel of the table, I present the proportion predicted to be rearrested within the three year follow up period using the following rule. If the CDF is larger than 0.50 by three years of release, the individual is projected to be rearrested, otherwise not. In addition to the predictions, I also present the proportion of the sample that actually failed within the follow-up period as a way to assess the accuracy of the projections. Lastly, I present the false positive and false negative rates resulting from the criterion described above.

The findings in this part of the table are quite remarkable. Although the counterfactuals consistently over-predict the three-year rearrest rates, the overall rate seems to follow the trend of actual arrests across states. That is, states that experience high levels of actual rearrest rates are those that are predicted to have higher levels of rearrest rates, relative to others. A simple scatter plot of the state specific actual and predicted rates demonstrates this point well (Figure 3.4). Although the predictions are always above the actual rates, i.e., the counterfactual are consistently over-predicting recidivism, the scatter plot clearly shows the positive association between the actual and the predicted rates.

More remarkable, however, are the false positive and false-negative rates. With the exception of MI, OH, and TX, where the false positive rates exceed 50 percent, the false positive rates in all other states is well below this amount. In fact, averaged across all 15 states (including MI, OH, and TX), the false positive rate is 38 percent and the false negative rate is 27 percent. This means roughly two-thirds of those individuals projected to be re-arrested within a three-year window based purely on knowing how they were accumulating

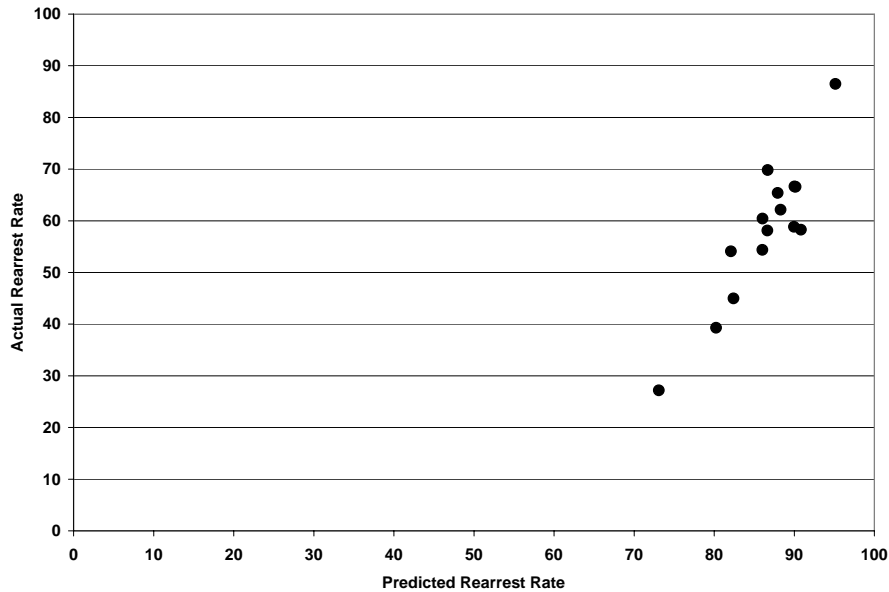


Figure 3.4: State specific predicted three-year rearrest rates by actual rearrest rates

crimes in their past, did actually get rearrested. Similarly, roughly three-quarters of those predicted to not be rearrested within the three year follow-up period actually did not fail.

Given the fairly predictable patterns that can be seen in Figure 3.1 and Figure 3.2, these findings, although remarkable, should not be that surprising. However, these projections are based on models that follow and capture long term secular trends over the life course of individuals. As such, they should be expected to perform much worse in the short run. To see that, I next computed the false positive and false negative rates for short term quarterly projections aggregated across all 15 states.

To do so, I first classify individual as being projected to be rearrested within the first quarter of release or not. Then I compare these projections with actual rearrests. Next, of those that were not projected to be rearrested within the first quarter, I classify individuals as being projected to be rearrested within the second quarter. I then compare these projections with the actual rearrests within this quarter. This allows me to compute a sequence of 12 quarterly short-term false positive and false negative rates. Figure 3.5 shows these sequences over the three years after release. Here it becomes evident that despite the fairly accurate long-term projections, the short-term performance of the counterfactual model is very poor.

It should be noted that these models were *not* developed for making short term projections. Rather, they were developed as a way of capturing longer term trends in offending trajectories over the pre-prison life course so that they could be used as a backdrop against which to assess the actual post-release trajectories. In the next section, I present results of the models that use these projected counterfactuals as the trajectory towards which each

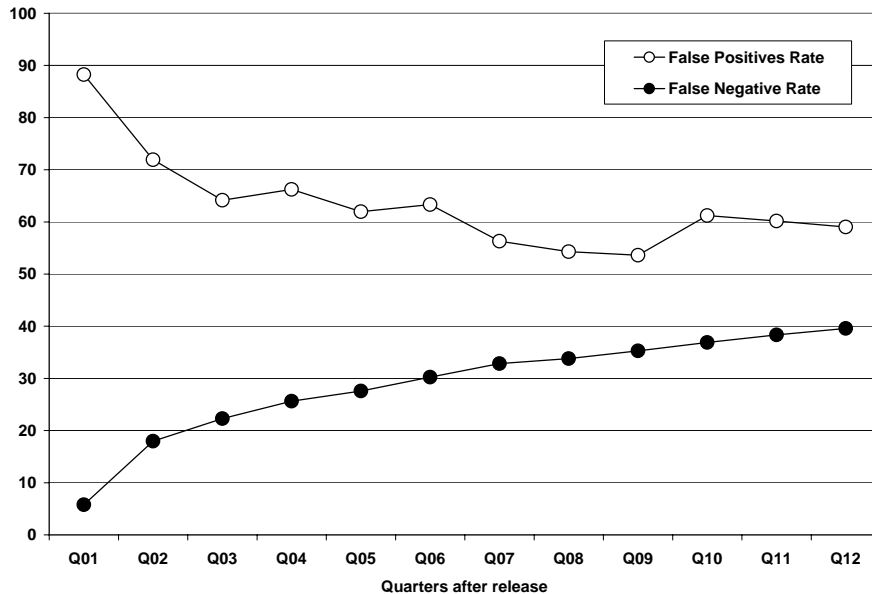


Figure 3.5: False positive and false negative rates when the counterfactual trajectory is used for making short-term (quarterly) projections

post-release trajectory is shrunk while ensuring that the evidence in the sample (in the form of constraints) is still satisfied.

3.4. MODELING POST-RELEASE TRAJECTORIES AS DEVIATIONS FROM COUNTERFACTUALS

As discussed in the previous chapter, the sole purpose of developing the counterfactual was to assess the post-release actual rearrest patterns in an attempt to understand how, if at all, the current incarceration has deflected the trajectory a particular individual was on. In order to do so, I first projected the rearrest hazard for each of the individuals in the sample utilizing knowledge about the event number they were at risk of when they came out of prison in 1994 (i.e., how far along on their arrest sequence they were), their age at release (i.e., how far along in their life they were), and all other variables used in the pre-prison based models. Note that even though the post-release sample includes censored observations—i.e., not everyone is rearrested within the follow-up period—we have a counterfactual trajectory for each and every individual in the sample. This counterfactual merely replace s_{rmi}^0 in the objective function (2.17) and we proceed to optimize it just as before.

Although the statistical significance of the Lagrange Multipliers can still be tested using the sandwich and modified sandwich estimates of the asymptotic standard errors, the interpretation of the Lagrange Multipliers is now different. Recall that a ‘+’ value on α_k now symbolizes an upward pressure on the trajectory *relative* to the counterfactual while a

Table 3.5: Summary of the state-specific hazard models of the first post-release rearrest event and their projections for the three-year post-release period

	AZ	CA	DE	FL	IL	MD	MI	MN	NJ	NY	NC	OH	OR	TX	VA
α_k															
INTERCEPT	++	++	++	++	++	++	++	++	++	++	++	++	++	++	++
EVENTNUM	++	++	++	++	++	++	++	++	++	++	++	++	++	++	++
AGE1ST	0	0	++	0	--	-	0	0	0	0	0	--	--	0	--
CARAGE	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--
CONFLAST	-	--	-	--	-	--	0	--	0	--	--	--	--	0	--
β_k															
INTERCEPT	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--
EVENTNUM	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--
AGE1ST	0	0	--	+	++	++	+	0	+	0	++	++	++	0	++
CARAGE	++	++	++	++	++	++	++	++	++	++	++	++	++	++	++
CONFLAST	++	++	+	++	++	++	0	++	0	++	++	++	+	+	++
3-year re-arrest projections from individual trajectories as deviations from their counterfactuals ^a															
Projected	77.9	61.7	97.0	77.2	81.1	80.0	26.6	73.2	69.2	69.5	62.0	12.3	77.0	41.7	72.7
Actual	62.1	54.1	86.5	65.4	69.8	66.6	39.3	60.4	58.1	58.3	54.4	27.2	66.6	45.0	58.8
False-Positives	29.2	29.5	12.1	24.3	21.3	25.6	41.9	27.8	28.3	28.9	32.3	40.7	22.4	39.1	32.8
False Negatives	31.5	27.7	40.0	30.4	31.7	35.0	32.5	28.3	27.7	29.2	32.6	22.7	30.0	33.6	36.5

Note: ++ = Positive coefficient with 95 percent confidence; + = positive coefficient with 90 percent confidence; -- = negative coefficient with 95 percent confidence; - = negative coefficient with 90 percent confidence; and 0 = coefficient statistically insignificant.

^a Projections are based on converting each individual's predicted hazard trajectories into cumulative densities using (3.2). The criteria for an individual to be projected to fail within 3years of release is if his(her) cdf had reached 0.50 within three years after release.

‘-’ value implies downward pressure on the trajectory *relative* to the counterfactual.

Consider, for example, a situation where all parameters are found to be statistically indistinguishable from zero (i.e., insignificant). That would mean that the post-release trajectory is statistically indistinguishable from the prior (i.e., the counterfactual). Hence, if one or more of the parameters are found to be significantly different from 0, this would indicate that, in the sample as a whole, there has been a deviation of at least *some* of the post-release trajectories from their counterfactuals. It should not be taken to mean that *every* trajectory has deviated from its counterfactual.

I present the results of the post-release sample in Table 3.5 in a manner analogous to the presentation in Table 3.4. The pattern of coefficients are different from those in Table 3.4. That is to be expected. However, unlike the pre-release models, the post-release model parameters vary a lot more across states. Moreover, some parameters even take the opposite signs. For example, the value of α_k for AGE1ST is positive and significant for DE but is negative and significant for IL. In a similar manner, the signs of the significant values of β_k for AGE1ST vary considerably across states. This suggests that the way trajectories are deflected between the pre- and the post-release periods varies across states and that the effects of AGE1ST in particular can even be reversed across different states.

On the other hand, there are some factors that exert unambiguous pressure on offending trajectories. Being later in the criminal career exerts an upward pressure on the offending trajectory relative to the counterfactual. That is, large values of EVENTNUM are associated with an upward pressure on the offending trajectory. Similarly, being closer to past cluster exerts a downward pressure on the trajectory relative to the counterfactual. As noted above, these are aggregate statements about the sample as a whole. The actual deflection for each and every releasee will be computed in the next section and the determinants of these *individual-level* deflections will be investigated there.

Signs of the deflection of the trajectories can be seen directly in the projected rearrest rates as well as the false positive and false negative rates. Although the prediction problem is no longer an out-of-sample one, simple comparisons between these projected rearrest rates and the counterfactual projections of the last section shows that the post-release projections are far superior to those of the counterfactuals. With the exception of MI and OH, where the false positive rates are about 40 percent, we see that the false positive rate typically is between 25 and 30 percent.

As further evidence that the posterior trajectories are sufficiently deflected from the priors, we can compute and plot the short-term (quarterly) predictions from these models. Figure 3.6 shows these curves. Cursory comparison with Figure 3.5 shows that the false positive rate is substantially lower. Moreover, within about 6 months of release, both the false positive and false negative rates are below 50 percent and then remain stable.

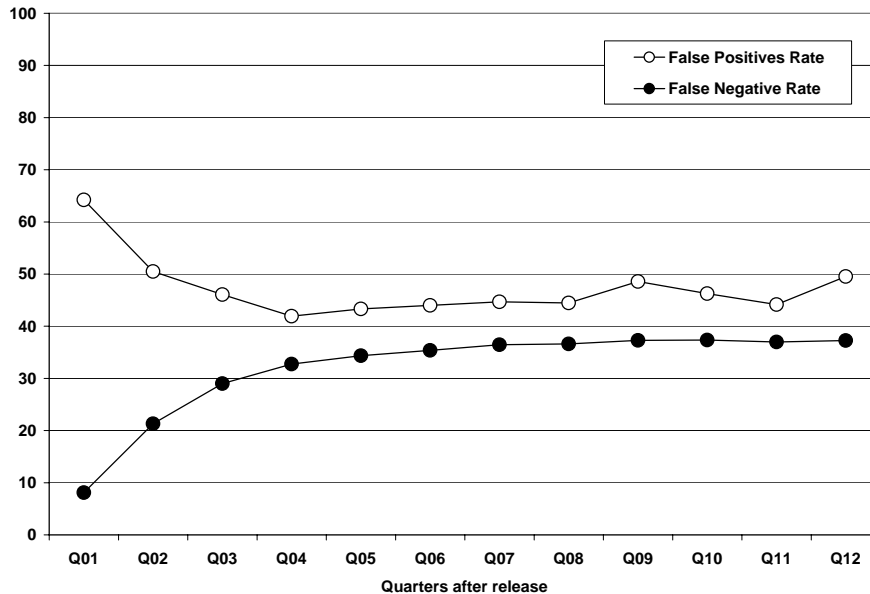


Figure 3.6: False positive and false negative rates when the post-release based trajectory, deviating from the counterfactual, is used for making short-term (quarterly) projections

3.5. CLASSIFYING AND UNDERSTANDING THE DETERMINANTS OF THE PRISON EXPERIENCE

The final set of results presented in the report are of models used to study the effects of various predictors on the incarceration experience quantified alternately as a continuous measure and as a categorical one.

The averaged divergence measure δ that was defined in the previous chapter is used to study this aspect of the model. First, the classification. Using (2.23) as a way to classify individuals as having had a deterrent, an incapacitative, and a criminogenic experience, the data reveals that only a small part of the sample (4.3 percent) actually were classified as having had a criminogenic experience. The largest share of them were classified as having had an incapacitative experience (56.2 percent) and the remaining (39.5 percent) experienced some deterrent effects. Note that these classifications are based on the entire residual life of the releasee (up to age 100 in this analysis). It is not based on just the follow-up period. Hence, a large share of people do experience deterrent effects. These numbers do *not* merely reflect the fact that the counterfactuals over-predicted re-arrest rates within the follow-up period.

Next, I present the results of a few simple linear and logistic regression models that are aimed at assisting practitioners determine, or at the very least investigate, what factors may be helpful in maximizing any deterrent benefits, and minimizing any criminogenic harm, resulting from incarceration.

A word of caution before I present these results. The next few sets of results are merely provided to demonstrate the approach. I do not make any recommendations based on these results. Much more detailed information is needed before explicit policy recommendations could be enumerated.

3.5.1. Discrete choice models of the incarceration experience

First, consider simple logistic regression models of whether or not a releasee's prison experience will be deterrent (rather than merely incapacitative or even criminogenic). Since the proportion of releasees that were deemed to have had a criminogenic experience is fairly small, I combine these classified as having had a criminogenic and incapacitative experience into one category. Hence, the estimates I present in Table 3.6 are from models that attempts to link various available attributes to the likelihood of being deterred versus not. Once again, the table presented here only summarizes the signs of the various predictors in affecting the likelihood a deterrent effect. Detailed coefficient estimates are provided in the Appendix.

Four sets of parameters are presented there. One of the key policy variables to be investigated—the type of release from prison—was not consistently available in all states. The variable was re-coded into discretionary release to supervision (PAROLE), mandatory release to supervision (MANDATORY), and unconditional release (UNCONDITIONAL). Based on this variable, I collapsed states into 4 groups. Group I includes all states that had sufficient detail to model the effects of various types of release mechanisms (MD, NY, NC, TX, and VA), Group II included states that only allowed a comparison of discretionary release to mandatory release (MN and OR), Group III included states that only allowed a comparison of conditional versus unconditional releases (AZ, FL, NJ, and OH), and Group IV included states that did not contain enough variation to permit estimating the effects of this policy variable on the effects of incarceration (CA, DE, IL, and MI).

Since the logistic regression models were predicting the probability of deterrent experience, therefore positive and significant coefficients can be expected to increase the likelihood of a releasee having been deterred as a result of this incarceration. Similarly, negative coefficients imply increased likelihood that the releasee had merely an incapacitative or even a criminogenic experience.

As should be expected, releasees that have higher numbers of prior arrests are *less* likely to experience deterrent effects. Those closer to their prior arrest clusters and those released later in life were *more* likely to experience deterrent effects. Surprisingly, those with later ages of first arrest were consistently less likely to experience deterrent effects. Among the Group I states, Blacks were more likely to experience deterrent effects while among Group IV states they were less like to be deterred. Males were less likely to be deterred by incarceration (among the states in Groups I, II, and IV) and, typically, prisoners released from Violent, Property, or Drug related crimes were less likely to experience deterrent effects (relative to Public Order crimes). Surprisingly, the release mechanism seemed

Table 3.6: Effects of predictors on the probability of a releasee having a deterrent (versus an incapacitative or criminogenic) incarceration experience.

	Group I ^a	Group II ^a	Group III ^a	Group IV ^a
# PRIOR ARRESTS	--	--	--	--
CARAGE	++	++	++	++
AGE1ST	--	--	--	--
RELAGE	++	++	++	++
BLACK	+	0	0	--
MALE	--	--	0	-
VIOLENT	0	-	--	--
PROPERTY	0	--	-	--
DRUG	0	--	0	0
PAROLE ^b	0	++
MANDATORY	0
CONDITIONAL	0	...

All models include an intercept term and fixed state effects.

... Variable not part of this model.

^a Group I: MD, NY, NC, TX, & VA; Group II: MN & OR; Group III: AZ, FL, NJ, & OH; and Group IV: CA, DE, IL, & MI.

^b Reference category is Unconditional for Group I model and MANDATORY for group II models.

to have minimal effect in explaining the type of experience release could expect. The only model in which the type of release played a significant role was among Group II states. Here, being released via discretionary release was more likely to result in a releasee being deterred than being released mandatorily.

As noted above, these findings are not intended to provide any specific policy recommendations. Rather, they are presented here as a means of showcasing the utility of the proposed analytical strategy in assisting practitioners in decision making. For instance, state and local authorities that have sufficiently detailed information about the programs that releasees participated in while in-prison, or the kinds of assistance being offered to them after release, whether or not they have employment available upon release, whether they are returning to a family with strong ties, etc., could all be used in the type of model described above in an attempt to study how, if at all these variables (many of which are choices available to practitioner and policy makers) can increase or decrease the likelihood that a releasee will be deterred from future crime.

Table 3.7: Effects of predictors on the average log deviation of the post-release trajectory from the counterfactual.

	Group I ^a	Group II ^a	Group III ^a	Group IV ^a
# PRIOR ARRESTS	--	--	--	--
CARAGE	++	++	++	++
AGE1ST	++	++	++	++
RELAGE	--	--	--	--
BLACK	0	0	0	0
MALE	++	++	++	++
VIOLENT	0	0	+	0
PROPERTY	0	0	0	0
DRUG	0	0	0	0
PAROLE ^b	0	–
MANDATORY	--
CONDITIONAL	0	...

All models include an intercept term and fixed state effects.

... Variable not part of this model.

^a Group I: MD, NY, NC, TX, & VA; Group II: MN & OR; Group III: AZ, FL, NJ, & OH; and Group IV: CA, DE, IL, & MI.

^b Reference category is Unconditional for Group I model and MANDATORY for group II models.

3.5.2. Linear regression models of the incarceration experience

In this section, I present results of using the δ statistic directly as the criterion variable. That is, rather than classify the average log divergence between the counterfactual and post-release hazard trajectories into discrete categories (deterrent, incapacitative, and criminogenic), δ can itself provide information on the incarceration experience. Therefore, simple OLS models can be used to study whether and to what extent various factors can be expected to increase/decrease the value of δ .

Note that larger positive values of δ imply strong criminogenic effects whereas large negative values of δ imply strong deterrent effects. Hence factors that can be expected to decrease δ significantly can then be considered as variables related with increased deterrent experiences. Hence, the results in this section are presented in a parallel fashion to those in the previous section. The same models are estimated for the same groups of states. Findings are presented in Table 3.7.

These regressions reveal some anomalous findings. First, the number of prior arrests and CARAGE now have the reverse effects as they did in the logistic regression models. That is, now, higher number of prior arrests is associated with a lower δ (implying larger deterrent effects) and being closer to the past clusters—i.e., higher CARAGE—implies larger values of δ (lower deterrent effects). These are qualitatively opposite to what was found in

the logistic regression analysis. As such, these findings should be viewed with some skepticism. It is possible, for example, that much of the co-variation between CARAGE and δ exists within a small range about zero. It is possible that this small range is completely included into the category of “incapacitation effect” when we convert the continuous δ into the classifications.

On the other hand, the linear regression findings lend strength to some of the other conclusions reached at using the logistic regression analysis. For example, RELAGE and AGE1ST have the same signs across all state groups *and* they have the same qualitative effect on the incarceration experience as was found in the categorical analysis. In a similar manner, females are (in this model) unambiguously more deterred by their incarceration experience than males. The offense for which releasees were incarcerated seems to have little or no contribution towards explaining variation in the deterrent effects. Finally, discretionary release (when compared with mandatory release) has a higher deterrent effect on releasees and mandatory release (as compared to an unconditional release) seems to have a higher deterrent effect on releasees. Similar sporadic findings of a deterrent effect of release mechanism were also found in the logistic regressions.

Hence, when used in concert, the two sets of analysis have the potential of strengthening the conclusions one may reach about the kinds of factors that can be expected to increase the deterrent benefits of incarceration and minimize its criminogenic harm.

3.6. SUMMARY OF FINDINGS

The research conducted, and reported on here, was largely a development effort. Despite that, some interesting findings emerged from the effort that are summarized below.

1. There was a fair amount of consistency among all the pre-prison based models of the criminal history accumulation processes across the 15 states analyzed. For example, being further along in the criminal career (i.e., being at risk of a higher arrest number) and starting the career later (i.e., having a higher age at first arrest) pretty consistently result in lowered hazard trajectories. Similarly, all else being equal, being closer to past arrest clusters, is consistently associated with increased hazard trajectories. There was less consistency among states when modeling the deviation between the counterfactual and actual rearrest hazard trajectories after release. Being later in the criminal career exerts an upward pressure on the offending trajectory relative to the counterfactual. Similarly, being closer to past cluster exerts a downward pressure on the trajectory relative to the counterfactual.
2. The criminal history accumulation process contains valuable information about the long-term secular trends in individuals’ offending patterns over the life course. The counterfactual trajectories, based on estimated models of the pre-prison based criminal history accumulation process and projected for the post-release period, perform remarkably well in predicting rearrests within three years of release.

3. As expected, the same counterfactuals do not perform as well when used for making short-term projections. The false-positive rates are at very high levels throughout the follow-up period. When updated with models of the post-release behavior, the models perform remarkably well.
4. In this analysis, large portions of the release cohort were classified as having had an incapacitative or a deterrent experience. A small proportion of the sample experienced criminogenic effects as a result of this incarceration.
5. Using these classifications as the criterion outcome, increased age at release and being closer to past clusters were consistently found to *increase* the likelihood of a releasee experiencing a deterrent effect. Having more prior accumulated arrests and having a later age at first arrest were both found to significantly *decrease* the likelihood of a deterrent effect. Being released to supervision was found not to deter releasees substantially.
6. Using the average log divergence between the counterfactual and the actual trajectories as the criterion some anomalous findings were uncovered. However, the effects of age at first arrest and age at release were qualitatively similar to what was found in the categorical analysis. Additionally, females were expected to experience larger deterrent effects than similar males.

3.7. CONCLUDING COMMENTS

In this chapter, I applied the analytical framework developed in this research effort to a particular data set. I estimated several models of the pre-prison criminal history accumulation process and used that to construct counterfactual trajectories for future offending patterns. Models of post-release offending trajectories for the next rearrest event were then estimated using the projected counterfactuals as prior knowledge. Furthermore, the post-release trajectories were compared with the counterfactuals for each individual in the post-release sample and values of the δ statistic (the average log deviation of the actual and counterfactual) were computed. Using the expected value of δ and its standard deviation, the current incarceration experience of each of the sample members was classified as having been deterrent, criminogenic, or merely incapacitative. Finally, simple models linking these experiences to available attributes were estimated and discussed.

The point of this exercise was to demonstrate the capabilities of the approach. As noted in the introductory chapter, no specific policy recommendations can or are being made as a result of this analysis. Its sole purpose was to develop and explain the analytical framework.

Before concluding this chapter, a point of clarification is in order. In this chapter, I have modeled the post-release trajectory as the evolution of the hazard *for the next arrest event* upon release. It is possible, though not explored in this report, to model the evolution

of hazards *for all future arrest events* after release. It is also possible to compute counterfactuals for each of these future rearrest events using estimates from the pre-prison based models. However, it seems somewhat awkward to speak of the deterrent, incapacitative and criminogenic effects of the current incarceration on the second, third, and subsequent rearrest after release. Consider, for example, if we are to find that, for a particular individual, this incarceration had an incapacitative effect for the 1st rearrest after release but a criminogenic effect for the 2nd rearrest after release. What are we to make of this finding? It seems to me cleaner to restrict these classifications to just the first rearrest event. Alternately, one could compute composite δ measures aggregated not only across the entire residual life of the release but across all subsequent rearrest events or aggregated for specific time periods (e.g., first six months following release). Exploring these extensions are promising areas for future work.

Chapter 4

Conclusion

In this chapter, I discuss the larger implications of this research effort and propose some promising directions for future research.

4.1. IMPLICATIONS

The analytical framework developed as a result of this research effort has important substantive, methodological, and practical implications.

4.1.1. Substantive implications

Substantively, the analytical framework developed here has the potential to shed light on a very important question: *How does incarceration affect individuals?* Although theoretical arguments for and against the use of incarceration as a crime control strategy abound, it is hard, in my opinion, to imagine that this important policy tool has the same effect on all persons at all ages and all times. As such, it would be very beneficial to be able to determine, or at the very least investigate, the types of individuals likely to be deterred by incarceration. In a similar way, it would be very beneficial to understand how incarceration can have differing impacts on the same people at various stages in their life and/or criminal careers. The framework developed here offers one way to directly investigate these issues.

There are several related substantive benefits that can be derived by extending this research in appropriate directions that are discussed in more detail below.

4.1.2. Methodological implications

When the detailed dated arrest histories of a sample of releasees is available to researchers, utilizing only one source of variation in the data—the total amount of criminal history accumulated prior to prison admission—for modeling the risk of future recidivism forces

analysts to waste valuable information and thereby forgo learning opportunities. A second source of variation available in these pre-prison arrest histories—the process by which individuals were accumulating these histories—contains immense amount of information about future offending patterns. The information-theoretic event-history models, developed in this research effort, allow this knowledge to be introduced into the modeling strategy in a very intuitive and easy way. The process by which individuals accumulate their pre-prison arrest histories, typically, have some very predictable patterns that can be modeled. These models allow simple projection of the risk (hazard) of future arrest events. These projections can be thought of as person specific micro-trajectories that trace out the evolution of rearrest hazards *had the individual not been incarcerated*. As such, they are perfect counterfactuals against which to assess the post-release offending patterns.

Statistical concepts such as Kullback-Leibler Directed Divergence measures, the family of Cressie-Read Power Divergence measures, and Information Entropy, are all inequality measures that capture the divergence between two probability distributions. Modifying these measures to capture divergence between two functions is straight forward. Therefore, building on information-theoretic foundations, divergence measures between counterfactual and actual trajectories can be developed that allow for a systematic definition of what it means for two trajectories to diverge *sufficiently*. One such measure was developed in this research effort. These measures allow for a simple classification of releasees into groups that were either deterred by their incarceration or were merely incapacitated or, in fact, had a criminogenic experience. Traditional modeling approaches, such as logistic and linear regressions, can then be used to investigate the correlates of these experiences.

Flexible functional form models of recidivism offer the possibility of increasing the predictive accuracy of the model because they are not bound by the assumptions of a particular functional form. For example, if researchers are unsure about the proportionality assumption, they may simultaneously impose proportionality and non-proportionality constraints using the data. That way, to the extent that one or the other models satisfies the real process generating the data, relevant Lagrange Multipliers will be distinguishable from 0 and the remaining will not. These flexible functional form models rely on, what is termed, the *Encompassing Principle* (see Chapter 14 in Hendry [1995]). They offer a nice way to introduce non-linearity, systematic heterogeneity, and mixed processes when modeling recidivism. In this research, the flexible hazard models were used to model both the criminal history accumulation process as well as the risk of post-release rearrest. Even if detailed arrest histories are unavailable to researchers, the information-theoretic approach can still be used vary profitably because it allows for very general forms for the links between attributes and the hazards.

4.1.3. Practical implications

Although much of the software needed for the analysis conducted here needed to be programmed from scratch, the availability of standard software allowing researchers to utilize

information and entropy based method is increasing rapidly. For example, SAS has introduced an experimental procedure under its ETS module called PROC ENTROPY that is designed for the estimation of linear and non-linear models using the Generalized Maximum Entropy (GME) approach introduced by Golan, Judge, and Miller (1996). Additionally, LIMDEP—another popular econometrics software—has recently added the GME methods for estimating binary and multinomial logit models.

Software needed to estimate generalized hazard models using the framework described in this report here is far from being developed. In the interim, researchers and practitioners will need to rely on routines and macros developed and made available to the public. In an Appendix to this report, I have printed out the SAS macro that I wrote in order to estimate the models presented in this paper. Researchers and practitioners are welcome to copy, edit, alter, and use that code freely. However, I do not offer any performance guarantees.

Depending on the size of the sample used as well as the hardware a particular research is utilizing, the performance can vary significantly. However, the procedure is very efficient. Using the IML module of SAS (Version 8.02), a model like that of Arizona's (presented in Table 3.3) took less than 30 seconds to converge on my Dell PC (with a 3.00 GHz CPU). Note that the pre-release data in Arizona has roughly 10,000 events. Using a quarterly grid from age 0 to 100 (i.e., $\mathbf{z} = (0, 0.25, 0.50, 0.75, 1, \dots, 99.5, 99.75, 100)'$) for the support space, this means that in each iteration, the procedure needed to evaluate a full $10,000 \times 401$ dimensional matrix. Despite that, the convergence was very rapid. With the California sample, the computer simply ran out of memory to store the matrix. Therefore, the sample needed to be truncated to 2500 individuals. This resulted in 21,838 events in the pre-release sample. For this sample, the model converged in 1.42 minutes. Therefore, despite the large sample sizes that state and local authorities may have at their disposal, the procedure should pose little or no problems on currently available computing power.

4.2. DIRECTIONS FOR FUTURE RESEARCH

The analytical framework developed in this project was not subject to simulation testing, as I concentrated on developing the framework and applying it to a substantive problem. An obvious direction for future research would be to assess the performance of the developed framework to Monte Carlo simulations. That effort would also help identify its strengths relative to existing approaches.

Another direction for future research, as was noted in the previous chapter, involves the expansion of the δ statistic to cover multiple rearrest events after release. A composite measure, aggregating the log divergence between the counterfactual and actual hazard trajectories for several rearrest events after release may (or may not) yield more clarity into the effects of incarceration.

As was noted at the end of Chapter 2, given that no model can hope to capture all

unobserved heterogeneity using available attributes, it may be desirable to allow the possibility of unobserved heterogeneity via finite mixture modelling techniques.

An interesting extension of the existing approach would be to allow the simultaneous modeling of various related repeated events. For example, the framework could be extended and used to study whether and how incarceration affects the *co-evolution* of the trajectories of offending and employment (or offending and drug use) over the life course.

Finally, it would be worth utilizing the above framework for exploring how the criminal history accumulation process is deflected by other interventions (e.g., marriage, divorce, relocation, drug treatment, etc.). A large amount of society's resources are spent on trying to divert individuals from criminal offending or drug use—outcomes that have been shown to have very predictable patterns. Typically, programs designed to do so are evaluated using the standard experimental or quasi-experimental approaches. These approaches are simply different research designs used for constructing plausible counterfactuals. However, there are several instances when experimental interventions are not possible and/or when comparable control groups are impossible to find. In such settings, it may be worth investigating whether the framework developed here can be used to construct plausible counterfactuals simply by modeling the process before intervention. In a sense, one would then be evaluating the success of the intervention using *embedded counterfactuals*¹—counterfactuals embedded in the individual's past—in order to study whether and to what extent the program was successful in achieving its goals.

¹Historians use this terminology to describe a mode of reasoning that allows them to investigate causes of historical events and actions that *cannot* be assessed using experimental or quasi-experimental approaches. See, for example, Schroeder (undated).

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Appendix A

Model estimates

In this Appendix, I provide detailed estimates of all the models summarized in Chapter 3. It is organized as follows. Table A.1 through Table A.15 provide parameters estimates along with diagnostics for each of the state specific models. The upper half of the panel provides estimates of the pre-prison criminal history accumulation process models. The lower half in each of these tables provides estimates of the post-release recidivism models *for the first release after release*. The model parameters reflect deviations from the pre-prison based counterfactuals.

Table A.16 through Table A.19 provide parameter estimates from the four sets of logistic regressions conducted on the likelihood of the individual's experience being deterrent versus not and Table A.20 through Table A.23 provide parameter estimates from the four sets of linear regressions conducted to explain variation in the δ statistic.

Table A.1: Pre-prison and post-release based hazard models of the criminal history accumulation process of prisoners released in 1994, AZ

		$\hat{\alpha}_k, \hat{\beta}_k$	a.s.e. ^a	Wald χ^2	p-value
<i>Pre-prison</i>					
α	INTERCEPT	-0.5762	0.0846	46.42	0.00
α	EVENTNUM	-0.0323	0.0045	51.09	0.00
α	AGE1ST	-0.0056	0.0018	9.38	0.00
α	CARAGE	0.0163	0.0016	97.22	0.00
α	CONFLAST	0.0887	0.0175	25.65	0.00
β	INTERCEPT	0.1539	0.0280	30.24	0.00
β	EVENTNUM	0.0086	0.0013	46.20	0.00
β	AGE1ST	0.0011	0.0005	4.13	0.04
β	CARAGE	-0.0043	0.0005	66.47	0.00
β	CONFLAST	-0.0264	0.0050	27.34	0.00
N = 10,920					
$\mathcal{L} = -28070.54$					
<i>Post-release</i>					
α	INTERCEPT	0.6637	0.0549	146.30	0.00
α	EVENTNUM	0.0314	0.0029	117.51	0.00
α	AGE1ST	-0.0021	0.0031	0.47	0.49
α	CARAGE	-0.0127	0.0010	147.93	0.00
α	CONFLAST	-0.0566	0.0305	3.45	0.06
β	INTERCEPT	-0.1845	0.0143	166.22	0.00
β	EVENTNUM	-0.0084	0.0007	129.02	0.00
β	AGE1ST	0.0006	0.0008	0.62	0.43
β	CARAGE	0.0035	0.0003	160.40	0.00
β	CONFLAST	0.0167	0.0085	3.84	0.05
N = 1,418					
$\mathcal{L} = -530.26$					

^a Modified sandwich variance estimates.

Table A.2: Pre-prison and post-release based hazard models of the criminal history accumulation process of prisoners released in 1994, CA

		$\hat{\alpha}_k, \hat{\beta}_k$	a.s.e. ^a	Wald χ^2	p-value
<i>Pre-prison</i>					
α	INTERCEPT	-0.5391	0.0400	181.93	0.00
α	EVENTNUM	-0.0213	0.0039	29.94	0.00
α	AGE1ST	-0.0089	0.0010	77.23	0.00
α	CARAGE	0.0157	0.0009	300.10	0.00
α	CONFLAST	0.0609	0.0180	11.43	0.00
β	INTERCEPT	0.1506	0.0129	136.98	0.00
β	EVENTNUM	0.0056	0.0011	25.66	0.00
β	AGE1ST	0.0018	0.0003	39.51	0.00
β	CARAGE	-0.0042	0.0003	246.15	0.00
β	CONFLAST	-0.0195	0.0054	13.10	0.00
N =	21,838				
\mathcal{G} =	-51560.73				
<i>Post-release</i>					
α	INTERCEPT	0.6557	0.0229	819.71	0.00
α	EVENTNUM	0.0224	0.0015	229.02	0.00
α	AGE1ST	0.0006	0.0010	0.28	0.60
α	CARAGE	-0.0121	0.0005	657.92	0.00
α	CONFLAST	-0.0450	0.0150	9.00	0.00
β	INTERCEPT	-0.1969	0.0063	964.15	0.00
β	EVENTNUM	-0.0059	0.0004	221.52	0.00
β	AGE1ST	0.0002	0.0003	0.67	0.41
β	CARAGE	0.0034	0.0001	758.60	0.00
β	CONFLAST	0.0142	0.0042	11.59	0.00
N =	6,902				
\mathcal{G} =	-2567.26				

^a Modified sandwich variance estimates.

Table A.3: Pre-prison and post-release based hazard models of the criminal history accumulation process of prisoners released in 1994, DE

		$\hat{\alpha}_k, \hat{\beta}_k$	a.s.e. ^a	Wald χ^2	p-value
<i>Pre-prison</i>					
α	INTERCEPT	-0.1589	0.0529	9.01	0.00
α	EVENTNUM	-0.0173	0.0038	21.17	0.00
α	AGE1ST	-0.0295	0.0017	294.87	0.00
α	CARAGE	0.0153	0.0011	188.23	0.00
α	CONFLAST	-0.0102	0.0246	0.17	0.68
β	INTERCEPT	0.0487	0.0168	8.45	0.00
β	EVENTNUM	0.0047	0.0011	17.43	0.00
β	AGE1ST	0.0075	0.0005	258.83	0.00
β	CARAGE	-0.0041	0.0004	131.98	0.00
β	CONFLAST	-0.0009	0.0073	0.02	0.90
N = 10,184					
$\mathcal{G} = -17726.91$					
<i>Post-release</i>					
α	INTERCEPT	0.2729	0.0712	14.69	0.00
α	EVENTNUM	0.0192	0.0031	37.35	0.00
α	AGE1ST	0.0213	0.0050	18.12	0.00
α	CARAGE	-0.0114	0.0015	55.88	0.00
α	CONFLAST	-0.0659	0.0399	2.73	0.10
β	INTERCEPT	-0.0852	0.0202	17.84	0.00
β	EVENTNUM	-0.0052	0.0009	34.08	0.00
β	AGE1ST	-0.0055	0.0014	15.75	0.00
β	CARAGE	0.0032	0.0004	58.57	0.00
β	CONFLAST	0.0213	0.0115	3.41	0.06
N = 659					
$\mathcal{G} = -202.36$					

^a Modified sandwich variance estimates.

Table A.4: Pre-prison and post-release based hazard models of the criminal history accumulation process of prisoners released in 1994, FL

		$\hat{\alpha}_k, \hat{\beta}_k$	a.s.e. ^a	Wald χ^2	p-value
<i>Pre-prison</i>					
α	INTERCEPT	-0.5787	0.0449	166.21	0.00
α	EVENTNUM	-0.0241	0.0019	162.09	0.00
α	AGE1ST	-0.0071	0.0012	32.49	0.00
α	CARAGE	0.0158	0.0008	350.92	0.00
α	CONFLAST	0.0794	0.0138	33.27	0.00
β	INTERCEPT	0.1595	0.0135	139.04	0.00
β	EVENTNUM	0.0065	0.0005	147.44	0.00
β	AGE1ST	0.0014	0.0003	16.40	0.00
β	CARAGE	-0.0042	0.0003	271.69	0.00
β	CONFLAST	-0.0244	0.0040	37.45	0.00
N =	25,729				
\mathcal{G} =	-57661.94				
<i>Post-release</i>					
α	INTERCEPT	0.8444	0.0342	608.89	0.00
α	EVENTNUM	0.0266	0.0020	178.96	0.00
α	AGE1ST	-0.0027	0.0019	1.95	0.16
α	CARAGE	-0.0142	0.0007	452.24	0.00
α	CONFLAST	-0.0571	0.0240	5.64	0.02
β	INTERCEPT	-0.2416	0.0092	695.52	0.00
β	EVENTNUM	-0.0071	0.0005	179.17	0.00
β	AGE1ST	0.0009	0.0005	3.61	0.06
β	CARAGE	0.0039	0.0002	506.59	0.00
β	CONFLAST	0.0189	0.0067	8.04	0.00
N =	2,554				
\mathcal{G} =	-874.94				

^a Modified sandwich variance estimates.

Table A.5: Pre-prison and post-release based hazard models of the criminal history accumulation process of prisoners released in 1994, IL

		$\hat{\alpha}_k, \hat{\beta}_k$	a.s.e. ^a	Wald χ^2	p-value
<i>Pre-prison</i>					
α	INTERCEPT	-0.6386	0.0580	121.19	0.00
α	EVENTNUM	-0.0271	0.0030	84.06	0.00
α	AGE1ST	-0.0081	0.0016	24.50	0.00
α	CARAGE	0.0182	0.0014	159.57	0.00
α	CONFLAST	0.0304	0.0257	1.40	0.24
β	INTERCEPT	0.1900	0.0182	108.60	0.00
β	EVENTNUM	0.0074	0.0009	74.23	0.00
β	AGE1ST	0.0014	0.0005	9.06	0.00
β	CARAGE	-0.0050	0.0004	125.82	0.00
β	CONFLAST	-0.0136	0.0076	3.21	0.07
N =	19,209				
\mathcal{G} =	-44910.71				
<i>Post-release</i>					
α	INTERCEPT	0.9450	0.0376	630.65	0.00
α	EVENTNUM	0.0274	0.0024	135.12	0.00
α	AGE1ST	-0.0068	0.0017	15.24	0.00
α	CARAGE	-0.0144	0.0008	363.05	0.00
α	CONFLAST	-0.0400	0.0212	3.56	0.06
β	INTERCEPT	-0.2824	0.0102	772.07	0.00
β	EVENTNUM	-0.0075	0.0006	141.08	0.00
β	AGE1ST	0.0022	0.0004	26.29	0.00
β	CARAGE	0.0042	0.0002	438.00	0.00
β	CONFLAST	0.0168	0.0060	7.79	0.01
N =	2,299				
\mathcal{G} =	-350.06				

^a Modified sandwich variance estimates.

Table A.6: Pre-prison and post-release based hazard models of the criminal history accumulation process of prisoners released in 1994, MD

		$\hat{\alpha}_k, \hat{\beta}_k$	a.s.e. ^a	Wald χ^2	p-value
<i>Pre-prison</i>					
α	INTERCEPT	-0.6929	0.0450	237.15	0.00
α	EVENTNUM	-0.0284	0.0065	19.03	0.00
α	AGE1ST	-0.0058	0.0014	16.61	0.00
α	CARAGE	0.0168	0.0013	176.70	0.00
α	CONFLAST	0.1054	0.0222	22.50	0.00
β	INTERCEPT	0.2008	0.0143	196.61	0.00
β	EVENTNUM	0.0076	0.0019	16.61	0.00
β	AGE1ST	0.0009	0.0004	4.93	0.03
β	CARAGE	-0.0045	0.0004	152.89	0.00
β	CONFLAST	-0.0317	0.0066	23.10	0.00
N = 12,509					
\mathcal{L} = -30394.20					
<i>Post-release</i>					
α	INTERCEPT	0.8522	0.0548	242.01	0.00
α	EVENTNUM	0.0283	0.0037	58.24	0.00
α	AGE1ST	-0.0038	0.0021	3.11	0.08
α	CARAGE	-0.0126	0.0010	155.61	0.00
α	CONFLAST	-0.0920	0.0327	7.91	0.00
β	INTERCEPT	-0.2561	0.0152	283.21	0.00
β	EVENTNUM	-0.0074	0.0010	51.86	0.00
β	AGE1ST	0.0015	0.0006	7.16	0.01
β	CARAGE	0.0036	0.0003	172.71	0.00
β	CONFLAST	0.0284	0.0092	9.52	0.00
N = 1,588					
\mathcal{L} = -513.13					

^a Modified sandwich variance estimates.

Table A.7: Pre-prison and post-release based hazard models of the criminal history accumulation process of prisoners released in 1994, MI

		$\hat{\alpha}_k, \hat{\beta}_k$	a.s.e. ^a	Wald χ^2	p-value
<i>Pre-prison</i>					
α	INTERCEPT	-0.6792	0.0430	249.49	0.00
α	EVENTNUM	-0.0695	0.0119	34.17	0.00
α	AGE1ST	-0.0066	0.0011	38.65	0.00
α	CARAGE	0.0233	0.0021	127.41	0.00
α	CONFLAST	0.0494	0.0304	2.64	0.10
β	INTERCEPT	0.1976	0.0152	169.68	0.00
β	EVENTNUM	0.0191	0.0033	32.57	0.00
β	AGE1ST	0.0010	0.0003	10.92	0.00
β	CARAGE	-0.0064	0.0006	117.07	0.00
β	CONFLAST	-0.0150	0.0090	2.79	0.09
N = 9,917					
\mathcal{G} = -31084.15					
<i>Post-release</i>					
α	INTERCEPT	0.7262	0.0610	141.51	0.00
α	EVENTNUM	0.0696	0.0059	140.38	0.00
α	AGE1ST	-0.0032	0.0030	1.16	0.28
α	CARAGE	-0.0197	0.0013	242.97	0.00
α	CONFLAST	0.0093	0.0364	0.07	0.80
β	INTERCEPT	-0.2251	0.0161	196.73	0.00
β	EVENTNUM	-0.0190	0.0015	155.72	0.00
β	AGE1ST	0.0013	0.0008	3.14	0.08
β	CARAGE	0.0056	0.0003	306.57	0.00
β	CONFLAST	-0.0017	0.0100	0.03	0.86
N = 1,939					
\mathcal{G} = -532.85					

^a Modified sandwich variance estimates.

Table A.8: Pre-prison and post-release based hazard models of the criminal history accumulation process of prisoners released in 1994, MN

		$\hat{\alpha}_k, \hat{\beta}_k$	a.s.e. ^a	Wald χ^2	p-value
<i>Pre-prison</i>					
α	INTERCEPT	-0.7845	0.0403	378.83	0.00
α	EVENTNUM	-0.0294	0.0048	37.09	0.00
α	AGE1ST	-0.0054	0.0009	39.72	0.00
α	CARAGE	0.0188	0.0011	303.19	0.00
α	CONFLAST	0.1193	0.0301	15.67	0.00
β	INTERCEPT	0.2375	0.0146	263.35	0.00
β	EVENTNUM	0.0081	0.0013	38.54	0.00
β	AGE1ST	0.0006	0.0002	5.28	0.02
β	CARAGE	-0.0053	0.0003	248.91	0.00
β	CONFLAST	-0.0369	0.0091	16.44	0.00
N = 12,196					
$\mathcal{L} = -30887.36$					
<i>Post-release</i>					
α	INTERCEPT	0.9734	0.0618	248.07	0.00
α	EVENTNUM	0.0332	0.0029	133.80	0.00
α	AGE1ST	0.0033	0.0032	1.08	0.30
α	CARAGE	-0.0170	0.0011	243.60	0.00
α	CONFLAST	-0.1675	0.0399	17.66	0.00
β	INTERCEPT	-0.3090	0.0171	327.02	0.00
β	EVENTNUM	-0.0090	0.0008	141.96	0.00
β	AGE1ST	-0.0002	0.0008	0.06	0.81
β	CARAGE	0.0051	0.0003	286.92	0.00
β	CONFLAST	0.0491	0.0116	18.09	0.00
N = 1,728					
$\mathcal{L} = -432.07$					

^a Modified sandwich variance estimates.

Table A.9: Pre-prison and post-release based hazard models of the criminal history accumulation process of prisoners released in 1994, NJ

		$\hat{\alpha}_k, \hat{\beta}_k$	a.s.e. ^a	Wald χ^2	p-value
<i>Pre-prison</i>					
α	INTERCEPT	-0.7725	0.0414	348.70	0.00
α	EVENTNUM	-0.0292	0.0046	40.02	0.00
α	AGE1ST	-0.0053	0.0013	17.44	0.00
α	CARAGE	0.0200	0.0011	331.66	0.00
α	CONFLAST	0.0255	0.0168	2.30	0.13
β	INTERCEPT	0.2322	0.0135	296.42	0.00
β	EVENTNUM	0.0082	0.0013	41.36	0.00
β	AGE1ST	0.0006	0.0003	2.70	0.10
β	CARAGE	-0.0056	0.0003	297.26	0.00
β	CONFLAST	-0.0092	0.0050	3.34	0.07
N =	17,136				
\mathcal{G} =	-40738.62				
<i>Post-release</i>					
α	INTERCEPT	1.0435	0.0588	314.95	0.00
α	EVENTNUM	0.0279	0.0035	61.71	0.00
α	AGE1ST	-0.0059	0.0042	2.03	0.15
α	CARAGE	-0.0171	0.0012	188.63	0.00
α	CONFLAST	-0.0305	0.0317	0.93	0.34
β	INTERCEPT	-0.3167	0.0158	402.06	0.00
β	EVENTNUM	-0.0079	0.0010	66.81	0.00
β	AGE1ST	0.0020	0.0011	3.06	0.08
β	CARAGE	0.0051	0.0003	220.52	0.00
β	CONFLAST	0.0110	0.0090	1.51	0.22
N =	2,128				
\mathcal{G} =	-663.95				

^a Modified sandwich variance estimates.

Table A.10: Pre-prison and post-release based hazard models of the criminal history accumulation process of prisoners released in 1994, NY

		$\hat{\alpha}_k, \hat{\beta}_k$	a.s.e. ^a	Wald χ^2	p-value
<i>Pre-prison</i>					
α	INTERCEPT	-0.5716	0.0433	174.10	0.00
α	EVENTNUM	-0.0039	0.0049	0.62	0.43
α	AGE1ST	-0.0100	0.0013	56.71	0.00
α	CARAGE	0.0115	0.0011	108.35	0.00
α	CONFLAST	0.0881	0.0139	39.98	0.00
β	INTERCEPT	0.1695	0.0132	165.27	0.00
β	EVENTNUM	0.0008	0.0014	0.34	0.56
β	AGE1ST	0.0020	0.0004	28.65	0.00
β	CARAGE	-0.0031	0.0003	88.81	0.00
β	CONFLAST	-0.0281	0.0042	45.54	0.00
N =	22,616				
\mathcal{G} =	-51160.63				
<i>Post-release</i>					
α	INTERCEPT	0.6992	0.0462	229.25	0.00
α	EVENTNUM	0.0081	0.0027	9.15	0.00
α	AGE1ST	0.0000	0.0025	0.00	1.00
α	CARAGE	-0.0079	0.0009	72.76	0.00
α	CONFLAST	-0.0833	0.0263	10.01	0.00
β	INTERCEPT	-0.2179	0.0126	300.00	0.00
β	EVENTNUM	-0.0020	0.0007	7.94	0.00
β	AGE1ST	0.0003	0.0007	0.22	0.64
β	CARAGE	0.0024	0.0002	91.09	0.00
β	CONFLAST	0.0271	0.0074	13.48	0.00
N =	2,390				
\mathcal{G} =	-1092.47				

^a Modified sandwich variance estimates.

Table A.11: Pre-prison and post-release based hazard models of the criminal history accumulation process of prisoners released in 1994, NC

		$\hat{\alpha}_k, \hat{\beta}_k$	a.s.e. ^a	Wald χ^2	p-value
<i>Pre-prison</i>					
α	INTERCEPT	-0.7516	0.0336	500.44	0.00
α	EVENTNUM	-0.0342	0.0058	35.06	0.00
α	AGE1ST	-0.0046	0.0009	28.85	0.00
α	CARAGE	0.0189	0.0013	214.09	0.00
α	CONFLAST	0.1141	0.0272	17.63	0.00
β	INTERCEPT	0.2157	0.0110	385.49	0.00
β	EVENTNUM	0.0092	0.0017	30.60	0.00
β	AGE1ST	0.0006	0.0002	5.25	0.02
β	CARAGE	-0.0051	0.0004	183.57	0.00
β	CONFLAST	-0.0339	0.0081	17.54	0.00
N =	12,424				
\mathcal{G} =	-34005.58				
<i>Post-release</i>					
α	INTERCEPT	0.8694	0.0495	308.61	0.00
α	EVENTNUM	0.0397	0.0040	97.16	0.00
α	AGE1ST	-0.0021	0.0021	0.99	0.32
α	CARAGE	-0.0158	0.0010	247.27	0.00
α	CONFLAST	-0.1484	0.0362	16.79	0.00
β	INTERCEPT	-0.2643	0.0139	362.28	0.00
β	EVENTNUM	-0.0106	0.0011	94.85	0.00
β	AGE1ST	0.0011	0.0005	4.07	0.04
β	CARAGE	0.0045	0.0003	288.54	0.00
β	CONFLAST	0.0429	0.0104	17.06	0.00
N =	2,047				
\mathcal{G} =	-668.35				

^a Modified sandwich variance estimates.

Table A.12: Pre-prison and post-release based hazard models of the criminal history accumulation process of prisoners released in 1994, OH

		$\hat{\alpha}_k, \hat{\beta}_k$	a.s.e. ^a	Wald χ^2	p-value
<i>Pre-prison</i>					
α	INTERCEPT	-0.8861	0.0400	489.73	0.00
α	EVENTNUM	-0.0547	0.0195	7.86	0.01
α	AGE1ST	-0.0044	0.0011	15.94	0.00
α	CARAGE	0.0244	0.0031	60.51	0.00
α	CONFLAST	0.1197	0.0626	3.65	0.06
β	INTERCEPT	0.2684	0.0142	357.95	0.00
β	EVENTNUM	0.0152	0.0058	6.93	0.01
β	AGE1ST	0.0002	0.0003	0.26	0.61
β	CARAGE	-0.0069	0.0010	52.12	0.00
β	CONFLAST	-0.0375	0.0191	3.86	0.05
N = 4,424					
$\mathcal{G} = -14312.27$					
<i>Post-release</i>					
α	INTERCEPT	0.9520	0.0857	123.37	0.00
α	EVENTNUM	0.0421	0.0121	12.07	0.00
α	AGE1ST	-0.0114	0.0038	8.96	0.00
α	CARAGE	-0.0158	0.0026	37.92	0.00
α	CONFLAST	-0.1725	0.0590	8.56	0.00
β	INTERCEPT	-0.3029	0.0231	172.51	0.00
β	EVENTNUM	-0.0115	0.0033	12.23	0.00
β	AGE1ST	0.0037	0.0010	14.62	0.00
β	CARAGE	0.0048	0.0007	47.51	0.00
β	CONFLAST	0.0540	0.0165	10.77	0.00
N = 1,100					
$\mathcal{G} = -308.96$					

^a Modified sandwich variance estimates.

Table A.13: Pre-prison and post-release based hazard models of the criminal history accumulation process of prisoners released in 1994, OR

		$\hat{\alpha}_k, \hat{\beta}_k$	a.s.e. ^a	Wald χ^2	p-value
<i>Pre-prison</i>					
α	INTERCEPT	-0.5697	0.0347	269.13	0.00
α	EVENTNUM	-0.0213	0.0021	101.28	0.00
α	AGE1ST	-0.0058	0.0011	29.08	0.00
α	CARAGE	0.0148	0.0007	512.47	0.00
α	CONFLAST	0.0636	0.0124	26.18	0.00
β	INTERCEPT	0.1551	0.0105	216.31	0.00
β	EVENTNUM	0.0057	0.0006	89.22	0.00
β	AGE1ST	0.0011	0.0003	13.83	0.00
β	CARAGE	-0.0039	0.0002	399.21	0.00
β	CONFLAST	-0.0198	0.0036	30.10	0.00
N =	19,780				
\mathcal{G} =	-39480.23				
<i>Post-release</i>					
α	INTERCEPT	0.8257	0.0611	182.40	0.00
α	EVENTNUM	0.0189	0.0026	53.87	0.00
α	AGE1ST	-0.0065	0.0025	6.59	0.01
α	CARAGE	-0.0109	0.0011	102.74	0.00
α	CONFLAST	-0.0628	0.0327	3.69	0.05
β	INTERCEPT	-0.2371	0.0165	206.53	0.00
β	EVENTNUM	-0.0049	0.0007	52.40	0.00
β	AGE1ST	0.0019	0.0006	8.85	0.00
β	CARAGE	0.0031	0.0003	119.46	0.00
β	CONFLAST	0.0168	0.0090	3.51	0.06
N =	1,465				
\mathcal{G} =	-490.40				

^a Modified sandwich variance estimates.

Table A.14: Pre-prison and post-release based hazard models of the criminal history accumulation process of prisoners released in 1994, TX

		$\hat{\alpha}_k, \hat{\beta}_k$	a.s.e. ^a	Wald χ^2	p-value
<i>Pre-prison</i>					
α	INTERCEPT	-0.5391	0.0398	183.53	0.00
α	EVENTNUM	-0.0268	0.0037	51.90	0.00
α	AGE1ST	-0.0108	0.0012	78.97	0.00
α	CARAGE	0.0158	0.0007	444.85	0.00
α	CONFLAST	0.0318	0.0163	3.78	0.05
β	INTERCEPT	0.1518	0.0126	144.85	0.00
β	EVENTNUM	0.0070	0.0010	47.83	0.00
β	AGE1ST	0.0023	0.0003	45.07	0.00
β	CARAGE	-0.0042	0.0002	386.21	0.00
β	CONFLAST	-0.0121	0.0048	6.45	0.01
N = 15,541					
\mathcal{G} = -44701.01					
<i>Post-release</i>					
α	INTERCEPT	0.5734	0.0569	101.43	0.00
α	EVENTNUM	0.0303	0.0045	46.39	0.00
α	AGE1ST	0.0048	0.0032	2.23	0.14
α	CARAGE	-0.0125	0.0012	112.92	0.00
α	CONFLAST	-0.0512	0.0332	2.37	0.12
β	INTERCEPT	-0.1748	0.0155	126.59	0.00
β	EVENTNUM	-0.0079	0.0012	45.72	0.00
β	AGE1ST	-0.0009	0.0008	1.21	0.27
β	CARAGE	0.0035	0.0003	125.22	0.00
β	CONFLAST	0.0167	0.0092	3.31	0.07
N = 2,410					
\mathcal{G} = -816.69					

^a Modified sandwich variance estimates.

Table A.15: Pre-prison and post-release based hazard models of the criminal history accumulation process of prisoners released in 1994, VA

		$\hat{\alpha}_k, \hat{\beta}_k$	a.s.e. ^a	Wald χ^2	p-value
<i>Pre-prison</i>					
α	INTERCEPT	-0.7281	0.0401	330.47	0.00
α	EVENTNUM	-0.0338	0.0021	264.31	0.00
α	AGE1ST	-0.0050	0.0011	19.64	0.00
α	CARAGE	0.0185	0.0007	646.05	0.00
α	CONFLAST	0.0981	0.0368	7.10	0.01
β	INTERCEPT	0.2110	0.0129	267.11	0.00
β	EVENTNUM	0.0092	0.0006	245.67	0.00
β	AGE1ST	0.0007	0.0003	4.25	0.04
β	CARAGE	-0.0051	0.0002	518.59	0.00
β	CONFLAST	-0.0314	0.0109	8.23	0.00
N = 14,649					
\mathcal{G} = -37187.62					
<i>Post-release</i>					
α	INTERCEPT	0.8845	0.0419	445.29	0.00
α	EVENTNUM	0.0302	0.0023	169.56	0.00
α	AGE1ST	-0.0064	0.0021	9.31	0.00
α	CARAGE	-0.0145	0.0009	237.44	0.00
α	CONFLAST	-0.2298	0.1125	4.17	0.04
β	INTERCEPT	-0.2617	0.0113	540.32	0.00
β	EVENTNUM	-0.0081	0.0006	179.83	0.00
β	AGE1ST	0.0022	0.0005	16.00	0.00
β	CARAGE	0.0041	0.0003	268.92	0.00
β	CONFLAST	0.0664	0.0312	4.53	0.03
N = 2,001					
\mathcal{G} = -807.70					

^a Modified sandwich variance estimates.

Table A.16: Logistic regression parameter estimates of the effects of attributes on the Log-odds of a releasee experiencing a deterrent effect, Group I states

	$\hat{\lambda}_k$	a.s.e. ^a	Wald χ^2	p-value
INTERCEPT	-1.9082	0.1657	132.56	0.00
CHIST	-0.1050	0.0069	230.84	0.00
CARAGE	0.0173	0.0023	58.12	0.00
AGE1ST	-0.1513	0.0053	831.27	0.00
RELAGE	0.1432	0.0048	877.30	0.00
BLACK	0.0890	0.0476	3.50	0.06
MALE	-0.1831	0.0911	4.04	0.04
VIOLENT	-0.1016	0.0769	1.74	0.19
PROPERTY	-0.0929	0.0810	1.32	0.25
DRUG	0.0345	0.0827	0.17	0.68
PAROLE ^b	-0.0397	0.0760	0.27	0.60
MANDATORY ^b	-0.0905	0.0758	1.43	0.23

^a Traditional variance estimates.

^b Reference category: UNCONDITIONAL.

Table A.17: Logistic regression parameter estimates of the effects of attributes on the Log-odds of a releasee experiencing a deterrent effect, Group II states

	$\hat{\lambda}_k$	a.s.e. ^a	Wald χ^2	p-value
INTERCEPT	1.4638	0.3143	21.69	0.00
CHIST	-0.1562	0.0115	183.27	0.00
CARAGE	0.0264	0.0046	32.39	0.00
AGE1ST	-0.2117	0.0118	319.42	0.00
RELAGE	0.0996	0.0083	145.22	0.00
BLACK	-0.1077	0.0987	1.19	0.27
MALE	-0.3871	0.1603	5.83	0.02
VIOLENT	-0.3189	0.1811	3.10	0.08
PROPERTY	-0.5510	0.1849	8.88	0.00
DRUG	-0.4539	0.1985	5.23	0.02
PAROLE ^b	0.1854	0.0922	4.04	0.04

^a Traditional variance estimates.

^b Reference category: MANDATORY.

Table A.18: Logistic regression parameter estimates of the effects of attributes on the Log-odds of a releasee experiencing a deterrent effect, Group III states

	$\hat{\lambda}_k$	a.s.e. ^a	Wald χ^2	p-value
INTERCEPT	-1.0208	0.1751	33.99	0.00
CHIST	-0.0732	0.0067	120.80	0.00
CARAGE	0.0114	0.0025	21.00	0.00
AGE1ST	-0.1272	0.0057	495.62	0.00
RELAGE	0.1092	0.0050	479.90	0.00
BLACK	-0.0222	0.0568	0.15	0.70
MALE	-0.0525	0.0994	0.28	0.60
VIOLENT	-0.1891	0.0892	4.49	0.03
PROPERTY	-0.1781	0.0950	3.52	0.06
DRUG	-0.0909	0.0964	0.89	0.35
CONDITIONAL ^b	-0.0786	0.0582	1.82	0.18

^a Traditional variance estimates.

^b Reference category: UNCONDITIONAL.

Table A.19: Logistic regression parameter estimates of the effects of attributes on the Log-odds of a releasee experiencing a deterrent effect, Group IV states

	$\hat{\lambda}_k$	a.s.e. ^a	Wald χ^2	p-value
INTERCEPT	-1.1504	0.1436	64.14	0.00
CHIST	-0.0945	0.0052	336.36	0.00
CARAGE	0.0139	0.0019	52.34	0.00
AGE1ST	-0.1530	0.0047	1078.50	0.00
RELAGE	0.1194	0.0043	770.91	0.00
BLACK	-0.1151	0.0464	6.15	0.01
MALE	-0.1604	0.0949	2.86	0.09
VIOLENT	-0.1829	0.0758	5.83	0.02
PROPERTY	-0.1757	0.0849	4.28	0.04
DRUG	-0.0192	0.0839	0.05	0.82

^a Traditional variance estimates.
Insufficient variation in the release mechanism variable

Table A.20: OLS parameter estimates of the effects of attributes on δ , Group I states

	$\hat{\lambda}_k$	a.s.e. ^a	Wald χ^2	p-value
INTERCEPT	-6.5221	0.1025	4046.98	0.00
CHIST	-0.0480	0.0034	193.81	0.00
CARAGE	0.0731	0.0013	3317.68	0.00
AGE1ST	0.1258	0.0028	2071.23	0.00
RELAGE	-0.0491	0.0025	376.50	0.00
BLACK	-0.0007	0.0283	0.00	0.98
MALE	0.3169	0.0547	33.60	0.00
VIOLENT	0.0209	0.0459	0.21	0.65
PROPERTY	-0.0366	0.0483	0.57	0.45
DRUG	-0.0733	0.0494	2.21	0.14
PAROLE ^b	0.0062	0.0452	0.02	0.89
MANDATORY ^b	-0.1549	0.0452	11.76	0.00

^a Traditional variance estimates.

^b Reference category: UNCONDITIONAL.

Table A.21: OLS parameter estimates of the effects of attributes on δ , Group II states

	$\hat{\lambda}_k$	a.s.e. ^a	Wald χ^2	p-value
INTERCEPT	-8.4852	0.1901	1991.46	0.00
CHIST	-0.0584	0.0054	116.91	0.00
CARAGE	0.0758	0.0025	926.26	0.00
AGE1ST	0.1632	0.0052	981.19	0.00
RELAGE	-0.0287	0.0046	39.82	0.00
BLACK	0.0544	0.0614	0.79	0.38
MALE	0.4451	0.1000	19.82	0.00
VIOLENT	0.1580	0.1153	1.88	0.17
PROPERTY	0.1706	0.1175	2.11	0.15
DRUG	-0.0351	0.1259	0.08	0.78
PAROLE ^b	-0.1078	0.0573	3.55	0.06

^a Traditional variance estimates.

^b Reference category: MANDATORY.

Table A.22: OLS parameter estimates of the effects of attributes on δ , Group III states

	$\hat{\lambda}_k$	a.s.e. ^a	Wald χ^2	p-value
INTERCEPT	-8.3727	0.1589	2775.54	0.00
CHIST	-0.1042	0.0050	429.15	0.00
CARAGE	0.0857	0.0021	1739.17	0.00
AGE1ST	0.1860	0.0044	1806.11	0.00
RELAGE	-0.0427	0.0038	125.02	0.00
BLACK	0.0309	0.0493	0.39	0.53
MALE	0.3480	0.0858	16.43	0.00
VIOLENT	0.1484	0.0774	3.68	0.06
PROPERTY	0.0913	0.0827	1.22	0.27
DRUG	-0.0061	0.0841	0.01	0.94
CONDITIONAL	-0.0366	0.0506	0.52	0.47

^a Traditional variance estimates.

^b Reference category: MANDATORY.

Table A.23: OLS parameter estimates of the effects of attributes on δ , Group IV states

	$\hat{\lambda}_k$	a.s.e. ^a	Wald χ^2	p-value
INTERCEPT	-6.7748	0.1058	4100.17	0.00
CHIST	-0.0671	0.0031	454.57	0.00
CARAGE	0.0792	0.0013	3593.19	0.00
AGE1ST	0.1431	0.0028	2548.12	0.00
RELAGE	-0.0365	0.0027	187.66	0.00
BLACK	-0.0067	0.0332	0.04	0.84
MALE	0.3660	0.0680	28.95	0.00
VIOLENT	0.0893	0.0550	2.64	0.10
PROPERTY	-0.0544	0.0612	0.79	0.37
DRUG	-0.0754	0.0608	1.54	0.21

^a Traditional variance estimates.

^b Reference category: MANDATORY.

Appendix B

Sample SAS Code

In this Appendix, I provide the SAS code I used to estimate the models presented in this report. This code is provided as reference material only as it is *not* generic. Researchers interested in using this code will need to scan through it and redefine variable names appropriately although some of the basic elements—like the list of independent variables for the first and second moment, the dependent variable, etc.—are passed to a macro as arguments. This code will also be archived at ICPSR shortly.

To estimate the pre-release and post-release models for the state of Arizona, for example, the following lines of code was run in SAS.

```
%LET ROOT=D:\AVI\NIJ_DRP04\ANALYSIS;
%INCLUDE "&ROOT.\PGMS\PPRMOD.MAC";
/* THESE VARIABLES ARE TO BE USED IN MODELING THE PRE-RELEASE
   ARREST HISTORY ACCUMULATION PROCESS */
%LET PREX1=INTERCEPT EVENTNUM AGE1ST CARAGE CONFINEDLAST;
%LET PREX2=INTERCEPT EVENTNUM AGE1ST CARAGE CONFINEDLAST;
/* THESE VARIABLES ARE TO BE USED IN MODELING THE POST-RELEASE
   RECIDIVISM MODELS */
%LET POSTX1_0=INTERCEPT EVENTNUM AGE1ST CARAGE CONFINEDLAST;
%LET POSTX2_0=INTERCEPT EVENTNUM AGE1ST CARAGE CONFINEDLAST;
/* CALL THE MACRO FOR EACH STATE SEPARATELY */
%PPRMOD(3, 3, &ROOT, DRP, &PREX1, &PREX2, &POSTX1_2, &POSTX2_2);
ENDSAS;
```

Here, PPRMOD is the name of a SAS Macro written for this analysis. It is printed verbatim on the next few pages. I do not offer any performance guarantees for the code below.

```
%MACRO PPRMOD(ST,ST2,BASEL,DSET,XXM,XXV,XXMF,XXVF);
```

```
\*****  
USAGE EXAMPLE:
```

```
%PPRMOD(ST,ST2,BASEL,DSET,XXM,XXV,XXMF,XXVF);
```

WHERE:

ST = State identifying code in data (for labeling purposes only)
ST2 = Second state identifying code (this is used for subsetting the data)
BASEL = Root directly under which data is to be found and where the output and log files are to be stored.
DSET = Name of data set to be used.
XXM = A list of X variables to be used for modeling the 1st moment of arrest age.
XXV = A list of X variables to be used for modeling the 2nd moment of arrest age.
XXMF = A list of variables (corresponding to XXM) to be used for predicting the first moment of the trajectory as well as for estimating the deflection.
XXVF = A list of variables (corresponding to XXV) to be used for predicting the first moment of the trajectory as well as for estimating the deflection.

ADDITIONAL DATA NEEDED:

In addition to the above variables, the data set must contain the following list of variables:

CASENUM = A unique individual ID number (person specific)
STATE = State of release
BEFOREREL = 1 if event is before prison admission, 0 otherwise
FIRSTPOST = 1 if this is the 1st post release event, 0 otherwise (note this should include censored spells)
ARRESTAGE = age at each subsequent arrest in the sample
AGELAST = Age at previous arrest (agelast = 0 for 1st arrest)
EVENTNUM = Arrest number (e.g., 1,2,3,...)
CENSOR = 1 if spell is censored, 0 if completed.
RELAGE = Age of release from current incarceration episode
RELAGEPQ01 = Release age + 1 quarter
RELAGEPQ02 = Release age + 2 quarters
RELAGEPQ03 = Release age + 3 quarters
...
RELAGEPQ12 = Release age + 12 quarters

```
*****/
```

```
LIBNAME SAF "&BASEL.\DATA";
```

```
FILENAME OUTFILE "&BASEL.\PGMS\OUTPUT\STATE&ST..LST";
```

```
FILENAME LGFILE "&BASEL.\PGMS\OUTPUT\STATE&ST..LOG";
```

```

PROC PRINTTO PRINT=OUTFILE LOG=LGFILE NEW;
RUN;

TITLE "OUTPUT FOR STATE=&ST.";

DATA PREREL&ST.; SET SAF.&DSET;
IF STATE=&ST2. AND BEFOREREL=1;
RUN;

%LET Y=ARRESTAGE;
%LET C=CENSOR;
%LET POSS=AGELAST;
%LET REL=RELAGEPQ01 RELAGEPQ02 RELAGEPQ03 RELAGEPQ04
        RELAGEPQ05 RELAGEPQ06 RELAGEPQ07 RELAGEPQ08
        RELAGEPQ09 RELAGEPQ10 RELAGEPQ11 RELAGEPQ12;
PROC CHART DATA=PREREL&ST.;
VBAR &Y.;
RUN;

DATA PSTREL&ST.(KEEP=STATE CASENUM &Y &C &XXM &XXV &XXMF &XXVF
                &REL RELAGE EVENTNUM AGELAST);

SET SAF.&DSET;
IF STATE=&ST. AND FIRSTPOST=1;
RUN;

PROC IML;
RESET NONAME;
USE PREREL&ST.;
READ ALL VAR{&Y} INTO YY;
READ ALL VAR{&C} INTO CENSOR;
READ ALL VAR{&XXM} INTO X1;
READ ALL VAR{&XXV} INTO X2;
READ ALL VAR{&POSS} INTO POSS;
READ ALL VAR{CASENUM} INTO CASENUM;
CLOSE PREREL&ST.;
Y=YY#(1-CENSOR);
N=NROW(Y);
K1=NCOL(X1);
K2=NCOL(X2);
Z=((0:400)/4)';
M=NROW(Z);

MONES = J(M,1,1);
NONES = J(N,1,1);

ARN_ = ROUND(YY*4)/4;
ARM1N_ = ROUND(POSS*4)/4;
S0 = EXP(J(N,M,0));

W = (ARM1N_*MONES' <= NONES*Z')#(NONES*Z' <= ARN_*MONES');
CASEN = UNIQUE(CASENUM)';

```

```

NIND = NROW(CASEN);

/* THIS IS THE DUAL OBJECTIVE FUNCTION */
start sercsod(bb) global(x1,x2,y,lyf,z,lzf,k1,k2,m,n,W,S,S0);
  b_ = bb[1:k1]; g_=bb[k1+1:k1+k2];
  mones = J(m,1,1);
  nones = J(n,1,1);
  S = S0#EXP(X1*B_*Z'+X1*G_*LZF'-1);
  llf = Y'*X1*B_ + LYF'*X2*G_ - nones'*(W#S)*mones;
  return(llf);
finish sercsod;

/* THIS IS THE ANALYTICAL GRADIENT OF THE DUAL OBJECTIVE FUNCTION */
start g_sercsod(bb) global(x1,x2,y,lyf,z,lzf,k1,k2,m,n,W,S,S0);
  mones = J(m,1,1);
  nones = J(n,1,1);
  GR1 = X1'*(Y-(W#S)*Z);
  GR2 = X2'*(LYF-(W#S)*LZF);
  gr = ( gr1 // gr2 )';
  return(gr);
finish g_sercsod;

/* THIS IS THE ANALYTICAL HESSIAN OF THE DUAL OBJECTIVE FUNCTION */
start h_sercsod(bb) global(x1,x2,y,lyf,z,lzf,k1,k2,m,n,W,S,S0);
  mones = J(m,1,1);
  nones = J(n,1,1);
  SW = (W#S);
  H1 = X1'*(((Z'#SW)*Z)#X1) || X1'*(((Z'#SW)*LZF)#X2) ;
  H2 = X2'*(((LZF'#SW)*Z)#X1) || X2'*(((LZF'#SW)*LZF)#X2) ;
  HS = - ( H1 // H2 ) ;
  return(hs);
finish h_sercsod;

LYF = y#log(y+(y=0));
LZF = z#log(z+(z=0));

/* DEFINING SOME STARTING VALUES AND OPTIONS */
optn = {1 1};
TCR = {10000 10000};
xstart = J(k1,1,0) // J(k2,1,0) ;

/* CALLING THE NEWTON-RHAPHSON NON-LINEAR OPTIMIZATION ROUTINE IN SAS IML */
CALL NLPNRA(rc,xres_,"sercsod",xstart,optn,,tcr,,,"g_sercsod","h_sercsod");

hh = H_SERCSOD(XRES_);
ff = sercsod(XRES_);

gop1_ = X1#(Y-(W#S)*Z) || X2#(LYF-(W#S)*LZF) ;
gop1 = gop1_'*gop1_;

gop2_ = J(NIND,NCOL(GOP1),0);

```

```

DO NN=1 TO NIND BY 1;
gop2_[NN,]=gop1_[loc(CASENUM=CASEN[NN]),][+,];
END;
gop2 = gop2_ *gop2_;

cov = inv(-hh);
ase = sqrt(vecdiag(cov));
bhat = xres_';
BHAT_NULL = Xstart;
wald = ((bhat-BHAT_NULL)/ase)##2;
pval = 1-probchi(wald,1);
VNM = {&XXM}||{&XXV};

cov_ = inv(-hh)*gop1*inv(-hh);
ase_ = sqrt(vecdiag(cov_));
wald_ = ((bhat-BHAT_NULL)/ase_)##2;
pval_ = 1-probchi(wald_,1);

cov__ = inv(-hh)*gop2*inv(-hh);
ase__ = sqrt(vecdiag(cov__));
wald__ = ((bhat-BHAT_NULL)/ase__)##2;
pval__ = 1-probchi(wald__,1);

PRINT "MODEL RESULTS";
print bhat[format=9.4 rowname=vnm colname="LAMBDA"]
ase[format=9.4 colname="ASE"]
wald[format=6.2 colname="WALD"]
pval[format=6.2 colname="PVAL" ] ;

PRINT "MODEL RESULTS: SANDWICH ESTIMATOR";
print bhat[format=9.4 rowname=vnm colname="LAMBDA"]
ase_[format=9.4 colname="ASE"]
wald_[format=6.2 colname="WALD"]
pval_[format=6.2 colname="PVAL" ] ;

PRINT "MODEL RESULTS: MODIFIED SANDWICH ESTIMATOR";
print bhat[format=9.4 rowname=vnm colname="LAMBDA"]
ase__[format=9.4 colname="ASE"]
wald__[format=6.2 colname="WALD"]
pval__[format=6.2 colname="PVAL" ] ;

PW2 = (ARM1N_*MONES' <= NONES*Z');
PWS2 = PW2#S;
PSC2 = J(N,M,0);

DO PIND2 = 1 TO N BY 1;
PSC2[PIND2,]=CUSUM(PWS2[PIND2,]);
END;

PC2 = 1-EXP(-PSC2);
PP2 = J(N,M,0);

```

```

PP2[,1] = PC2[,1];
DO PFF2 = 2 TO M BY 1;
PP2[,PFF2] = PC2[,PFF2]-PC2[,PFF2-1];
END;

YHAT = (PP2)*Z;
e1 = y-YHAT;
e2 = y-y[:];
sse_m = e1'*e1;
sse_t = e2'*e2;
rsq = 100*(1-(sse_m/sse_t));
print ff rsq;

/* COMPUTING THE PREDICTED PROBABILITIES FOR A SET OF CHARACTERISTICS */

USE PSTREL&ST.;
READ ALL VAR{STATE CASENUM} INTO STATECASE;
READ ALL VAR{&Y} INTO YY;
READ ALL VAR{&C} INTO CENSOR;
READ ALL VAR{&XXM} INTO X1;
READ ALL VAR{&XXV} INTO X2;
READ ALL VAR{&XXMF} INTO X1F;
READ ALL VAR{&XXVF} INTO X2F;
READ ALL VAR{&REL} INTO RELMAT;
READ ALL VAR{RELAGE} INTO POSS;
READ ALL VAR{EVENTNUM} INTO EVN;
READ ALL VAR{CASENUM} INTO CASENUM;
CLOSE PSTREL&ST.;
Y = YY*(1-CENSOR);
RELAGEMAT = FLOOR(RELMAT*4)/4;
N2 = NROW(X1);
FOL = NCOL(RELAGEMAT);

POS = FLOOR(POSS*4)/4;
W = (J(N2,1,1)*Z' >= POS*MONES');
S0 = EXP(J(N2,M,0));

b_ = BHAT[1:k1]; g_=BHAT[k1+1:k1+k2];
X1BC = X1*B_;
X2BC = X2*G_;

S = S0#EXP(X1*B_*Z'+X2*G_*LZF'-1);
WS = W#S;
SC = J(N2,M,0);

DO IND = 1 TO N2 BY 1;
SC[IND,]=CUSUM(WS[IND,]);
END;

C = 1-EXP(-SC);

```



```

CDF = J(N2,FOL,0);

DO FF = 1 TO FOL BY 1;
CDF[,FF] = C#(J(N2,1,1)*Z'=RELAGEMAT[,FF]*MONES')*MONES;
END;

/* REDEFINING SOME VARIABLE FOR THE RECIDIVISM MODEL */
ARN2_ = ROUND(YY*4)/4;
ARM1N2_ = ROUND(POSS*4)/4;
S0 = S;
N = N2;
NONES = J(N,1,1);

W = (ARM1N2_*MONES' <= NONES*Z')#(NONES*Z' <= ARN2_*MONES');
LYF = y#log(y+(y=0));
LZF = z#log(z+(z=0));
FREE S;

X1=X1F;
X2=X2F;

K1=NCOL(X1);
K2=NCOL(X2);

CASEN = UNIQUE(CASENUM)';
NIND = NROW(CASEN);

xstart = J(k1,1,0) // J(k2,1,0) ;

CALL NLPNRA(rc,xres_,"sercsod",xstart,optn,,tcr,,,"g_sercsod","h_sercsod");
* computing standard errors and test statistics for the parameters ;

hh = H_SERCSOD(XRES_);
ff = sercsod(XRES_);

gop1_ = X1#(Y-(W#S)*Z) || X2#(LYF-(W#S)*LZF) ;
gop1 = gop1_'*gop1_;

gop2_ = J(NIND,NCOL(GOP1),0);
DO NN=1 TO NIND BY 1;
gop2_[NN,]=gop1_[loc(CASENUM=CASEN[NN]),][+,];
END;
gop2 = gop2_'*gop2_;

cov = inv(-hh);
ase = sqrt(vecdiag(cov));
bhat = xres_';
BHAT_NULL = Xstart;
wald = ((bhat-BHAT_NULL)/ase)##2;
pval = 1-probchi(wald,1);
VNM = {&XXMF} || {&XXVF};

```

```

cov_ = inv(-hh)*gop1*inv(-hh);
ase_ = sqrt(vecdiag(cov_));
wald_ = ((bhat-BHAT_NULL)/ase_)##2;
pval_ = 1-probchi(wald_,1);

cov__ = inv(-hh)*gop2*inv(-hh);
ase__ = sqrt(vecdiag(cov__));
wald__ = ((bhat-BHAT_NULL)/ase__)##2;
pval__ = 1-probchi(wald__,1);

PRINT "COUNTERFACTUAL MODEL RESULTS";
print bhat[format=9.4 rowname=vnm colname="LAMBDA"]
ase[format=9.4 colname="ASE"]
wald[format=6.2 colname="WALD"]
pval[format=6.2 colname="PVAL"] ;

PRINT "COUNTERFACTUAL MODEL RESULTS: SANDWICH ESTIMATOR";
print bhat[format=9.4 rowname=vnm colname="LAMBDA"]
ase_[format=9.4 colname="ASE"]
wald_[format=6.2 colname="WALD"]
pval_[format=6.2 colname="PVAL"] ;

PRINT "COUNTERFACTUAL MODEL RESULTS: MODIFIED SANDWICH ESTIMATOR";
print bhat[format=9.4 rowname=vnm colname="LAMBDA"]
ase__[format=9.4 colname="ASE"]
wald__[format=6.2 colname="WALD"]
pval__[format=6.2 colname="PVAL"] ;

W = (J(N,1,1)*Z' >= POS*MONES');
WS2 = W#S;
SC2 = J(N,M,0);

DO IND = 1 TO N BY 1;
SC2[IND,]=CUSUM(WS2[IND,]);
END;

C2 = 1-EXP(-SC2);

CDF2 = J(N,FOL,0);
DO FF = 1 TO FOL BY 1;
CDF2[,FF] = C2#(J(N,1,1)*Z'=RELAGEMAT[,FF]*MONES')*MONES;
END;

b_ = XRES_[1:k1]; g_=XRES_[k1+1:k1+k2];
X1B = X1*B_;
X2B = X2*G_;

W_ = (J(N,1,1)*Z' >= POS*MONES')#(J(N,1,1)*Z' <= RELAGEMAT[,FOL]*MONES');
WS2_ = W_#S;
WSS_ = WS2_*MONES;

```

```

DELTA = ((WS2_/(WSS_*MONES'))#LOG(S/S0))*MONES;
DELTASTD = SQRT( ((WS2_/(WSS_*MONES'))#(LOG(S/S0)##2))*MONES
- (((WS2_/(WSS_*MONES'))#LOG(S/S0))*MONES)##2 );

MATOUT = STATECASE || POSS || YY || CENSOR || EVN || DELTA || DELTASTD ||
X1B || X2B || X1BC || X2BC || RELAGEMAT || CDF || CDF2 ;
CREATE OUTD&ST. FROM MATOUT[COLNAME={STATE CASENUM RELAGE ARRESTAGE CENSOR
EVENTNUM DELTA DELTASTD X1B X2B X1BC X2BC
RELAGEPQ01 RELAGEPQ02 RELAGEPQ03 RELAGEPQ04
RELAGEPQ05 RELAGEPQ06 RELAGEPQ07 RELAGEPQ08
RELAGEPQ09 RELAGEPQ10 RELAGEPQ11 RELAGEPQ12
CDFQ01 CDFQ02 CDFQ03 CDFQ04
CDFQ05 CDFQ06 CDFQ07 CDFQ08
CDFQ09 CDFQ10 CDFQ11 CDFQ12
CDF2Q01 CDF2Q02 CDF2Q03 CDF2Q04
CDF2Q05 CDF2Q06 CDF2Q07 CDF2Q08
CDF2Q09 CDF2Q10 CDF2Q11 CDF2Q12}];
APPEND FROM MATOUT;
CLOSE OUTD&ST.;

QUIT;

PROC UNIVARIATE DATA=OUTD&ST.;
VAR CDFQ12 CDF2Q12 DELTA DELTASTD;
RUN;

PROC CHART DATA=OUTD&ST.;
VBAR CDFQ12 CDF2Q12 DELTA DELTASTD;
RUN;

DATA SAF.OUTD&ST.; SET OUTD&ST.;
RECID = (CENSOR = 0);
RECIDP= (CDFQ12>0.5);
RECIDP2=(CDF2Q12>0.5);
DELTAHI = DELTA+2*DELTASTD;
DELTALO = DELTA-2*DELTASTD;
DELTACAT = (DELTALO <= 0 <= DELTAHI)*0 + (DELTALO > 0) - (DELTAHI < 0);
RUN;

PROC FREQ DATA=SAF.OUTD&ST.;
TABLE RECID*RECIDP RECID*RECIDP2 DELTACAT;
RUN;

PROC PRINTTO;
RUN;
%MEND;

```