

# Effects of index-fund investing on commodity futures prices\*

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## Abstract

The last decade brought substantial increased participation in commodity markets by index funds that maintain long positions in the near futures contracts. Policy makers and academic studies have reached sharply different conclusions about the effects of these funds on commodity futures prices. This paper proposes a unifying framework for examining this question, noting that according to a simple model of futures arbitrage, if index-fund buying influences prices by changing the risk premium, then the notional positions of the index investors should help predict excess returns in these contracts. We find no evidence that the positions of traders in agricultural contracts identified by the CFTC as following an index strategy can help predict returns on the near futures contracts. We review evidence that these positions might help predict changes in oil futures prices, and find that while there is some support for this in the earlier data, this appears to be driven by some of the dramatic features of the 2007-2009 recession, with the relation breaking down out of sample.

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# 1 Introduction

The last decade has seen a phenomenal increased participation by financial investors in commodity futures markets. A typical strategy is to take a long position in a near futures contract, and as the contract nears maturity, sell the position and assume a new long position in the next contract, with the goal being to create an artificial asset that tracks price changes in the underlying commodity. Barclays Capital estimated that exchange traded financial products following such strategies grew from negligible amounts in 2003 to a quarter trillion dollars by 2008 (Irwin and Sanders (2011)). Stoll and Whaley (2010) found that in recent years up to half of the open interest in outstanding agricultural commodity futures contracts was held by institutions characterized by the Commodity Futures Trading Commission (CFTC) as commodity index traders.

This trend has been accompanied by a broad public perception that increased participation by financial institutions in commodity futures markets has made an important contribution to the increase in commodity prices observed since 2004. This position has been championed, for example, by hedge fund manager Michael Masters in testimony before the U.S. Congress (Masters (2008)) and former Congressional Representative Joseph Kennedy (Kennedy (2012)).

Surveys of previous academic studies by Irwin and Sanders (2011) and Fattouh, Kilian, and Mahadeva (forthcoming), as well as our own review in Section 2 below, failed to find much empirical support for these claims. What accounts for their continued prominence in policy discussions? Masters (2009) saw the case as simple and clear-cut:

Buying pressure from Index Speculators overwhelmed selling pressure from pro-

ducers and the result was skyrocketing commodity prices.

This claim involves two separate links: first, that increased volume on the buy side drives up the price of a futures contract, and second, that higher futures prices would be sufficient on their own to produce an increase in spot prices. Possible channels for the second link have been discussed by Hamilton (2009), Knittel and Pindyck (2013), and Sockin and Xiong (2013). In this paper we focus on the first link—by what mechanism could increased index-fund buying affect the equilibrium price of a futures contract, and how would we look for evidence of such an effect?

After reviewing the previous literature in Section 2, we sketch in Section 3 a simple model in which an increased volume of buy orders could affect futures prices by changing the equilibrium risk premium. We show that an implication of this framework is that regressions similar to those run by previous researchers can be a useful way to measure the impact of index-fund investing on commodity futures prices. We note that according to our theoretical formulation, it would be the notional positions of the index-fund investors rather than the number of contracts or related measures that would help predict log returns if index investing were having a significant effect. In Section 4, we use data on the 12 commodities covered by the Supplemental Commitment of Traders, and find, consistent with most of the earlier literature, that index-fund investing seems to have had little impact on futures prices in these markets. Section 5 examines the evidence on oil markets. We first reproduce some of the findings in Singleton (forthcoming) that are consistent with the claim that index-fund buying affected oil futures prices. We then review the criticisms raised by Irwin and Sanders (2012) about Singleton’s method for inferring the crude oil positions of index-fund traders, and generalize

the method to mitigate some of these criticisms. We find that while such measures still fit in sample, their out-of-sample performance is poor. Our conclusions are summarized in Section 6.

## **2 Previous literature on the effects of index-fund investing on commodity futures prices.**

One piece of evidence sometimes viewed as supportive of the view that financial speculation has played a role in recent commodity price movements is the observation that the correlation between commodity price changes and other financial returns has increased substantially in recent years. Tang and Xiong (2012) found this correlation is stronger among commodities included in the main index funds than for commodities not included, and Buyuksahin and Robe (2010) and Buyuksahin and Robe (2011) related these correlations specifically to micro data on positions of different types of commodity traders. However, as Fattouh, Kilian, and Mahadeva (forthcoming) noted, the increasing correlation could also be attributed to an increasing importance of common factors, such as the growing importance of emerging markets in both commodity markets and global economic activity and the global character of the financial crisis in 2007-2009, factors to which commodity traders would logically respond.

Another approach uses structural vector autoregressions. One common strategy is to interpret a simultaneous unanticipated rise in prices and commodity inventories as reflecting speculative demand pressure. Kilian and Murphy (forthcoming) concluded that such a model rules out speculative trading as a possible cause of the 2003-2008 surge in oil prices. On

the other hand, Lombardi and Robays (2011) and Juvenal and Petrella (2011) found a small role for speculation using alternative specifications. In addition to sensitivity to specification, there is a fundamental identification challenge in using these strategies to distinguish a rise in prices and inventories that results from destabilizing speculation from one that represents a socially optimal response to rationally perceived future market tightness.<sup>1</sup>

A third strand in the literature examines whether changes in commodity futures prices could be predicted on the basis of the positions of different types of commodity traders. Here again, the evidence is mostly negative. Brunetti, Buyuksahin, and Harris (2011) used proprietary CFTC data over 2005-2009 on daily positions of traders disaggregated into merchants, manufacturers, floor brokers, swap dealers, and hedge funds. They found that changes in net positions of any of the groups could not help to predict changes in the prices of futures contracts for the three commodities they studied (crude oil, natural gas, and corn). Sanders and Irwin (2011a) used the CFTC's publicly available Disaggregated Commitment of Traders Report on weekly net positions of swap dealers, and found these were no help in predicting returns on 14 different commodity futures contracts over 2006-2009. Sanders and Irwin (2011b) used proprietary CFTC data to extend the public Supplemental Commitment of Traders (SCOT), which categorizes certain participants as commodity index traders, back to 2004. They found that changes in the positions of index traders did not help predict weekly returns for corn or wheat but found some predictability for soybeans under some specifications. Stoll and Whaley (2010) used the public SCOT for 12 agricultural commodities over 2006-2009 and found that changes in the long positions of commodity index traders predicted weekly returns

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<sup>1</sup>For further discussion see Kilian and Murphy (2012) and Fattouh, Kilian, and Mahadeva (forthcoming).

for cotton contracts but none of the other 11 commodities. Alquist and Gervais (2011) used the public CFTC Commitment of Traders Report to measure net positions of commercial and non-commercial traders, and found that changes in either category could not predict monthly changes in oil prices or the futures-spot spread over 2003-2010, though there was statistically significant predictability when the sample was extended back to 1993. Irwin and Sanders (2012) used the CFTC's Index Investment Data on quarterly positions in 19 commodities held by commodity index funds. They found in a pooled regression that changes in these positions did not predict futures returns over 2008-2011. They also separately analyzed whether changes in futures positions of a particular oil- or gas-specific exchange traded fund could predict daily returns on those contracts over 2006-2011, and again found no predictability. Buyuksahin and Harris (2011) used proprietary CFTC data on daily positions broken down by non-commercials, commercials, swap dealers, hedge funds, and floor broker-dealers. They found the last category could help predict changes in oil futures prices one day ahead, but no predictability for any of the other categories or other horizons. By contrast, Singleton (forthcoming) found that a variety of measures, including a 13-week change in index-fund holdings imputed from the SCOT, could help predict weekly and monthly returns on crude oil futures contracts over September 2006 to January 2010.

As we will see in Section 3 below, it is possible to motivate regressions similar to these from a simple model of risk premia in commodity futures contracts. Keynes (1930) proposed that risk premia in commodity futures prices could arise from the desire of producers of the physical commodity to hedge their price risk by selling futures contracts. In order to persuade a counterparty to take the other side, the equilibrium price of a futures contract might be

pushed below the expected future spot price to produce a situation sometimes described as “normal backwardation.” Evidence on backwardation is mixed. Carter, Rausser, and Schmitz (1983), Chang (1985), Bessembinder (1992), and De Roon, Nijman, and Veld (2000) provided empirical support for such an interpretation of the risk premium in commodity futures, while Marcus (1984), Hartzmark (1987), and Kolb (1992) concluded that it does not hold as a general characterization.

Acharya, Lochstoer, and Ramadorai (forthcoming), Cheng, Kirilenko, and Xiong (2012), and Hamilton and Wu (2011) proposed that the growing volume of commodity index investors could produce an analogous exogenous price pressure on the buy side, with Hamilton and Wu (2011) finding that the average compensation to the long position in oil futures contracts has decreased but become substantially more volatile since 2005. Etula (forthcoming), Acharya, Lochstoer, and Ramadorai (forthcoming), Danielsson, Shin, and Zigrand (2011), and Cheng, Kirilenko, and Xiong (2012) have stressed the role of limited working capital on the part of potential arbitrageurs as the key factor determining how much the futures price might deviate from the expected future spot price. In the following section, we follow Hamilton and Wu (2011) in using a simple quadratic objective function as an approximation to a more detailed model of the capital limitations of potential arbitrageurs. Hamilton and Wu (2011) used this framework to infer risk prices from the predictability of futures returns based on their own lagged values. By contrast, in this paper we study the relation between futures returns and lagged observations on the contract positions of commodity-index traders, and show how the framework can be used to motivate and interpret some simple regression tests of the hypothesis that index-fund investing has an independent effect on commodity futures prices.

### 3 Index-fund investors and the price of risk.

Let  $F_{nt}$  denote the price of a commodity associated with an  $n$ -period futures contract agreed upon at date  $t$ . Entering such a contract requires maintaining a margin account, to which funds must be added if the market moves against the trader and from which funds can be withdrawn if the market moves in the trader's favor. Following Duffie (1992, p. 39), one can think of the initial margin deposit as funds the trader would have held in that form in any case. From that perspective, each unit of the commodity purchased through a long position in the contract is associated with zero initial cost and a cash flow at  $t + 1$  of  $F_{n-1,t+1} - F_{nt}$ . If index-fund buyers want to take the long side of the contract, somebody else must be persuaded to take the short side. We will refer to the index fund's counterparty as an "arbitrageur", and assume that what the arbitrageur cares about is the mean and variance of their composite portfolio. Let  $z_{nt}$  denote a representative arbitrageur's notional exposure (with  $z_{nt} > 0$  denoting a long position and  $z_{nt} < 0$  a short); thus for example  $z_{nt}/F_{nt}$  is the number of barrels of oil purchased through an  $n$ -period contract. An arbitrageur who takes a position  $z_{nt}$  would experience a cash flow at time  $t + 1$  given by

$$z_{nt} \left[ \frac{F_{n-1,t+1} - F_{nt}}{F_{nt}} \right]. \quad (1)$$

In addition to potential positions in a variety of futures contracts, we presume that the arbitrageur also invests amounts  $q_{jt}$  in assets  $j = 0, 1, \dots, J$  (where asset  $j = 0$  is presumed to be risk free). If the gross return for asset  $j$  between  $t$  and  $t + 1$  is represented as  $\exp(r_{j,t+1})$ , then

the arbitrageur's wealth at  $t + 1$  will be

$$W_{t+1} = \sum_{j=0}^J q_{jt} \exp(r_{j,t+1}) + \sum_{n=1}^N z_{nt} \frac{F_{n-1,t+1} - F_{nt}}{F_{nt}}.$$

We assume that the arbitrageur chooses  $\{q_{0t}, \dots, q_{Jt}, z_{1t}, \dots, z_{nt}\}$  so as to maximize

$$E_t(W_{t+1}) - (\gamma/2)\text{Var}_t(W_{t+1}) \quad (2)$$

subject to  $\sum_{j=0}^J q_{jt} = W_t$ . We also conjecture that in equilibrium log asset returns and commodity futures prices are affine functions of a vector of factors  $x_t$ ,

$$f_{nt} = \log F_{nt} = \alpha_n + \beta'_n x_t \quad n = 1, \dots, N \quad (3)$$

$$r_{jt} = \xi_j + \psi'_j x_t \quad j = 1, \dots, J,$$

where the factors themselves can be described using a Gaussian vector autoregression:

$$x_{t+1} = c + \rho x_t + \Sigma u_{t+1} \quad u_t \sim \text{i.i.d. } N(0, I_m). \quad (4)$$

Under these assumptions, Hamilton and Wu (2011) showed that

$$\begin{aligned} E_t(W_{t+1}) &\approx q_{0t}(1 + r_{0,t+1}) + \sum_{j=1}^J q_{jt} \left[ 1 + \xi_j + \psi'_j(c + \rho x_t) + (1/2)\psi'_j \Sigma \Sigma' \psi_j \right] \\ &\quad + \sum_{n=1}^N z_{nt} \left[ \alpha_{n-1} + \beta'_{n-1}(c + \rho x_t) - \alpha_n - \beta'_n x_t + (1/2)\beta'_{n-1} \Sigma \Sigma' \beta_{n-1} \right] \end{aligned} \quad (5)$$

$$\text{Var}_t(W_{t+1}) \approx \left( \sum_{j=1}^J q_{jt} \psi'_j + \sum_{n=1}^N z_{nt} \beta'_{n-1} \right) \Sigma \Sigma' \left( \sum_{j=1}^J q_{jt} \psi_j + \sum_{\ell=1}^N z_{\ell t} \beta_{\ell-1} \right). \quad (6)$$

The arbitrageur's first-order condition associated with the choice of  $z_{nt}$  is then characterized by

$$\alpha_{n-1} + \beta'_{n-1}(c + \rho x_t) - \alpha_n - \beta'_n x_t + (1/2) \beta'_{n-1} \Sigma \Sigma' \beta_{n-1} = \beta'_{n-1} \lambda_t \quad (7)$$

where  $\lambda_t$  depends on the positions that arbitrageurs take in the various contracts according to

$$\lambda_t = \gamma \Sigma \Sigma' \left( \sum_{j=1}^J q_{jt} \psi_j + \sum_{\ell=1}^N z_{\ell t} \beta_{\ell-1} \right). \quad (8)$$

If we further conjecture that in equilibrium these positions are also affine functions of the underlying factors,

$$\lambda_t = \lambda + \Lambda x_t, \quad (9)$$

then equations (7) and (9) turn out to imply a recursion that the commodity-futures loadings  $\alpha_n$  and  $\beta_n$  would satisfy that are very similar to those used in affine models of the term structure of interest rates (e.g., Ang and Piazzesi (2003)).

The term  $\lambda_t$  allows the possibility of nonzero expected returns in equilibrium and is often referred to as the price of risk. If arbitrageurs are risk neutral, then  $\gamma$  and  $\lambda_t$  in (8) are both 0 and (7) implies that the expected net gain from any futures position (1) is always zero. More generally, with nonzero  $\gamma$ , equation (8) describes how changes in arbitrageurs' risk exposure coming from changes in  $q_{jt}$  or  $z_{\ell t}$  would be associated with changes in expected returns. In particular, consider the effects of an exogenous increase in index-fund buying pressure on the  $n$ th contract. In equilibrium, prices must be such as to persuade arbitrageurs to take the

opposite side, that is, the values of  $\alpha_n$  and  $\beta_n$ , must be such that (7) holds for  $z_{nt}$  given by the necessary negative magnitude. Higher buying must be matched by more negative values for  $z_{nt}$  which change the risk premium in (7) through (8).

Hamilton and Wu (2011) estimated values of the structural parameters of this system  $(c, \rho, \Sigma, \lambda, \Lambda)$  by inferring factors indirectly from the observed time-series properties of oil futures prices. By contrast, in this paper we propose to use direct observations on the positions of index-fund investors. Note that we can substitute (4), (3) and (9) into (7) to deduce

$$f_{n-1,t+1} - f_{nt} = \kappa_{n-1} + \pi'_{n-1}x_t + \varepsilon_{n-1,t+1} \quad (10)$$

where the theory predicts  $\kappa_{n-1} = \beta'_{n-1}\lambda - (1/2)\beta'_{n-1}\Sigma\Sigma'\beta_{n-1}$ ,  $\pi'_{n-1} = \beta'_{n-1}\Lambda$ , and  $\varepsilon_{n-1,t+1} = \beta'_{n-1}\Sigma u_{t+1}$ . Thus a core implication of this model of risk aversion is a linear relation between the expected log returns and the notional positions  $z_{nt}$  of arbitrageurs in commodity futures contracts. Note that if arbitrageurs are risk neutral ( $\gamma = 0$ ), then we should find  $\pi_{n-1} = 0$ . On the other hand, risk-averse arbitrageurs would require compensation for taking the opposite position from index-fund buyers. If index funds are long, arbitrageurs are short, and expect subsequently to close their futures positions at a lower price than the initial contract. This would imply a negative coefficient on the element of  $x_t$  corresponding to a measure of the level of index-fund buying— if index buying makes the price of a futures contract higher than it would otherwise be, the expected excess return for a long position on that contract would be negative. The framework thus provides a motivation and interpretation for regressions similar to those reviewed in Section 2.

As a simple example, suppose that  $t$  represents months and index-fund investors always

desire a long position with notional exposure  $K_t$  in the 2-month contract, selling their position as the month comes to a close in order to take a position  $K_{t+1}$  in the new 2-month contract.

Then prices must be such that in equilibrium,

$$z_{nt} = \begin{cases} -K_t & \text{if } n = 2 \\ 0 & \text{otherwise} \end{cases} .$$

In the absence of other risk factors, we would then from (8) have the following simple expression determining the price of commodity-futures risk:

$$\lambda_t = -\gamma \Sigma \Sigma' \beta_1 K_t.$$

If we postulate an additional vector of factors  $x_t^*$  that matter for commodity price fundamentals in determining the value of  $f_{0t}$ , then the complete vector of factors is given by  $x_t = (K_t, x_t^*)'$  and we have that  $f_{nt} = \alpha_n + \beta_n' x_t$ , with futures prices a function of both fundamentals  $x_t^*$  and index-fund buying  $K_t$ . If we were to rule out feedback from futures prices to fundamentals through mechanisms investigated by Knittel and Pindyck (2013), and Sockin and Xiong (2013), the first element of  $\beta_0$  would be zero but the first element of  $\beta_n$  would generally be nonzero for all  $n > 0$ .<sup>2</sup>

In principle, performing the regression (10) would require observation on the demands for

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<sup>2</sup>In the above example in which index funds want only the 2-month contract at time  $t$ , an arbitrageur who shorts this contract is exposed to the complete vector of factor risks associated with this contract through  $\beta_1' x_{t+1}$ , including for example fundamentals uncertainty about the price of the underlying commodity. Assuming these fundamentals are positively serially correlated, if there was zero expected return associated with a 1-period contract purchased at  $t$ , an arbitrageur would want to be long this contract to hedge some of the risk associated with being short the 2-period contract. Since there is no one to take the other side of this 1-period contract, equilibrium then requires a negative expected return on a 1-period contract purchased at  $t$  just as on a 2-period contract purchased at  $t$ . For details see Hamilton and Wu (2011).

futures contracts coming from all the arbitrageurs' counterparties, which would include not just index-fund traders but also commercial hedgers, as well as all other factors influencing risk of any other assets held by arbitrageurs. There is nonetheless a robust implication of the reduced-form equation (10). Unless the positions of commercial hedgers and index-fund traders are perfectly negatively correlated, the positions of index-fund traders will be correlated with the net buying pressure facing arbitrageurs. If the latter is exerting a significant effect on the pricing of futures contracts, we should find a nonzero coefficient on  $\pi_{n-1}$  in (10) when  $x_t$  is based on observable measures of the notional positions taken by index-fund traders. We look for empirical evidence of such an effect in the next section.

## **4 Predicting futures returns for agricultural commodities.**

For 12 agricultural commodities, since 2006 the CFTC has been providing through its Supplemental Commitments of Traders Report weekly positions for traders it characterizes as “replicating a commodity index by establishing long futures positions in the component markets and then rolling those positions forward from future to future using a fixed methodology” (CFTC (2012)). While some of these index traders are pension funds or other managed funds taking a direct position in futures contracts, the majority represent positions by swap dealers, who offer their clients an over-the-counter product that mimics some futures-based index (Stoll and Whaley (2010)). The swap dealers are thus implicitly short in futures agreements arranged over-the-counter, and hedge with an offsetting long position on organized exchanges

that get reported to the CFTC. While the CFTC designations are not without some problems (Cheng, Kirilenko, and Xiong (2012), Stoll and Whaley (2010)), these appear to be the best high-frequency data that are publicly available for our purposes.

The SCOT is released on a Friday and reflects positions as of the preceding Tuesday. Let  $t$  denote a week ending on a particular Tuesday and  $X_t$  the long positions (measured in number of contracts) being held by commodity index traders as identified by SCOT. Let  $F_t$  denote the price of the near contract as of the market close on the day for which SCOT reports  $X_t$ .<sup>3</sup> If this is the contract being held by a typical index trader, then

$$\tilde{x}_t = 100(\ln X_t + \ln F_t)$$

would correspond to the log of index traders' notional exposure.<sup>4</sup>

Our interest centers on the predictability of  $r_t$ , the weekly return of a given contract.<sup>5</sup> The first two rows within each block of Table 1 report coefficients and standard errors for the following regression estimated for  $t$  running from April 11, 2006 to January 3, 2012:

$$r_t = \alpha_1 + \phi_1 r_{t-1} + \pi_1 \tilde{x}_{t-1} + \varepsilon_{1t}. \quad (11)$$

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<sup>3</sup>Daily futures prices were purchased from Norma's Historical Data (<http://www.normahistoricaldata.com/>). For a few days in our sample, SCOT data are reported for days on which we have no closing futures prices. For these observations, we used the futures price as of the following day.

<sup>4</sup>Note that  $X_t$  is measured in number of contracts, so that the true measure of notional exposure would further multiply  $X_t$  by the number of barrels of oil in a single contract. This would simply add a constant to  $\tilde{x}_t$  and would have no effect on the slope coefficients in any of the regressions reported in this section, so we have always used the simpler expression given in the text.

<sup>5</sup>For most weeks,  $r_t$  is just  $100(f_t - f_{t-1})$  where  $f_t = \ln(F_t)$  the log of the price of the nearest contract. In other words,  $r_t$  is the percent change in price of the near contract. In the case when the near contract as of date  $t - 1$  had expired as of date  $t$ , we took  $r_t$  to be 100 times the change between  $f_t$  and the log of the price of that same contract as of  $t - 1$  (at which date it was the second available contract).

The coefficient estimates  $\hat{\phi}_1$  and  $\hat{\pi}_1$  are not statistically significantly different from zero for any of the 12 commodities for which index trader positions are reported, and adjusted  $R^2$  for these regressions are usually negative. This result is consistent with the large number of previous studies discussed in Section 2 that have found limited predictability of commodity futures returns using related regressions.

Equations (4) and (10) can be viewed as the central implications of the model of risk pricing sketched in Section 3. Given observed data on futures prices and  $x_t$ , it is straightforward to estimate the unrestricted reduced form implications of these models using ordinary least squares. These coefficients could then be used to infer values for the parameters  $(c, \rho, \Sigma, \lambda, \Lambda)$  of the structural model using methods described by Hamilton and Wu (2012) and Hamilton and Wu (2011), and in fact this simple, intuitive approach to estimation turns out to be asymptotically equivalent to full information maximum likelihood estimation of the model. However, when the key reduced-form parameters  $\phi$  and  $\pi$  are statistically indistinguishable from zero, one would have little confidence in any values for the risk-pricing parameters in  $\Lambda$  that one might infer from the data, and for this reason we have chosen not to try to go beyond the simple reduced-form estimates reported here. Our conclusion is that although in principle index-fund buying of commodity futures could influence pricing of risk, we do not find confirmation of that in the week-to-week variability of the notional value of reported commodity index trader positions.

If the factors governing the price of risk are stationary, the dependent variable in (11) would be stationary, in which case one might prefer to use the weekly change in index-trader notional positions rather than the level as the explanatory variable. The third and fourth

rows of each block in Table 1 report OLS coefficient estimates and standard errors for the regression

$$r_t = \alpha_2 + \phi_2 r_{t-1} + \pi_2 (\tilde{x}_{t-1} - \tilde{x}_{t-2}) + \varepsilon_{2t}. \quad (12)$$

The coefficients on the change in index notional positions turn out to be statistically significant at the 5% level for cotton and sugar but of opposite signs, and neither  $\hat{\phi}$  nor  $\hat{\pi}$  are statistically significantly different from zero for any of the other 10 commodities. We again conclude that there appears to be very little indication in the data that changes in positions of index traders can help explain risk premia in commodity futures prices.

Singleton (forthcoming) has recently suggested that investment flows may matter over longer periods than a week, and instead bases his analysis of crude oil futures returns on the change in notional positions over a 3-month period. The fifth and sixth rows of each block in Table 1 report coefficient estimates and standard errors for our 12 agricultural commodities in which the predictive variable is the lagged 13-week change in the commodity index notional position:

$$r_t = \alpha_3 + \phi_3 r_{t-1} + \pi_3 (\tilde{x}_{t-1} - \tilde{x}_{t-14}) + \varepsilon_{3t}. \quad (13)$$

None of the 24 estimated slope coefficients is statistically distinguishable from zero. To summarize, we find no persuasive evidence that either the level, weekly change, or 13-week change in index-trader positions is related to the risk premium in agricultural commodities.

Finally, we report some simple evidence that is robust with respect to any problems in measuring the volume of index buying itself and makes use of higher-frequency features of the data. The two main indexes that buyers seek to track are the S&P-Goldman Sachs

Commodity Index and the Dow Jones-UBS Commodity Index. Each of these has a defined calendar schedule at which a near contract is sold and the next contract is purchased. The Goldman strategy begins the roll into the next contract on the 5th business day of the month and is completed on the 9th, whereas the Dow Jones strategy begins the roll on the 6th and ends on the 10th. It is simple enough to ask whether there is anything special about price movements on these particular days.

We calculated the daily return on the near contract  $r_\tau = 100(f_\tau - f_{\tau-1})$  where  $\tau$  now indexes business days, and estimated the OLS regression

$$r_\tau = \alpha_4 + \pi_4 S_\tau + \varepsilon_{4\tau}. \quad (14)$$

Here  $S_\tau = 1$  if both (1)  $\tau$  is the 5th through the 10th business day of the month and (2) the Goldman and Dow Jones strategies would be selling the near contract during that period; otherwise,  $S_\tau = 0$ . In the case of crude oil, for which a new contract exists every month,  $S_\tau$  is a simple calendar dummy tracking the 5th through 10th business days of the month. For all other commodities, some months are not traded; for example, there is no February contract in soybeans. Thus as of the beginning of January, the near soybean contract would be the March contract. The index funds would not be selling their soybean position during January, so  $S_\tau$  would remain zero for soybeans throughout the month of January. Note that the OLS estimate  $\hat{\pi}_4$  is thus numerically equal to the difference between the average daily return from a long position on the near contract that is sold on days when the index funds are selling that contract compared to the return on the near contract on non-roll days. Moreover, because

the average return over 6 days is numerically identical to  $(1/6)$  times the 6-day return,

$$N^{-1} \sum_{n=1}^N r_{\tau+n} = (100/N)(f_{\tau+N} - f_{\tau}),$$

one can equivalently interpret regression (14) as indicating the average result if one buys the near contract on the day before the index funds begin to sell and sells on the day when the funds are finished selling their positions.

Columns 1 and 2 of Table 2 report coefficient estimates and standard errors for (14) fit to daily returns on the near contract for the commodities we analyze. We find a statistically significant value for  $\hat{\pi}_4$  for only 1 of the 12 agricultural commodities (soybeans), and this is of the opposite sign predicted by the simple price impact hypothesis— if index-fund selling is depressing the price on roll days, one would expect the price of the near contract to fall rather than rise on those days.

Columns 3 and 4 of Table 2 report results for the analogous regressions using the next contract. Here only 2 of the estimated coefficients (namely, those for soybeans and hogs) are statistically significantly different from zero. And while these are of the predicted sign (a positive coefficient consistent with the claim that index buying of the next contract is pushing the price of the contract up), note that for beans a statistically significant positive coefficient was found for both the near contract that funds are selling (column 2) as well as the next contract that funds are buying (column 4).

Finally, in columns 5 and 6 we report results when the dependent variable is the return on the next contract minus the return on the near. Here  $\pi_4$  can be interpreted as the average

excess returns for someone who is simultaneously buying the next contract and selling the near. Only one commodity (hogs) has a coefficient that is statistically significantly different from zero.

By contrast, Mou (2010) has recently reported statistically significant differences in commodity futures returns across the index fund roll. Mou combined the evidence across different commodities, which potentially could give the test more power. However, we find the individual spread coefficients to be positive as often as negative, so pooling alone seems unlikely to be the only explanation for the differences in results. Mou also based his calculations on holding strategies that begin 5 to 10 business days before the index-fund roll, though this makes it difficult to separate end-of-month and expiry effects from those of the roll itself.

## **5 Predicting returns for crude oil contracts.**

Although there appears to be limited relation between commodity index positions and agricultural futures returns, Singleton (forthcoming) reported that a number of interesting variables appear to help predict returns on crude oil futures contracts. Our interest in this paper is the strong predictive power he found for a measure of holdings by index-fund traders in crude oil futures contracts.

The CFTC does not report a weekly estimate of index-fund positions in crude oil. Singleton's approach was to use an idea suggested by Masters (2008). Masters claimed that the vast majority of index-fund buyers were following one of two strategies, trying to track either the S&P-Goldman Sachs Commodity Index or the Dow Jones-UBS (formerly Dow Jones-AIG)

Commodity Index. Each of these would take positions in a particular set of commodities and roll them over according to a prespecified calendar schedule. Let  $\tilde{X}_{it}$  be the notional value of contracts in agricultural commodity  $i$  reported by SCOT to have been held by index-fund traders on date  $t$ , that is,  $\tilde{X}_{it} = X_{it}F_{it}Q_i$  for  $X_{it}$  the number of contracts held by index-fund traders,  $F_{it}$  the futures price, and  $Q_i$  the number of units of the commodity held by a single contract.<sup>6</sup> Suppose we assume that this is composed entirely of either traders following the Goldman strategy, whose notional holdings we denote by  $\tilde{X}_{it}^G$ , or traders following the Dow Jones strategy ( $\tilde{X}_{it}^D$ ):

$$\tilde{X}_{it} = \tilde{X}_{it}^G + \tilde{X}_{it}^D.$$

Masters (2008) noted that while the Dow Jones index holds soybean oil, the Goldman index does not, in which case

$$\tilde{X}_{\text{bean.oil},t} = \tilde{X}_{\text{bean.oil},t}^D.$$

We further know that someone trying to replicate the Dow Jones index would have their total notional exposure  $\tilde{D}_t$  allocated across the commodities according to known weights  $\delta_{it}^D$ ,<sup>7</sup> so that  $\tilde{X}_{it}^D = \delta_{it}^D \tilde{X}_t^D$ . Hence one could use the SCOT bean oil figures to infer the total notional holdings of Dow Jones investors,  $\tilde{X}_t^D = \tilde{X}_{\text{bean.oil},t} / \delta_{\text{bean.oil},t}^D$ , and from this impute holdings of Dow Jones investors in crude oil contracts on the basis of SCOT reported holdings of soybean oil:

$$\tilde{X}_{\text{crude.oil},t}^{D, [\text{bean.oil}]} = \delta_{\text{crude.oil},t}^D \tilde{X}_{\text{bean.oil},t} / \delta_{\text{bean.oil},t}^D.$$

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<sup>6</sup>Note that this is a slight change in notation from the previous sections, where we instead measured  $\tilde{X}_{it}$  as just  $X_{it}F_{it}$ . As noted in footnote 5, the slope coefficients in the previous section would be numerically identical regardless of which convention is used, but the added term  $Q_{it}$  needs to be included for the Masters-type calculations used in this section.

<sup>7</sup>We thank Dow Jones for providing us with historical values for the weights  $\delta_{it}^D$ .

We have added the superscript [bean\_oil] to this estimate of crude oil notional holdings to clarify that the underlying SCOT data from which it is derived in fact describe soybean oil holdings rather than crude oil. Similarly, the Goldman index holds Kansas City wheat whereas Dow Jones does not, giving an estimate of Goldman holdings of crude oil contracts:<sup>8</sup>

$$\tilde{X}_{\text{crude\_oil},t}^{G,[\text{KC-wheat}]} = \delta_{\text{crude\_oil},t}^G \tilde{X}_{\text{KC-wheat},t} / \delta_{\text{KC-wheat},t}^G. \quad (15)$$

The Goldman index also holds feeder cattle which Dow Jones does not, affording an alternative estimate

$$\tilde{X}_{\text{crude\_oil},t}^{G,[\text{feeder\_cattle}]} = \delta_{\text{crude\_oil},t}^G \tilde{X}_{\text{feeder\_cattle},t} / \delta_{\text{feeder\_cattle},t}^G. \quad (16)$$

Masters proposed to use the average of (15) and (16) as an estimate of Goldman crude oil contract holdings. The sum of the oil holdings imputed to these two funds is then his estimate of total index-fund holdings of crude oil contracts:

$$\tilde{X}_{\text{crude\_oil},t}^{[\text{Masters}]} = \tilde{X}_{\text{crude\_oil},t}^{D,[\text{bean\_oil}]} + (1/2) \left( \tilde{X}_{\text{crude\_oil},t}^{G,[\text{KC-wheat}]} + \tilde{X}_{\text{crude\_oil},t}^{G,[\text{feeder\_cattle}]} \right). \quad (17)$$

Figure 1 plots the number of contracts associated with this value for  $\tilde{X}_{\text{crude\_oil},t}^{[\text{Masters}]}$  against the price of crude oil based on the near contract, updating similar figures in Masters (2008) and Singleton (forthcoming). The figure suggests a strong connection between these two series, particularly during 2008 and 2009.

We repeated our basic regressions (11)-(13) for  $r_t$  now the weekly return on the near crude

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<sup>8</sup>We thank Standard & Poor's for providing us with historical values for  $\delta_{it}^G$ .

oil futures contract and  $\tilde{x}_t = 100 \ln \tilde{X}_{\text{crude.oil},t}^{[\text{Masters}]}$ . These results are reported in the first block of Table 3. Both the levels and weekly-difference regression results are similar to those for agricultural commodities, with negative values for  $\overline{R}^2$  and statistically insignificant coefficients. We also find using daily data (last rows of Table 2) no evidence of excess returns from buying the near or next crude oil contract during the period in which many index traders are rolling contracts. However, the last row of the first block of Table 3 reproduces Singleton's finding that the 13-week change in  $\tilde{X}_{\text{crude.oil},t}^{[\text{Masters}]}$  appears to be quite helpful for predicting changes in crude oil futures prices.

Irwin and Sanders (2012) have recently raised several strong criticisms of using  $\tilde{X}_{\text{crude.oil},t}^{[\text{Masters}]}$  as a measure of index-fund positions in crude oil futures. Irwin and Sanders noted first that although for some dates the two measures  $\tilde{X}_{\text{crude.oil},t}^{G, [\text{KC-wheat}]}$  and  $\tilde{X}_{\text{crude.oil},t}^{G, [\text{feeder-cattle}]}$  are reasonably close, for other dates they can differ greatly. In terms of this concern, we would point out that in fact there is no need to restrict the inference as Masters did only to commodities that appear in one of the indexes but not the other. Note that the central claim is that

$$\tilde{X}_{it} = \delta_{it}^G \tilde{X}_t^G + \delta_{it}^D \tilde{X}_t^D \quad (18)$$

where  $\tilde{X}_{it}$ ,  $\delta_{it}^G$ , and  $\delta_{it}^D$  are all observed directly. Given any two arbitrary agricultural commodities  $i$  and  $j$ , one can use the two equations in (18) to solve for the implied total holdings of the two indexes,  $\tilde{X}_t^G$  and  $\tilde{X}_t^D$ . Hence for any two arbitrary agricultural commodities  $i$  and

$j$  there exists a Masters-type estimate of crude oil holdings:

$$\tilde{X}_{\text{crude.oil},t}^{[i,j]} = \begin{bmatrix} \delta_{\text{crude.oil},t}^G & \delta_{\text{crude.oil},t}^D \end{bmatrix} \begin{bmatrix} \delta_{it}^G & \delta_{it}^D \\ \delta_{jt}^G & \delta_{jt}^D \end{bmatrix}^{-1} \begin{bmatrix} \tilde{X}_{it} \\ \tilde{X}_{jt} \end{bmatrix}. \quad (19)$$

To illustrate the variability of such measures, we calculated (19) where  $j = \text{soybean oil}$  (one of the series used by Masters and Singleton) and  $i$  corresponding to any one of the other 11 possible choices. Plots of  $\tilde{X}_{\text{crude.oil},t}^{[i,\text{bean.oil}]}$  for different  $i$  are plotted in Figure 2. These series indeed appear to be fairly sensitive to the choice of  $i$ .

One way to deal with this issue is to generalize Masters' averaging idea. There's no reason in fact not to use all 12 agricultural commodities together, choosing  $\tilde{X}_t^G$  and  $\tilde{X}_t^D$  so as to minimize the sum of squared discrepancies in predicting the SCOT reported value for  $\tilde{X}_{it}$  across the 12 commodities. This amounts to treating the collection of equations (18) for  $i = 1, \dots, 12$  and for a given  $t$  as a sample of size 12 in which the dependent variable is  $\tilde{X}_{it}$  and explanatory variables are  $\delta_{it}^G$  and  $\delta_{it}^D$ :

$$\tilde{X}_{\text{crude.oil},t}^{[\text{all}]} = \begin{bmatrix} \delta_{\text{crude.oil},t}^G & \delta_{\text{crude.oil},t}^D \end{bmatrix} \begin{bmatrix} \sum_{i=1}^{12} (\delta_{it}^G)^2 & \sum_{i=1}^{12} \delta_{it}^G \delta_{it}^D \\ \sum_{i=1}^{12} \delta_{it}^D \delta_{it}^G & \sum_{i=1}^{12} (\delta_{it}^D)^2 \end{bmatrix}^{-1} \begin{bmatrix} \sum_{i=1}^{12} \delta_{it}^G \tilde{X}_{it} \\ \sum_{i=1}^{12} \delta_{it}^D \tilde{X}_{it} \end{bmatrix}. \quad (20)$$

These regression-based estimates of index-fund holdings are also plotted in Figure 2.

We repeated our predictive regressions using  $\tilde{X}_{\text{crude.oil},t}^{[\text{all}]}$  in place of  $\tilde{X}_{\text{crude.oil},t}^{[\text{Masters}]}$  in the second block of Table 3. The results turn out to be quite similar to those based on Masters' original series. Nothing is significant and  $\bar{R}^2$  are negative for the levels or first-difference specifications, but there is significant predictability from the 13-week change in  $\tilde{X}_{\text{crude.oil},t}^{[\text{all}]}$ . Interestingly, we

found the same is true for every one of the bivariate estimates plotted in Figure 2: the 13-week change in crude oil index-trader positions, inferred from soybean oil and any other arbitrary agricultural commodity, appear to help predict crude oil returns.

A second concern that Irwin and Sanders (2012) raised about Masters' methodology is that the index oil holdings as imputed from agricultural commodity positions are quite different from direct estimates of crude oil positions that the CFTC reports in its new Index Investment Data report. Unfortunately, the Index Investment Data report is only available at a quarterly frequency and for a shorter period than SCOT, so is not usable for the kind of regressions we're interested in here. However, it is puzzling that agricultural positions cannot predict agricultural prices but do predict crude oil prices, and that a direct measure of crude oil index holding would do a poorer job at predicting oil prices than does an index imputed from agricultural holdings.

One way to shed further light on these issues is to investigate whether the in-sample success of regression (13) translates into useful out-of-sample forecasts. Since Singleton (forthcoming) was written, we have obtained an additional 2 years of data, which allow us to perform a true out-of-sample exercise to see whether the 13-week change has actual predictive power outside of the sample for which it was originally proposed.

We re-estimated equation (13) for a sample ending January 12, 2010, the same ending date used by Singleton. The specification performs even better over this subsample, raising the  $\overline{R}^2$  to 0.083 (see the first two rows of Table 4). However, if we use the coefficients estimated over April 11, 2006 to January 12, 2010 to forecast weekly crude oil returns over January 17, 2010 to January 3, 2012, the mean squared forecast error is 23.8, which is 22% bigger than

the error one would make if one simply always expected zero returns on the near contract.

Returning to Figure 1, the striking feature of the Masters series is that it collapses as the recession worsened in 2008 but began to rebound sharply before the recovery began, key movements that precede equally dramatic parallel moves in oil prices. The close fit over Singleton's original sample period seems to result from the broad comovement of the series during the 2007-2009 recession. It's interesting to note that if we replace  $r_t$  in expression (13) with the weekly return on the U.S. S&P500 stock price index, but with the second explanatory variable still  $100[\ln \tilde{X}_{\text{crude.oil},t-1}^{\text{Masters}} - \tilde{X}_{\text{crude.oil},t-14}^{\text{Masters}}]$ , for the 2006-2009 subsample the Masters variable would also appear to be statistically significant (see the last rows of Table 4). In other words, if we used only data from the recession, we would conclude that index-trader positions in soybean oil, Kansas City wheat, and feeder cattle could also be used to predict stock prices. Once again, however, a relation estimated over this period has a bigger out-of-sample MSE than the simple no-change forecast.

## 6 Conclusion.

The increased participation by financial investors in commodity futures markets over the last decade has been quite substantial. In principle this could have influenced the risk premium, and Hamilton and Wu (2011) found significant changes in the behavior of the risk premium on oil futures contracts before and after 2005. In this paper we studied data since 2006 to look for a systematic relation between the notional value of commodity futures contracts held on behalf of index-fund investors and expected returns on futures contracts. We found essentially no

relation for the 12 agricultural commodities for which the CFTC reports such positions. We reviewed evidence that positions in crude oil contracts imputed from the reported agricultural holdings could help predict crude oil futures returns, and noted that the methodology for such imputation could be generalized to make use of all the available data. We confirmed that these imputed holdings appear to help predict crude oil returns over 2006-2009, though this is closely related to the dynamics of index investing during the Great Recession, and indeed the same imputed holdings also appear to predict stock returns over that period. We found, however, that both relations broke down when trying to describe the data since 2009.

Our overall conclusion is thus consistent with most of the previous literature—there seems to be little evidence that index-fund investing is exerting a measurable effect on commodity futures prices. As noted in the introduction, even if one could demonstrate an effect of index-fund buying on commodity futures prices, it would be a separate challenge to explain how this could also end up changing the equilibrium spot price. We conclude that it is difficult to find much empirical foundation for a view that continues to have a significant impact on policy decisions.

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Table 1: Tests for predictability of agricultural commodity returns

Beans		Wheat			Corn			
	const	$r_{t-1}$	$X_{t-1}$	$\bar{R}^2$	const	$r_{t-1}$	$X_{t-1}$	$\bar{R}^2$
level	10.8033 (9.5554)	-0.0032 (0.0576)	-0.0056 (0.0051)	-0.0026	30.8385 (17.5042)	0.0014 (0.0576)	-0.0166 (0.0094)	0.0036
1-wk diff	0.2640 (0.2294)	-0.0443 (0.1329)	0.0321 (0.1012)	-0.0064	-0.0489 (0.3076)	0.1817 (0.1804)	-0.1738 (0.1583)	-0.0027
13-wk diff	0.2303 (0.2333)	-0.0191 (0.0596)	0.0082 (0.0099)	-0.0044	-0.0570 (0.3084)	-0.0008 (0.0593)	-0.0058 (0.0147)	-0.0062
BeanOil		Cattle			Cocoa			
	const	$r_{t-1}$	$X_{t-1}$	$\bar{R}^2$	const	$r_{t-1}$	$X_{t-1}$	$\bar{R}^2$
level	8.9077 (7.7142)	0.0098 (0.0576)	-0.0058 (0.0051)	-0.0024	4.0293 (6.8256)	-0.0628 (0.0574)	-0.0024 (0.0042)	-0.0013
1-wk diff	0.1748 (0.2282)	-0.1026 (0.0943)	0.1034 (0.0701)	0.0006	0.0746 (0.1200)	-0.1521 (0.0966)	0.0717 (0.0640)	0.0017
13-wk diff	0.1801 (0.2314)	0.0046 (0.0591)	0.0024 (0.0097)	-0.0065	0.0740 (0.1204)	-0.0738 (0.0581)	0.0069 (0.0077)	0.0002
Coffee		Cotton			FedCattle			
	const	$r_{t-1}$	$X_{t-1}$	$\bar{R}^2$	const	$r_{t-1}$	$X_{t-1}$	$\bar{R}^2$
level	3.8530 (9.2057)	-0.0329 (0.0579)	-0.0024 (0.0059)	-0.0050	2.3353 (11.7130)	0.0644 (0.0586)	-0.0014 (0.0075)	-0.0027
1-wk diff	0.1362 (0.2358)	-0.0011 (0.1246)	-0.0293 (0.0955)	-0.0052	0.1601 (0.2691)	-0.2249 (0.1287)	0.2530* (0.1013)	0.0176
13-wk diff	0.1454 (0.2367)	-0.0290 (0.0591)	-0.0054 (0.0115)	-0.0048	0.1482 (0.2718)	0.0563 (0.0600)	0.0046 (0.0112)	-0.0022
Hogs		KCWheat			Sugar			
	const	$r_{t-1}$	$X_{t-1}$	$\bar{R}^2$	const	$r_{t-1}$	$X_{t-1}$	$\bar{R}^2$
level	-10.9569 (9.5152)	0.0530 (0.0584)	0.0069 (0.0061)	0.0018	9.0292 (12.0041)	0.0269 (0.0579)	-0.0053 (0.0071)	-0.0043
1-wk diff	-0.1522 (0.1992)	0.1016 (0.0946)	-0.0352 (0.0722)	-0.0017	0.0755 (0.2848)	-0.0062 (0.1091)	0.0263 (0.0836)	-0.0059
13-wk diff	-0.1394 (0.1994)	0.0510 (0.0591)	0.0104 (0.0102)	0.0010	0.0662 (0.2853)	0.0152 (0.0592)	0.0065 (0.0113)	-0.0051

Notes to Table 1. OLS coefficients (with standard errors in parentheses) for regressions (11), (12), and (13), for  $X_{t-1} = \tilde{x}_{t-1}$  for the level rows,  $X_{t-1} = (\tilde{x}_{t-1} - \tilde{x}_{t-2})$  for the 1-wk diff rows, and  $X_{t-1} = (\tilde{x}_{t-1} - \tilde{x}_{t-14})$  for the 13-wk diff rows. All regressions estimated April 11, 2006 to January 3, 2012.

Table 2: Average returns during index-fund roll versus normal times

	1 <sup>st</sup> contract		2 <sup>nd</sup> contract		spread	
Beans	0.0195 (0.0523)	0.3710* (0.1513)	-0.0015 (0.0481)	0.3720* (0.1392)	-0.0211 (0.0178)	0.0010 (0.0515)
Wheat	-0.0069 (0.0701)	-0.0619 (0.2028)	-0.0116 (0.0664)	-0.0861 (0.1920)	-0.0046 (0.0113)	-0.0242 (0.0327)
Corn	0.0164 (0.0626)	0.0509 (0.1811)	0.0112 (0.0601)	0.0550 (0.1740)	-0.0052 (0.0118)	0.0041 (0.0343)
BeanOil	0.0131 (0.0480)	0.2267 (0.1390)	0.0060 (0.0472)	0.1851 (0.1367)	-0.0071 (0.0059)	-0.0415 (0.0172)
Cattle	0.0260 (0.0268)	-0.0574 (0.0712)	-0.0111 (0.0259)	-0.0445 (0.0688)	-0.0371 (0.0127)	0.0129 (0.0337)
Cocoa	0.0043 (0.0565)	0.0958 (0.1632)	0.0056 (0.0537)	0.0406 (0.1553)	0.0013 (0.0159)	-0.0552 (0.0458)
Coffee	0.0339 (0.0521)	-0.0663 (0.1506)	0.0184 (0.0508)	-0.0529 (0.1468)	-0.0155 (0.0057)	0.0133 (0.0164)
Cotton	-0.0035 (0.0579)	0.0731 (0.1881)	0.0227 (0.0526)	-0.0987 (0.1705)	0.0249 (0.0225)	-0.1920 (0.0728)
FedCattle	0.0146 (0.0229)	-0.0646 (0.0526)	0.0166 (0.0264)	-0.0761 (0.0605)	0.0019 (0.0114)	-0.0115 (0.0260)
Hogs	-0.0542 (0.0385)	0.0896 (0.0942)	-0.0752 (0.0411)	0.2428* (0.1006)	-0.0210 (0.0256)	0.1532* (0.0627)
KCWheat	0.0135 (0.0624)	-0.0748 (0.1806)	0.0086 (0.0601)	-0.0924 (0.1739)	-0.0049 (0.0115)	-0.0176 (0.0334)
Sugar	-0.0309 (0.0690)	0.4393 (0.2241)	-0.0255 (0.0624)	0.3293 (0.2025)	0.0053 (0.0175)	-0.1099 (0.0569)
Oil	0.0282 (0.0808)	-0.1863 (0.1508)	0.0127 (0.0749)	-0.1425 (0.1399)	-0.0155 (0.0213)	0.0438 (0.0398)

*Notes to Table 2.* Coefficient estimates (standard errors in parentheses) from OLS estimation of (14) using daily data from April 11, 2006 to December 30, 2011.

Table 3: Tests for predictability of crude oil returns

Oil: CIT-Masters				
	const	$r_{t-1}$	$X_{t-1}$	$\bar{R}^2$
level	-5.4784 (11.1081)	-0.0314 (0.0582)	0.0030 (0.0063)	-0.0052
1-wk diff	-0.0760 (0.3117)	0.1006 (0.1151)	-0.1340 (0.1039)	-0.0004
13-wk diff	-0.2298 (0.3048)	-0.1171 (0.0606)	0.0440* (0.0111)	0.0438
Oil: CIT-regression				
	const	$r_{t-1}$	$X_{t-1}$	$\bar{R}^2$
level	-4.4562 (14.8859)	-0.0306 (0.0584)	0.0025 (0.0085)	-0.0057
1-wk diff	-0.1147 (0.3112)	-0.0472 (0.0964)	0.0191 (0.0767)	-0.0057
13-wk diff	-0.1337 (0.3025)	-0.1240* (0.0606)	0.0448* (0.0107)	0.0499

*Notes to Table 3.* OLS coefficients (with standard errors in parentheses) for regressions (11), (12), and (13). CIT-Masters uses  $\tilde{x}_{t-1} = \ln(\tilde{X}_{\text{crude.oil},t}^{\text{Masters}})$  from equation(17) and  $X_{t-1} = \tilde{x}_{t-1}$  for the level rows,  $X_{t-1} = (\tilde{x}_{t-1} - \tilde{x}_{t-2})$  for the 1-wk diff rows, and  $X_{t-1} = (\tilde{x}_{t-1} - \tilde{x}_{t-14})$  for the 13-wk diff rows. CIT-regression uses  $\tilde{x}_{t-1} = \ln(\tilde{X}_{\text{crude.oil},t}^{\text{all}})$  from equation(20). All regressions estimated April 11, 2006 to January 3, 2012.

Table 4: In-sample and post-sample predictability of crude oil and stock market returns

	In-sample				Post-sample MSE	
	const	$r_{t-1}$	$X_{t-1}$	$\bar{R}^2$	regression	random walk
Oil	-0.4858 (0.3937)	-0.1507* (0.0750)	0.0553* (0.0123)	0.0834	23.8206	21.9747
S&P500	-0.1332 (0.2043)	-0.0637 (0.0718)	0.0125* (0.0059)	0.0130	6.5597	6.3688

*Notes to Table 4.* In-sample: OLS coefficients (standard errors in parentheses) for regression (13) as estimated over April 11, 2006 to January 12, 2010, with  $X_{t-1} = (\tilde{x}_{t-1} - \tilde{x}_{t-14})$  for  $\tilde{x}_{t-1} = \ln(\tilde{X}_{\text{crude\_oil},t}^{\text{Masters}})$ . Oil regression uses weekly percentage change in near crude oil contract for  $r_t$  and  $r_{t-1}$ . S&P500 uses percentage change in S&P500 for  $r_t$  and  $r_{t-1}$ . Post-sample MSE for regression reports mean squared error over January 17, 2010 to January 3, 2012 using the historically estimated regression. Post-sample MSE for random walk reports the average squared value of  $r_t$  over January 17, 2010 to January 3, 2012.

Figure 1: Price of near crude oil contract (left scale) and number of crude oil contracts held by index traders as imputed by Masters' method (right scale).

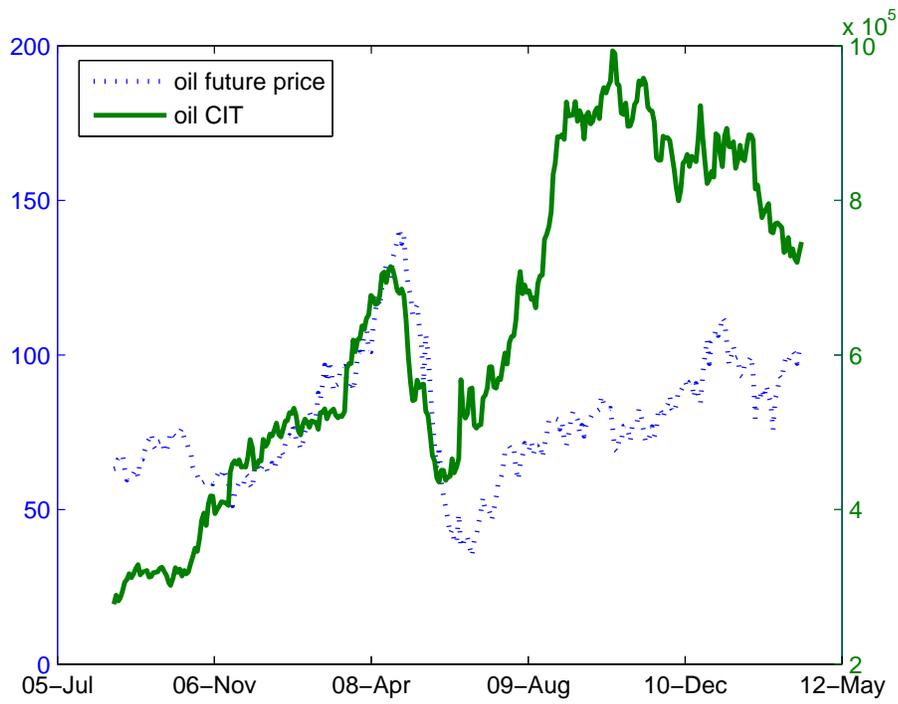
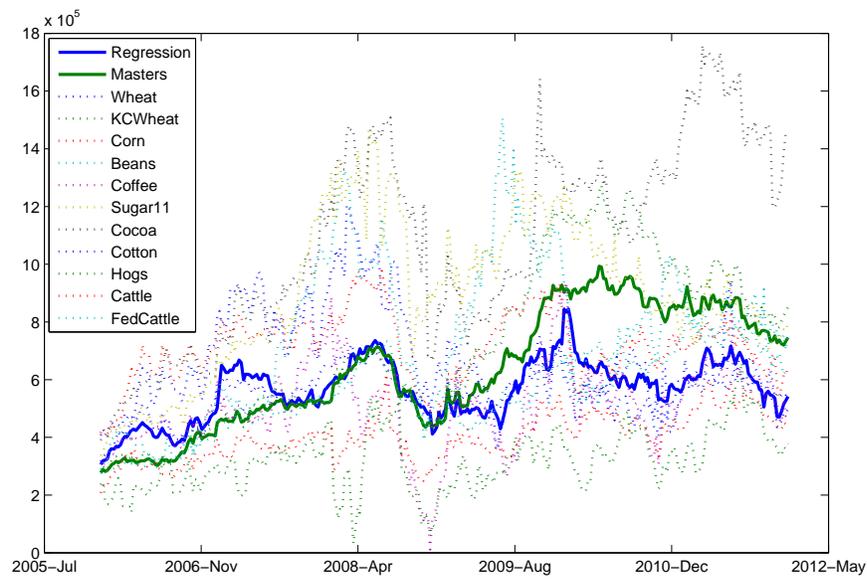


Figure 2: Holdings of crude oil contracts held by commodity index traders imputed by alternative methods



*Notes to Figure 2* Number of oil contracts held by index funds as imputed using Masters' method (equation (17)), regression method (equation(20)), and bivariate inferences using soybean oil and one other commodity as specified in equation(19).